

1 **APPROXIMATE CALCULATION OF THERMODYNAMIC CHARACTERISTICS OF**
2 **CALCIUM CRYSTALLINE COMPOUNDS AND COPPER, ZINC AND COBALT**
3 **COMPOUNDS**
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7 **ABSTRACT**

In this article the relationship between the entropies of crystalline calcium compounds and copper, zinc and cobalt compounds were analyzed. Thermal capacity dependence of temperature for acidic phosphates of copper, zinc and cobalt, determining value of enthalpy and entropy of copper, zinc and cobalt phosphates have been determined and the possibility to conduct thermodynamic analysis of reactions for their formation were established. Accordingly the data of thermodynamic analysis of temperature conditions for obtaining double superphosphate, the most formation of monosubstituted phosphates of copper, zinc and cobalt, and possibility of formation disubstituted of copper phosphates.

8 **Keywords:** double superphosphate, thermodynamics, microelements, phosphates, enthalpy,
9 entropy, thermal capacity, mineral fertilizers, microfertilizers, phosphates of copper, zinc and
10 cobalt.
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12 **1. INTRODUCTION**

13 Intensive research in the field of microelement containing compounds is due to the progress
14 and satisfaction of needs the modern field of agriculture and technology, the development of new
15 and improvement of real methods for obtaining mineral fertilizers. Of particular interest to
16 microelement containing compounds in practical aspect, is associated with the production of new
17 mineral microelement containing complex fertilizers.

18 Researching of many years conducted in our country and abroad, established that the use of
19 fertilizers containing trace elements (zinc, copper, molybdenum, boron, manganese, cobalt),
20 increases plant yields and improves the quality of agricultural products [1]. When microelements
21 interact with the main components of mineral fertilizers, different processes may occur with
22 formation of new compounds, therefore the study of the physicochemical properties of new
23 substances is of great importance.

24 Thermodynamic values of many elements, chemical compounds, ions, and minerals are either
25 absent or have a considerable precision in their values in reference books and scientific literatures.
26 The main requirements for thermodynamic properties are considered to be their reliability in critical
27 analysis, assessment of determination method, mutually consistency and etc. Therefore, the feature
28 of research is use of available reference dates about of thermodynamic properties of elements,
29 chemical compounds for purpose of subsequent determination of various correlations and functions,
30 using different calculation methods [2].

31 **2. STATEMENT OF RESEARCH**

32 In this aspect, the method of M.Kh. Karapetyanes gives the following relationship between
33 the entropies of crystalline calcium compounds and compounds of copper, zinc, and cobalt (Figure
34 1-3).

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$$S^{\circ}_{298\text{CuX}} = 3,517 S^{\circ}_{298\text{CaX}} + 25,202 \quad (1)$$

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$$S^{\circ}_{298\text{ZnX}} = 3,852 S^{\circ}_{298\text{CaX}} + 11,639 \quad (2)$$

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$$S^{\circ}_{298\text{CoX}} = 3,643 S^{\circ}_{298\text{CaX}} + 17,208 \quad (3)$$

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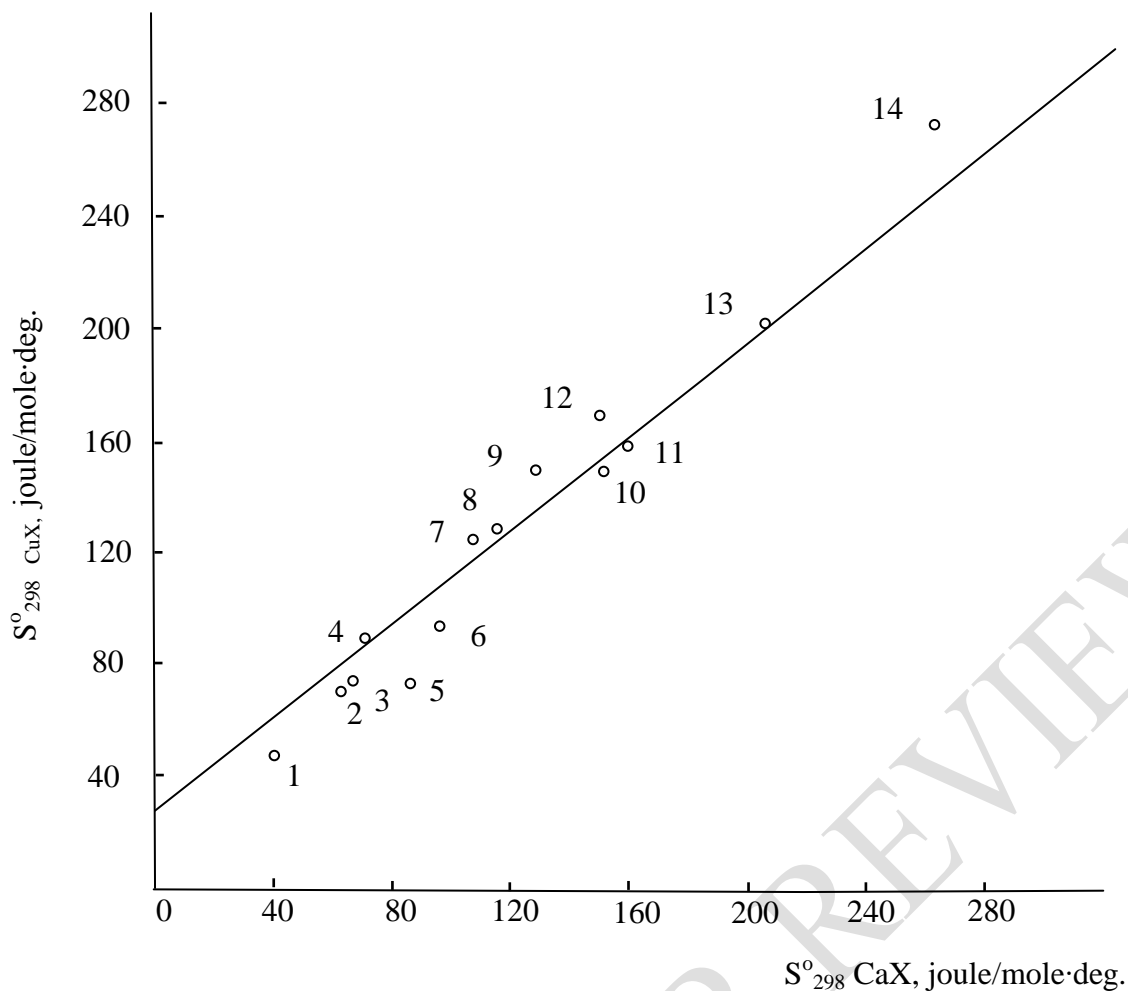


Fig. 1. Comparison of standard entropies of crystalline compounds of copper and calcium (M = Cu or Ca): 1-MO, 2-MS, 3-MSeO₄, 4-MF₂, 5-M(OH)₂, 6-MCO₃, 7-MCl₂, 8-MSO₄, 9-MMoO₄, 10-MFe₂O₄, 11-MWO₄, 12-MI₂, 13-M(NO₃)₂

V.A. Kireev [3] showed that when comparing the entropy of analogous compounds of sodium and magnesium, related to 2 g/eq. of compound, the difference of S°_{298} varies between 45.39-70.34 joule/mole·deg.. Accordingly to Kelly's data of entropy increments, this difference should be to $\Delta = J S^{\circ}_{\text{Na}^+} - J S^{\circ}_{\text{Mg}^{2+}} = 2 \cdot 40.19 - 24.70 = 55.68$ joule/mole·degree.

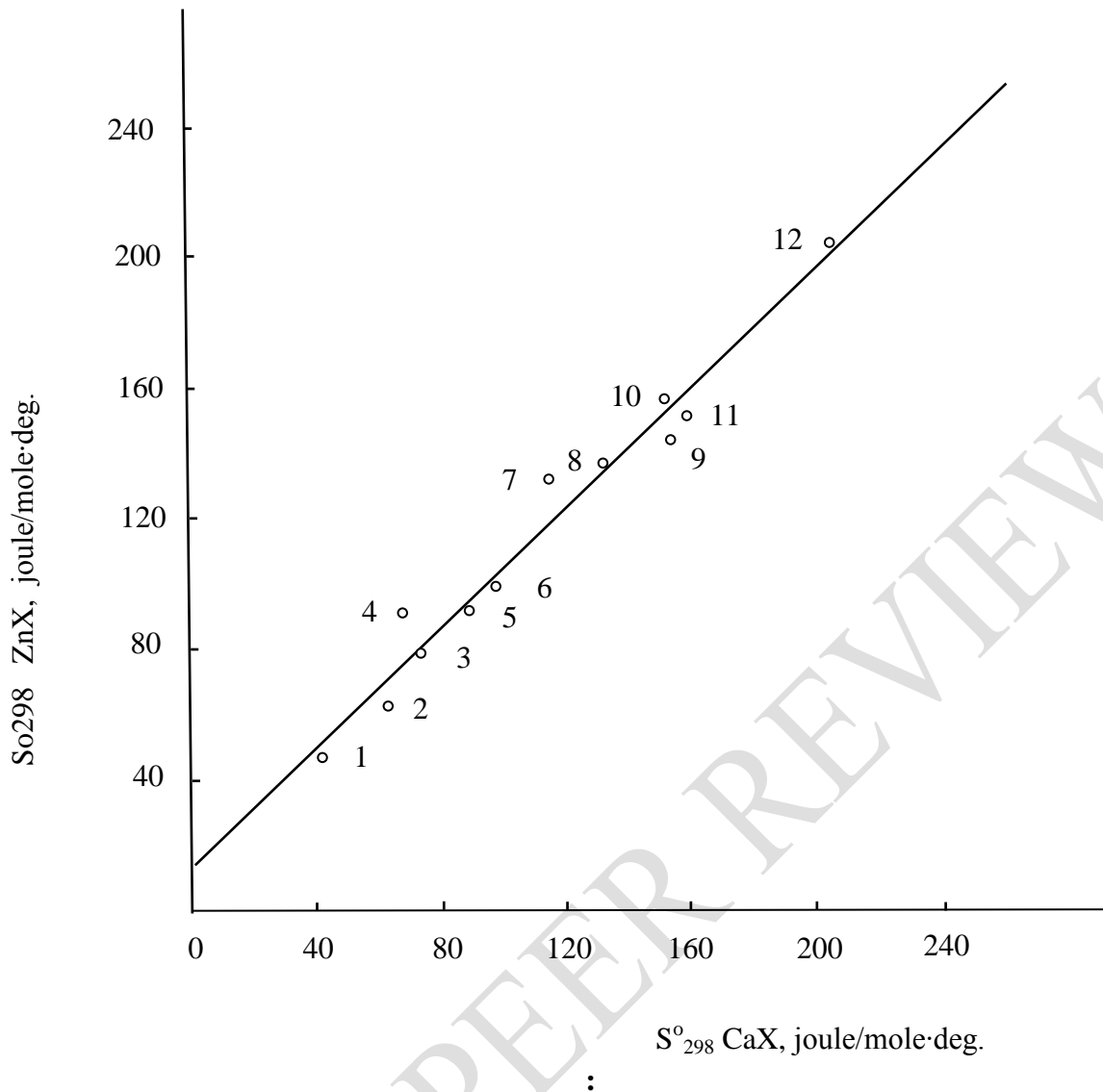


Fig.2. Comparison of standard entropies of crystalline zinc and calcium compounds (M = Zn or Co): 1-MO, 2-MS, 3-MF₂, 4-MSeO₄, 5-M(OH)₂, 6- MCO₃, 7-MSO₄, 8-MMoO₄, 9-MFe₂O₄, 10-MI₂, 11- MWO₄, 12-M(NO₃)₂.

On the base of mentioned below equalities we are calculated the S°_{298} phosphates of copper, zinc and cobalt using the entropy of calcium phosphates.

$$S^{\circ}_{298\text{CuX}} = S^{\circ}_{298\text{CaX}} + 3,768 \quad (4)$$

$$S^{\circ}_{298\text{ZnX}} = S^{\circ}_{298\text{CaX}} + 1,675 \quad (5)$$

$$S^{\circ}_{298\text{CoX}} = S^{\circ}_{298\text{CaX}} + 4,605 \quad (6)$$

The laboratory tests results are shown in Table 1. It is seen, the data obtained by independent methods are well congruent with each other, especially the values of S°_{298} found using by Kelly increments and Berthelot principle [4]. The Karapetyanes method gives somewhat lower results of entropy. It is seen from Figures 1-3, the scatter of points around straight lines is significant, therefore, the accuracy of equations 1-3, and hence the entropy values obtained by this method, is low.

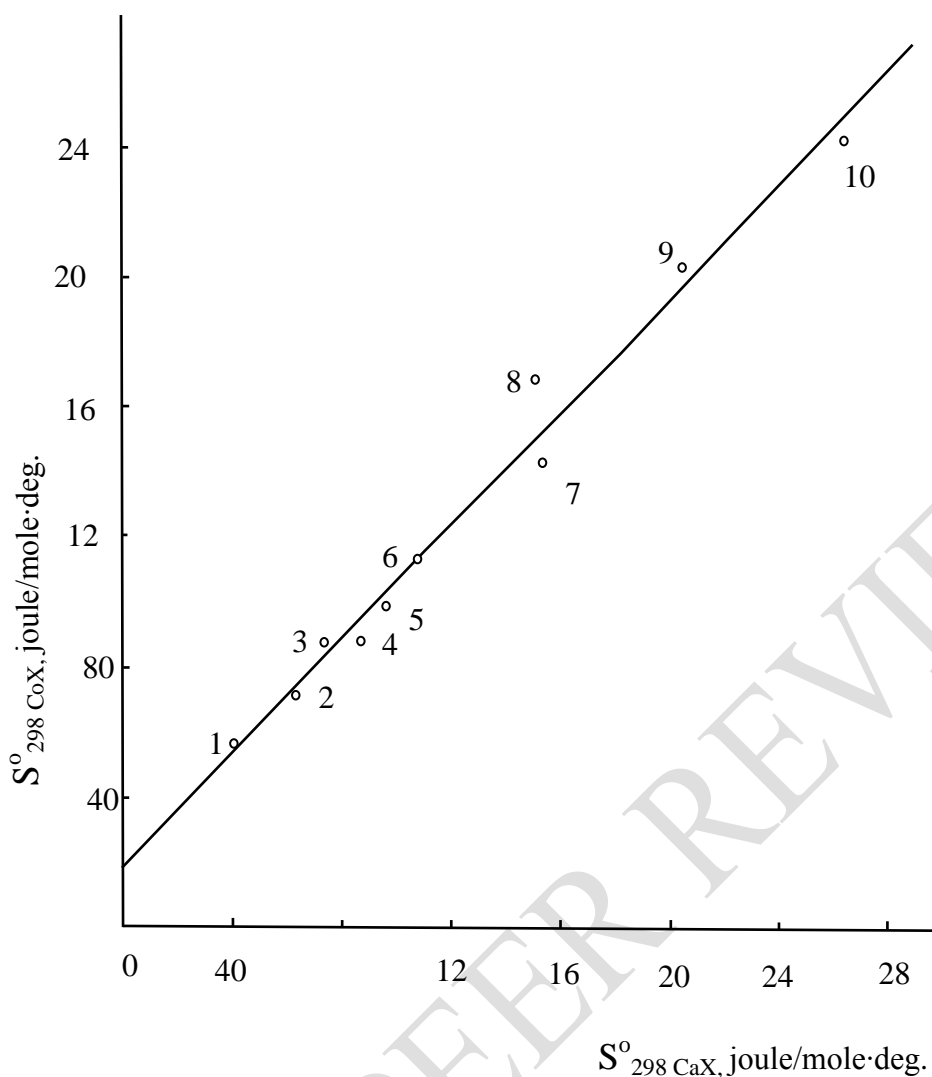


Fig.3. Comparison of standard entropies of crystalline compounds of cobalt and calcium (M = Co or Ca): 1- MO, 2-MS, 3-MF₂, 4-M(OH)₂, 5-MCO₃, 6-MCl₂, 7-MF₂O₄, 8-MI₂, 9-M(NO₃)₂, 10-MSeO₃·2H₂O

Previously has not been carried out an experimental study of heat capacity of copper, zinc, and cobalt phosphates. B.S. Kogan obtained equations for calculating the heat capacity of potassium phosphates and phosphoric acids at elevated temperatures using the method of I.L. Landia [5-6]. By the same method B.M. Beglov calculated the high-temperature heat capacities of condensed ammonium, lithium, rubidium and cesium phosphates [7]. We also used this method, which makes it possible to calculate the high-temperature heat capacities of substances according to their standard entropy.

Table 1. Results the calculation of entropy copper, zinc and cobalt phosphates

Compounds	J/mole-degree		
	Accordingly to Berthelot's method	Accordingly to Karapetyant's method	Accordingly to Kelly's increments
Cu(H ₂ PO ₄) ₂	194.31	183.59	193.43
CuHPO ₄	117.48	118.28	115.22
Cu ₃ (PO ₄) ₂	247.15	226.59	244.93
Cu ₂ P ₂ O ₇	195.48	183.38	193.22
Zn(H ₂ PO ₄) ₂	193.14	186.52	191.34
ZnHPO ₄	114.84	114.38	113.13
Zn ₃ (PO ₄) ₂	244.55	234.00	242.83
Zn ₂ P ₂ O ₇	192.89	186.31	191.13
Co(H ₂ PO ₄) ₂	191.76	182.59	194.27
CoHPO ₄	113.53	114.38	116.06
Co ₃ (PO ₄) ₂	240.25	227.51	245.77
Co ₂ P ₂ O ₇	191.55	182.42	194.02

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Calculation schemes for different groups of phosphates were different due to the specificity of the method and individual characteristics of the compounds. Dependence of heat capacity on temperature for acidic phosphates of copper, zinc and cobalt is determined [6], as for "complex oxygen compounds containing gaseous oxides (H₂O) and not having polymorphic transformations". It was also taken into account that they refer to inorganic compounds of hydrogen. The calculation procedure was carried out accordingly to well-known rules.

The results of calculation of heat capacity copper, zinc and cobalt phosphates are shown in Table 2.

Table 2. Temperature dependence of heat capacity of copper, zinc and cobalt phosphates

Compounds	S ^o ₂₉₈ , J/mole-degree	T, °K	C _{p298} , J/mole-degree	C _p ^o = a+BT+CT ² , J/mol-degree		
				a	B·10 ²	C·10 ⁻⁵
Cu(H ₂ PO ₄) ₂	194.31	1410	203.06	246.35	7.62	58.62
CuHPO ₄	117.48	1174	106.35	143.11	1.34	36.22
Cu ₃ (PO ₄) ₂	247.15	1117	186.80	282.23	3.60	31.86
Cu ₂ P ₂ O ₇	195.48	1194	214.45	239.23	2.97	29.94
Zn(H ₂ PO ₄) ₂	193.14	1429	202.31	245.43	7.58	58.36
ZnHPO ₄	114.84	1201	105.76	134.10	2.93	32.95
Zn ₃ (PO ₄) ₂	244.55	1128	257.11	282.19	3.56	31.74
Zn ₂ P ₂ O ₇	192.83	1211	214.36	239.02	2.97	29.77
Co(H ₂ PO ₄) ₂	191.76	1439	201.89	244.84	7.58	58.16
CoHPO ₄	113.55	1215	105.51	133.64	2.93	32.78
Co ₃ (PO ₄) ₂	243.25	1135	257.07	281.86	3.60	31.53
Co ₂ P ₂ O ₇	191.55	1219	214.36	239.11	2.93	29.73

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The high-temperature heat capacities of triple-substituted phosphates and pyrophosphates of microelements were calculated accordingly [6], as for ionic oxygen compounds consisting of solid oxides that do not have polymorphic transformations and are suitable for thermal characteristics under the column "other cases".

The obtained equations are valid in temperature range from 298°K to decomposition

205 temperature of adequate phosphate.

206 **3. RESULTS AND DISCUSSION**

207 Having determined the enthalpy and entropy of copper, zinc, and cobalt phosphates, we were
208 able to perform thermodynamic analysis of reactions for their formations.

209 Thermodynamic analysis makes it possible to predetermine possibility of particular reaction
210 and, therefore, the salt composition of final products, which is extremely complicated due to the
211 complexity of the initial and final products. Therefore, reactions of copper, zinc and cobalt sulfate
212 interactions with orthophosphoric acid and monocalcium phosphate, i.e., those which are possible in
213 process of obtaining double superphosphate containing microelements, were subjected to analysis.
214 For each reaction, we found values of isobaric-isothermal potential and discussed by it about
215 possibility of particular reaction (negative value of ΔG).

216 Thermodynamic calculations of possibility the formation of phosphates of microelements in
217 the process for obtaining double superphosphate were carried out using the simplified formula $\Delta G =$
218 $\Delta H - T\Delta S$ without heat capacities. The results obtained are presented in Table 3.

219 Thermodynamic analysis showed that sulfate salts of copper, zinc and cobalt behave
220 differently in reactions with phosphoric acid and monocalcium phosphate. As can be seen from
221 table 3, sulfates of microelements at 25°C should not interact with phosphoric acid. With an
222 increase the temperature, the probability of reactions increases and starting from 59.3°C, only
223 formation twice-substituted copper phosphate. For formation of twice-substituted phosphates of
224 zinc and cobalt, higher temperature is required.

225 In the interaction of copper sulfate, zinc and cobalt with monocalcium phosphate, is possible
226 formation of monosubstituted and twice-substituted metal phosphates. Thermodynamically more
227 likely is formation of monosubstituted phosphates of copper, zinc and cobalt, the isobaric-
228 isothermal potential of reactions (1) and (6) has more negative value.

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Table 3. Thermodynamic characteristics of reactions of formation of microelements phosphates

№	Reactions	ΔH°_{298} kJ/mole	ΔS°_{298} j/mole·degree	ΔG°_{298} kJ/mole	ΔG°_{353} kJ/mole	T, °K
1.	$\text{CuSO}_4 \cdot 5\text{H}_2\text{O} + 2\text{H}_3\text{PO}_4 = \text{Cu}(\text{H}_2\text{PO}_4)_2 + \text{H}_2\text{SO}_4 + 5\text{H}_2\text{O}$	18.98	26.21	11.17	9.67	997.15
2.	$\text{CuSO}_4 \cdot 5\text{H}_2\text{O} + \text{H}_3\text{PO}_4 = \text{CuHPO}_4 + \text{H}_2\text{SO}_4 + 5\text{H}_2\text{O}$	19.76	42.52	1.45	-0.88	332.31
3.	$\text{CuSO}_4 \cdot 5\text{H}_2\text{O} + \text{Ca}(\text{H}_2\text{PO}_4)_2 = \text{Cu}(\text{H}_2\text{PO}_4)_2 + \text{CaSO}_4 + 5\text{H}_2\text{O}$	-0.43	38.89	-12.02	-14.94	8.94
4.	$\text{CuSO}_4 \cdot 5\text{H}_2\text{O} + \text{Ca}(\text{H}_2\text{PO}_4)_2 = \text{CuHPO}_4 + \text{CaSO}_4 + \text{H}_3\text{PO}_4 + 5\text{H}_2\text{O}$	10.34	55.20	-6.11	-10.26	187.32
5.	$\text{ZnSO}_4 \cdot 7\text{H}_2\text{O} + 2\text{H}_3\text{PO}_4 = \text{Zn}(\text{H}_2\text{PO}_4)_2 + \text{H}_2\text{SO}_4 + 7\text{H}_2\text{O}$	22.66	37.99	11.34	9.25	596.47
6.	$\text{ZnSO}_4 \cdot 7\text{H}_2\text{O} + \text{H}_3\text{PO}_4 = \text{ZnHPO}_4 + \text{H}_2\text{SO}_4 + 7\text{H}_2\text{O}$	25.12	54.28	9.08	6.09	462.79
7.	$\text{ZnSO}_4 \cdot 7\text{H}_2\text{O} + \text{Ca}(\text{H}_2\text{PO}_4)_2 = \text{Zn}(\text{H}_2\text{PO}_4)_2 + \text{CaSO}_4 + 7\text{H}_2\text{O}$	3.25	50.67	-11.85	-14.64	64.14
8.	$\text{ZnSO}_4 \cdot 7\text{H}_2\text{O} + \text{Ca}(\text{H}_2\text{PO}_4)_2 = \text{ZnHPO}_4 + \text{CaSO}_4 + \text{H}_3\text{PO}_4 + 7\text{H}_2\text{O}$	15.84	66.96	-4.11	7.80	236.56
9.	$\text{CoSO}_4 \cdot 7\text{H}_2\text{O} + 2\text{H}_3\text{PO}_4 = \text{Co}(\text{H}_2\text{PO}_4)_2 + \text{H}_2\text{SO}_4 + 7\text{H}_2\text{O}$	23.66	40.36	11.63	9.431	586.22
10.	$\text{CoSO}_4 \cdot 7\text{H}_2\text{O} + \text{H}_3\text{PO}_4 = \text{CoHPO}_4 + \text{H}_2\text{SO}_4 + 7\text{H}_2\text{O}$	5.46	56.67	8.57	5.46	449.27
11.	$\text{CoSO}_4 \cdot 7\text{H}_2\text{O} + \text{Ca}(\text{H}_2\text{PO}_4)_2 = \text{Co}(\text{H}_2\text{PO}_4)_2 + \text{CaSO}_4 + 7\text{H}_2\text{O}$	4.25	53.04	-11.56	-14.47	80.13
12.	$\text{CoSO}_4 \cdot 7\text{H}_2\text{O} + \text{Ca}(\text{H}_2\text{PO}_4)_2 = \text{CoHPO}_4 + \text{CaSO}_4 + \text{H}_3\text{PO}_4 + 7\text{H}_2\text{O}$	16.05	69.35	-4.62	-8.43	231.44

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234 **4. CONCLUSION**

235 Thus, dates of thermodynamic analysis indicate that under the temperature conditions of obtaining
236 double superphosphate, the formation of mono-substituted phosphates of copper, zinc, and cobalt is
237 most likely and is possible the formation of twice- substituted copper phosphates.

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240 **Authors have declared that no competing interests exist. The products used for this**
241 **research are commonly and predominantly use products in our area of research and**
242 **country. There is absolutely no conflict of interest between the authors and producers of**
243 **the products because we do not intend to use these products as an avenue for any**
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