Original Research Article

COMPARATIVE STUDY OF FAILURE RATE OF BANK'S ATM : LOG NORMAL DISTRIBUTION APPRAOCH

ABSTRACT

This research determined time to failure rate and number of successful transaction of selected banks in Nigeria, using Log normal distribution. Transformation technique was applied to the log-normal model to obtain a quadratic equation or polynomial regression that assisted in determining the parameters of the log-normal model. Also, one-way ANOVA was used to test for equality of the mean (or average) time to failure rate and mean number of successful service time of the banks. The research fitted the log-normal models of the banks and the result showed that GT-Bank model has the highest variation of 90.3% for number of successful service time (t), while Fidelity bank model has the highest variation of 56.6% for time of failure rate with the help of SPSS 21 statistical software. The one-way ANOVA result of the number of successful service time (min) showed a significant difference. The Tukey comparison tests showed that GT bank is significant at (5% or 10%) from others while UBA bank is significant at 10% from others. Hence, the number of successful service time (min) was the same for other banks except UBA). The one- way ANOVA result of the banks in number of Time to Failure (t) (min) showed no significant difference among the five banks.

Key words: Failure rate and successful transaction, Log normal distribution, Transformation, polynomial regression, ANOVA, Tukey comparison tests

1.0 INTRODUCTION

Reliability of an equipment or machine is the probability that it will work and serve well for a specified period of time. This probability is modeled as a lifetime distribution.

Linear regression is a popular statistical tool that has been used successfully in many areas including survival analysis. In survival analysis, a log-transformation of the response

variable converts a conventional linear model to an accelerated failure time model, which is an appealing alternative to the Cox (1972) proportional hazards model because of its direct interpretation (cf. Reid 1994).

According to Grambsch, and Therneut (2000), survival analysis deals with time to an event in system. An event can be death in biological system and failure in technical system. Often the time to an event is not known exactly but is known to fall in some interval, this phenomenon is called censoring which could be random or non-informative in analytical approach. There are three main types of censoring, right, left and interval. If the event occur beyond the end of the study, then the data is right censored. Left censored data occurs when the event is observed, but the exact event time is unknown. Interval censoring means that individuals come in and out of observation and are missing. Most survival analytic method are designed for right censored observation.

The traditional regression methods are not equipped to handle censored data due to the fact that the time to event is restricted and is assumed to have a skewed distribution, and there is need to employ a statistical method that put into consideration the restriction caused by survival data.

One well known and widely applied method is the use of log-normal regression model. It is used to predict response variable or to estimate the mean of the response variable of the original scale for a new set of covariate values. (Haipeng, S and Zhengyuan Z. 2007). In probability theory, a log-normal distribution is a continuous probability distribution of a random variable whose logarithm is normally distributed. Thus, if the random variable x is log-normally distributed, then y = In(x) has a normal distribution. Alternatively, if y has a normal distribution, then the exponential function of y, x = exp(y), has a log-normal distribution. A random variable which is log-normally distributed takes only positive real values. The distribution is occasionally referred to as the Galton distribution.

The log-normal distribution is a statistical distribution of random variable that has a normally distributed logarithm. Log-normal distribution can model a random variable x, where log x is normally distributed. These distribution, under multiplication and division, are self replicating. It is useful for modeling data that are skewed with low mean value and large variance. The log-normal distribution has been called the most commonly used life distribution model for any technology application. Stahel et al., (2014).

Several studies have been done in the areas of log-normal distribution, log-normal regression, analysis of variance to test the equality of several mean. Some of such studies are the works of Kenneth (2011), Serfling (2002), Christopher et al (2015), Mehta et al (2017). Osborne, (2010), Rama, (2015), Akbar et al (2016), Maria et al (2016), Stefano and Toscani (2018), and many more.

However, failure of automated teller machines in banks is rampant and frustrating. These has cause unnecessary delays in cash withdrawals as well as other activities cash may have been used for. This calls for measures to mitigate the failure rates of ATM and to do this, the time to failure rate needs to be ascertained first and consequently put under control. Hence the study seeks to analyze the time to failure rate and successful transaction of different banks by fitting their log-normal model of successful transaction before failure of each ATM occurs, fitting a log-normal model of time to failure of automated teller machine of different banks, determining the time to failure rate and number of successful transaction in each bank, and determining the analysis of variance with log-normal data to test the equality of the mean (Average successful transaction) of the different banks.

Section 2 is the scope and limitation of study, section three and four are the research design and methodology respectively. Data analysis and interpretation of results, summary and conclusions are presented in section five, six and seven respectively.

2. SCOPE/ DELIMITATION OF THE STUDY

The study is carried out in five different banks in Port Harcourt ATM randomly selected by the use of simple random sampling technique. Twenty observations of time to failure and number of successful service time before failure were taken from each of the selected Automated Teller Machine. The nature of failure considered was out of cash and out of network or service and as such may not be extended to other source of failure. Hence the study only covers the following banks in Port Harcourt.

- 1. First Bank, East/West Road Rumuokoro
- 2. GT Bank, East/West Road Rumuokoro
- 3. UBA Bank, East/West Road, Port Harcourt
- 4. Ecobank, East/West Road Rumuokoro
- 5. Fidelity Bank, East/West Road Rumuokoro

3. Research Design

Primary data was collected from each of the banks. The number of successful transaction (y), successful service time (t) (min) and time to failure (t) (min) of five banks were obtained as shown below:

Tabe 3.1 DATA ON FIRST BANK SERVICE RECORD

Sample	No. of Successful	Successful Service Time (t)	Time to Failure (t) (min)
1	Transaction (Y)	(min)	2
1.	6	8	2
2.	10	14	3
3.	8	6	5
4.	12	18	10
5.	2	5	8
6.	5	4	2
7.	13	9	12
8.	4	12	2
9.	23	32	8
10.	9	6	22
11.	2	4	2
12.	11	20	32
13.	31	44	14
14.	29	38	19
15.	17	21	5
16.	14	38	33
17.	16	12	2
18.	20	46	28
19.	11	8	2
20.	13	12	8

Table 3.2: DATA ON GT BANK SERVICE RECORD

Sample	No. of successful Transaction (Y)	Successful Service Time (t) (min)	Time to Failure (t) (min)
1.	6	11	10
2.	10	16	5
3.	8	10	2
4.	15	26	3
5.	18	30	5
6.	12	22	2
7.	24	36	1
8.	18	24	1
9.	28	42	2
10.	3	4	6
11.	14	30	12
12.	19	46	12
13.	21	28	18
14.	34	46	8
15.	20	23	4
16.	27	49	32
17.	32	51	2
18.	13	27	4
19.	16	30	40
20.	17	28	7

Table 3.3: DATA ON FIDELITY BANK SERVICE RECORD

Sample	No. of Successful Transaction (Y)	Successful Service Time (t) (min)	Time to Failure (t) (min)
1.	3	4	1
2.	6	8	2
3.	4	3	2
4.	11	9	12
5.	18	22	10
6.	8	15	3
7.	14	14	5
8.	19	22	14
9.	10	18	21
10.	13	24	11
11.	23	32	12
12.	25	37	2
13.	27	41	32
14.	12	20	24
15.	12	22	8
16.	26	41	34
17.	21	40	32
18.	28	52	38
19.	30	58	40
20.	15	28	12

Table 3.4: DATA ON ECOBANK SERVICE RECORD

Sample	No. of Successful Transaction (Y)	Successful Service Time (t) (min)	Time to Failure (t) (min)
1.	2	9	3
2.	4	12	4
3.	12	18	14
4.	6	8	2
5.	11	10	2
6.	17	13	1
7.	8	4	12
8.	22	33	11
9.	18	14	6
10.	28	36	19
11.	8	12	2
12.	24	29	21
13.	9	11	5
14.	30	27	4
15.	19	14	24
16.	16	18	13
17.	23	19	4
18.	35	48	22
19.	14	9	1
20.	17	8	9

Table 3.5 DATA ON UBA BANK SERVICE RECORD

Sample	No. of Successful Transaction (Y)	Successful Service Time (t) (min)	Time to Failure (t) (min)
1.	4	8	2
2.	12	5	1
3.	9	11	3

4.	18	24	20
5.	3	5	2
6.	12	13	1
7.	6	9	2
8.	11	7	10
9.	24	32	8
10.	22	12	2
11.	15	9	27
12.	14	12	4
13.	7	15	12
14.	9	8	6
15.	13	11	9
16.	19	28	5
17.	32	43	30
18.	26	34	5
19.	10	12	3
20.	18	33	14

4. **methodology**: The Lognormal Distribution

Let x_1, x_2 - - - xn be independent positive random variable such that

$$Tn = \prod_{i=1}^{n} xi \qquad . \tag{1}$$

Then the log of their product is equivalent to the sum of their logs

In Tn =
$$\sum_{i=1}^{n} In(xi)$$
 . (2)

The following four assumptions are implicit in the use of the Lognormal distribution. These are;

- 1. Stochastically independent
- 2. Normally distributed
- 3. Constant variance
- 4. Mean equal to zero.

Therefor, if Z = log(x) is normally distributed, then the distribution of x is called a log-normal distribution. The probability density function is given as;

> 0

 $t \in (0, \infty)$

Where x = t

$$Mean = exp^{(\mu + \delta^{\frac{2}{2}})}$$

Variance = $exp[(\delta^2) - 1] exp^{[2\mu + \delta^2]}$ and

The cumulative density function is given as

CDF =
$$\frac{1}{2} + \frac{1}{2} exp^{\frac{[In(t)-\mu]}{\sqrt{2\delta}}}$$

 $f(t) = \frac{1}{t\delta\sqrt{2\pi}} exp^{\frac{-(In(t)-\mu)^2}{2\delta^2}}$

Taking natural logarithm to base e on both sides

$$In f(t) = In \left(t\delta\sqrt{2\pi}\right)^{-1} - \frac{(Int-\mu)^2}{2\delta^2}$$

$$In f(t) = -In \left(t\delta\sqrt{2\pi}\right) - \frac{(Int-\mu)^2}{2\delta^2}$$

$$In f(t) = -In(t) - In(\delta \sqrt{2\pi}) - \frac{1}{2\delta^2} \left[(Int)^2 - 2\mu In(t) + \mu^2 \right]$$

$$Inf(t) = -In(t) - In\left(\delta\sqrt{2\pi}\right) - \frac{(Int)^2}{2\delta^2} + \frac{\mu}{\delta^2} + \frac{\mu}{\delta^2} In(t) - \frac{\mu^2}{2\delta^2}$$

Collect like terms

$$Inf(t) = -\left(\delta\sqrt{2\pi}\right) - \frac{\mu^2}{2\delta^2} + \frac{\mu}{\delta^2} In(t) - In(t) - \frac{(Int)^2}{2\delta^2}$$

$$= - \left[In \left(\delta \sqrt{2\pi} \right) + \frac{\mu^2}{2\delta^2} \right] + \left(\frac{\mu}{\delta^2} - 1 \right) In(t) - \frac{1}{2\delta^2} (Int)^2$$

$$Inf(t) = \beta_0 + \beta_1 In(t) + \beta_2 (In(t))^2$$

where

$$y = Inf(t)$$

$$x = In(t)$$
 and $x^2 = [In(t)]^2$

Then, from equation 4, obtain that

$$\beta_0 = -\left[In\left(\delta\sqrt{2\pi}\right) + \frac{\mu^2}{2\delta^2}\right]$$

$$\beta_1 = \left(\frac{\mu}{\delta^2} - 1\right)$$

$$\beta_2 = -\frac{1}{2\delta^2}$$

Equation 4 is a quadratic regression model or curvilinear model.

4.1 Parameter Estimation using Regression Techniques

A multiple linear regression model with K predictor variable (independent variables) x_1 , x_2 - - - x_k and a response variable (dependent variable) y was a generization in equation 4, then, the normal equation matrix can be written as

$$(\hat{B}_0 \hat{B}_1 \hat{B}_2) = \begin{bmatrix} n & \Sigma x_1 & \Sigma x_2 & \Sigma x_1 & \Sigma x_1^2 & \Sigma x_1 x_2 & \Sigma x_2 & \Sigma x_1 x_2 & \Sigma x_2^2 \end{bmatrix} \begin{bmatrix} \Sigma y & \Sigma x_1 y & \Sigma x_1 y & \Sigma x_2 & \Sigma x_1 & \Sigma x_2 & \Sigma x_1 & \Sigma x_2 & \Sigma x_2 & \Sigma x_1 & \Sigma x_2 & \Sigma x_2 & \Sigma x_1 & \Sigma x_2 & \Sigma x_1 & \Sigma x_2 & \Sigma x_2$$

. . . 5

$$^{\land} B = (x^1 x)^{-1} (x^1 y)$$

Where
$$x_1 = x = In (t)$$

 $x_2 = x^2 = [In (t)]^2$

 $\hat{\ }B_0,\ \hat{\ }B_1$ and $\hat{\ }B_2$ are the parameter estimate.

4.2 One – way ANOVA (Analysis of variance)

The ANOVA is used to measure the difference between variation amongst samples and variation within samples. It is a ratio of the variation between samples to the variation within sample which is based on the F-ratio. The model of the one-way ANOVA is

$$x_{ii} = \mu + x_i + e_{ii}$$

$$y_{ij} N(N_y, \delta_y^2)$$

$$x_i N (0, \delta_x^2)$$

$$e_i$$
 N $(0, \delta_e^2)$

Where

 x_{ij} denote the jth observation from ith treatment

 μ is the mean of the observation

 x_i is fixed effects of the model

 e_{ij} is the error term or the disturbance

4.2.1 Identifying sum of squares

Total sum of squares TSS
$$n \sum i = 1$$
 $n \sum j = 1$ $\left(x_{ij} - \overline{x}\right)^2 = k \sum i = 1$ $n \sum j = 1$ $x_{ij}^2 - \frac{T^2}{nk}$

Between sum of squares (BSS) = $\frac{1}{n}$ $k \sum i = 1$ $Ti.^2 - \frac{T^2}{nk}$ Within sum of squares (WSS) = $\frac{1}{k}$ $n \sum j = 1$ $T_{-j}^2 - \frac{T^2}{nk}$

4.2.2 One-Way ANOVA Table

Source of variation	Sum of	Degree of	Mean square	F-ratio
	squares	freedom		
Between samples (treatment)	BSS	<i>k</i> − 1	$MSB = \frac{BSS}{K-1}$	MSB MSN
Within samples (Error)	WSS	k(n-1)	$MSW = \frac{WSS}{K(n-1)}$	
Total	TSS	(nk-1)		

4.2.3 Hypothesis Test

Ho: $\mu_1 = \mu_2 = \mu_3 = \dots \mu_n$ (There is no significant difference in the mean successful transaction of the five different banks.

H1: Not all the μ 's are equal, i = 1, 2, ...n There is a significant difference in the mean successful transaction of the five different banks).

4.2.4 Sample size

A sample is a subset of population unit selected for the purpose of drawing conclusion about the entire population unit. The sample size was obtained using the Yale formula;

$$n = \frac{N}{1 + Ne^2} = 100/5 = 20$$

5. DATA ANALYSIS AND INTERPRETATIONS

In section four, Log-normal model parameters were derived for both number of successful service time (t) (min) and time to failure (t) (min). Thus, the parameters of the Log-normal model of five different banks were obtained in section 5.1 below with the help of SPSS 21 statistical software using data in table 3.1 to table 3.5 above.

5.1 Parameters Estimates of the Log-Normal Model of Five Banks, Using Regression Techniques

The parameters and R-squared of the five different banks for both number of successful service time (t) (min) and time to failure (t) (min) are in Appendix A and summarised in Table 5.1 below.

Table 5.1: Log-normal Models of Five Banks (Transformed models)

	Log-norn	nal Models	
Banks	Time of failure (t)	Number of successful Service time (t)	Remarks
Baliks	Parameters estimates±Standard error (R²)	Parameters estimates±Standard error (R²)	- Kemarks
	[Regr.ANOVA Values]	[Regr.ANOVA Values]	
First Bank	B ₀ =1.246±0.657 (25.8%) [0.080]	B ₀ =-0.906±1.245 (67.6%) [0.000]	SST
	B ₁ =0.875±0.791	B ₁ =1.791±1.003	
	B ₂ =-0.130±0.197	B ₂ =-0.193±0.189	
GT-Bank	B ₀ =3.091±0.346 (10.0%) [0.409]	B ₀ =-0.860±0.657 (90.3%) [0.000]	SST
	B ₁ =-0.564±0.422	B ₁ =0.843±0.479	
	B ₂ =-0.155±0.113	B ₂ =-0.100±0.085	
Fidelity Bank	B ₀ =1.515±0.334 (56.6%) [0.001]	B ₀ =3.233±1.285 (89.1%) [0.000]	SST
	B ₁ =0.628±0.372	B ₁ =0.551±0.073	
	B ₂ =-0.051±0.091	B ₂ =-0.066±0.087	
Eco-Bank	B ₀ =2.511±0.403 (28.7%) [0.057]	B ₀ =1.971±1.985 (47.8%) [0.004]	SST
	B ₁ =-0.558±0.549	B ₁ =-0.383±1.483	
	B ₂ =-0.258±0.160	B ₂ =-0.217±0.270	
UBA Bank	B ₀ =2.169±0.342 (22.1%) [0.120]	B ₀ =0.904±1.786 (55.8%) [0.001]	SST
	B ₁ =0.054±0.451	B ₁ =0.517±1.372	
	`B ₂ =-0.065±0.128	B ₂ =-0.035±0.252	

Footnote: SST- Successful Service Time

Recall, from Equation (3) that constants

$$\beta_0 = -\left[\ln\left(\sigma\sqrt{2\pi}\right) + \frac{\mu^2}{2\sigma^2}\right], \ \beta_1 = \left(\frac{\mu}{\sigma^2} - 1\right) \text{ and } \beta_2 = -\frac{1}{2\sigma^2}$$

Then, to determine the parameters of the Log-normal models (μ and σ^2)

$$\sigma^2 = -\frac{1}{2\beta_2}$$
 and $\mu = \sigma^2(\beta_1 + 1)$

Table 5.2: Log-normal Models Parameters of Five Banks (Variance, standard deviation and Mean)

	Log-normal Models				
	Time of failure (t) Number of successful Service time (t)				
Banks	Parameters	Parameters			
First Bank	$\sigma^2 = 3.85 \sigma = 1.96 \mu = 7.21$	$\sigma^2 = 2.59 \ \sigma = 1.61 \ \mu = 7.23$			

GT-Bank	$\sigma^2 = 3.23 \ \sigma = 1.80 \ \mu = 1.41$	$\sigma^2 = 5.00 \ \sigma = 2.24 \ \mu = 9.22$
Fidelity Bank	$\sigma^2 = 9.80 \ \sigma = 3.13 \ \mu = 15.96$	$\sigma^2 = 7.58 \ \sigma = 2.75 \ \mu = 11.75$
Eco-Bank	$\sigma^2 = 1.94 \sigma = 1.39 \mu = 0.86$	$\sigma^2 = 2.30 \ \sigma = 1.52 \ \mu = 1.42$
UBA Bank	σ^2 =7.69 σ = 2.77 μ =8.11	$\sigma^2 = 14.29 \ \sigma = 3.78 \ \mu = 21.67$

The Log-normal model of GT-Bank has the highest variation of 90.3% for number of successful service time (t), while the Log-normal model of Fidelity bank has the highest variation of 56.6% for time of failure rate.

The estimate Log-normal models are

$$f(t) = \frac{1}{t\sigma\sqrt{2\pi}}e^{\left(\frac{Lnt-\mu}{\sigma}\right)^2} = \frac{1}{2.24t\sqrt{2\pi}}e^{\left(\frac{Lnt-9.22}{2.24}\right)^2}$$
 for number of successful

service time (t)

$$f(t) = \frac{1}{t\sigma\sqrt{2\pi}}e^{\left(\frac{Lnt-\mu}{\sigma}\right)^2} = \frac{1}{3.13t\sqrt{2\pi}}e^{\left(\frac{Lnt-15.96}{3.13}\right)^2}$$
 for time of failure rate

5.3 One-Way ANOVA Successful Service Time (T) (Min) and Time to Failure (T) (Min) Between the Five Bank

The section is divided into two part, 1) one-way ANOVA successful service time (t) (min) and 2) one-way ANOVA time to failure (t) (min)

Table 5.3. One-Way ANOVA Successful Service Time (T) (Min) of the Five Banks ANOVA

 Successful Service Time (t) (min)

 Sum of Squares
 df
 Mean Square
 F
 Sig.

 Between Groups
 2486.340
 4
 621.585
 3.587
 .009

 Within Groups
 16460.250
 95
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Since p value of the one-way ANOVA is 0.009 which is less than the critical values of 0.05. we conclude that there is significant difference among the five banks number of successful service time (t).

Therefore, the LSD and Tukey comparison tests were done to identify the bank that is significant as shown below.

Table 5.4 multiple comparison test for successful service time LSD

Multiple Comparisons

Dependent Variable: Successful Service Time (t) (min)

LSD

(I) 1=First bank,	(J) 1=First bank,	Mean Difference	Std. Error	Sig.	95% Confide	nce Interval
2=GT Bank,	2=GT Bank,	(I-J)			Lower Bound	Upper Bound
3=Fidility,	3=Fidility,					
4=Ecobank, 5=	4=Ecobank, 5=					
UBA	UBA					
	2.00	-11.10000*	4.16252	.009	-19.3636	-2.8364
1.00	3.00	-7.65000	4.16252	.069	-15.9136	.6136
1.00	4.00	.25000	4.16252	.952	-8.0136	8.5136
	5.00	1.30000	4.16252	.755	-6.9636	9.5636
	1.00	11.10000*	4.16252	.009	2.8364	19.3636
2.00	3.00	3.45000	4.16252	.409	-4.8136	11.7136
2.00	4.00	11.35000*	4.16252	.008	3.0864	19.6136
	5.00	12.40000*	4.16252	.004	4.1364	20.6636
	1.00	7.65000	4.16252	.069	6136	15.9136
3.00	2.00	-3.45000	4.16252	.409	-11.7136	4.8136
3.00	4.00	7.90000	4.16252	.061	3636	16.1636
	5.00	8.95000^*	4.16252	.034	.6864	17.2136
	1.00	25000	4.16252	.952	-8.5136	8.0136
	2.00	-11.35000*	4.16252	.008	-19.6136	-3.0864
4.00	3.00	-7.90000	4.16252	.061	-16.1636	.3636
	5.00	1.05000	4.16252	.801	-7.2136	9.3136
	1.00	-1.30000	4.16252	.755	-9.5636	6.9636
5.00	2.00	-12.40000*	4.16252	.004	-20.6636	-4.1364
5.00	3.00	-8.95000*	4.16252	.034	-17.2136	6864
	4.00	-1.05000	4.16252	.801	-9.3136	7.2136

^{*.} The mean difference is significant at the 0.05 level.

Table 5.5 multiple comparison test for successful service time TUKEY HSD

Multiple Comparisons

Dependent Variable: Successful Service Time (t) (min)

Tukey HSD

(I) 1=First bank,	(J) 1=First bank,	Mean Difference	Std. Error	Sig.	95% Confide	nce Interval
2=GT Bank,	2=GT Bank,	(I-J)			Lower Bound	Upper Bound
3=Fidility,	3=Fidility,					
4=Ecobank, 5=	4=Ecobank, 5=					
UBA	UBA					
	2.00	-11.10000	4.16252	.067	-22.6754	.4754
	3.00	-7.65000	4.16252	.358	-19.2254	3.9254
1.00	4.00	.25000	4.16252	1.000	-11.3254	11.8254
	5.00	1.30000	4.16252	.998	-10.2754	12.8754
	1.00	11.10000	4.16252	.067	4754	22.6754
2 00	3.00	3.45000	4.16252	.921	-8.1254	15.0254
2.00	4.00	11.35000	4.16252	.057	2254	22.9254
	5.00	12.40000*	4.16252	.029	.8246	23.9754
	1.00	7.65000	4.16252	.358	-3.9254	19.2254
2.00	2.00	-3.45000	4.16252	.921	-15.0254	8.1254
3.00	4.00	7.90000	4.16252	.326	-3.6754	19.4754
	5.00	8.95000	4.16252	.208	-2.6254	20.5254
4.00	1.00	25000	4.16252	1.000	-11.8254	11.3254
4.00	2.00	-11.35000	4.16252	.057	-22.9254	.2254

	3.00	-7.90000	4.16252	.326	-19.4754	3.6754
	5.00	1.05000	4.16252	.999	-10.5254	12.6254
	1.00	-1.30000	4.16252	.998	-12.8754	10.2754
5.00	2.00	-12.40000*	4.16252	.029	-23.9754	8246
3.00	3.00	-8.95000	4.16252	.208	-20.5254	2.6254
	4.00	-1.05000	4.16252	.999	-12.6254	10.5254

^{*.} The mean difference is significant at the 0.05 level.

Successful	Service	Time	(t)	(min)	۱

(I) 1=First bank, 2=GT Bank, 3=Fidility, 4=Ecobank, 5= UBA	(J) 1=First bank, 2=GT Bank, 3=Fidility, 4=Ecobank, 5= UBA	N	Subset for alpha = 0.05	
			1	2
TukeyHSD ^a	5.00 4.00 1.00 3.00 2.00 Sig.	20 20 20 20 20 20	16.5500 17.6000 17.8500 25.5000	17.6000 17.8500 25.5000 28.9500 .057

Means for groups in homogeneous subsets are displayed.

Then, the Tukeycomparison tests show that GT bank is not significant at (5% or 10%) from others since it p-value is 0.208; while UBA bank is significant at 10% from others (p-value 0.057). Hence, the number of successful service time (min) are not the same for all the five banks (or the number of successful service time (min) are the same for other banks except UBA).

5.4 One-Way ANOVA Time to Failure (T) (Min) of the Five Banks

ANOVA

Time to Failure (t) (min)

the control of the co							
	Sum of Squares	df	Mean Square	F	Sig.		
Between Groups	757.700	4	189.425	1.828	.130		
Within Groups	9845.050	95	103.632				
Total	10602.750	99					

Time to Failure (t) (min)

Tukey HSD

VAR0001 0	N	Subset for alpha = 0.05	
5.00	20	8.3000	

a. Uses Harmonic Mean Sample Size = 20.000.

2.00	20	8.8000
4.00	20	8.9500
1.00	20	10.9500
3.00	20	15.7500
Sig.		.149

Means for groups in homogeneous subsets are displayed.

a. Uses Harmonic Mean Sample

Size = 20.000.

Since p value of the one-way ANOVA is 0.130 which is greater than the critical values of 0.05. We conclude that there is no significant difference among the five banks number of Time to Failure (t) (min). Tukey comparison tests confirmed no significant difference since the p-value of 0.149 is greater than 5%. Hence, time to failure rate are the same for all the five banks.

5.1 SUMMARY

This research was aimed at determining the time of failure rate and number of successful transaction in five banks using log-normal models. Transformation technique was applied to the log-normal model to obtain a quadratic equation (or polynomial regression) that helped to determine the parameters of the log-normal model. In addition, a one way ANOVA was used to test the equality of the mean (or average) time of failure rate and mean number of successful transaction of the five banks.

5.2 CONCLUSION

The research fitted a log-normal models to the five different randomly selected banks. GT-Bank model has the highest variation of 90.3% for number of successful service time (t), while Fidelity bank model has the highest variation of 56.6% for time of failure rate.

The one-way ANOVA result of the number of successful service time (t)showed a significant difference. The Tukey comparison tests showed that GT bank was not significant at (5% or 10%) from others while UBA bank was significant at 10% from others. Hence, the number of successful service time (min) were not the same for all the five banks (or the number of successful service time (min) were the same for other banks except UBA).

The one-way ANOVA result of the five banks of number of Time to Failure (t) (min) showed no significant difference among the banks. Tukey comparison tests confirm no significant difference. Hence, time to failure rate are the same for all the five banks.

5.3 RECOMMENDATIONS

This analysis should be carried out using other reliability measures.

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APPENDIX A

FIRST BANK SERVICE RECORD LOG-NORMAL MODEL Time to Failure (t) (min)

Model Summary

	mousi cumuary							
Model	R	R Square	Adjusted R Square	Std. Error of the Estimate				
1	.508ª	.258	.170	.69972				

a. Predictors: (Constant), LN(Xf)2, LN(Xf)

ANOVA^a

Ī	Model	Sum of Squares	df	Mean Square	F	Sig.
I	Regression	2.888	2	1.444	2.949	.080 ^b
ŀ	1 Residual	8.323	17	.490		
	Total	11.211	19			

a. Dependent Variable: LNY

b. Predictors: (Constant), LN(Xf)2, LN(Xf)

Coefficients^a

Model		Unstandardized Coefficients		Standardized Coefficients	t	Sig.
		В	Std. Error	Beta		
	(Constant)	1.246	.657		1.898	.075
1	LN(Xf)	.875	.791	1.175	1.106	.284
I	LN(Xf)2	130	.197	701	659	.519

a. Dependent Variable: LNY

LOG-NORMAL MODEL FOR Successful Service Time (t) (min)

Variables Entered/Removed^a

Model	Variables Entered	Variables Removed	Method
1	$LN(Xs)2, LN(Xs)^b$		Enter

a. Dependent Variable: LNY

b. All requested variables entered.

Model Summary

Model	l R R Squa		Adjusted R	Std. Error of	
			Square	the Estimate	
1	.822ª	.676	.638	.46230	

a. Predictors: (Constant), LN(Xs)2, LN(Xs)

ANOVA^a

M	odel	Sum of Squares	df	Mean Square	F	Sig.
	Regression	7.578	2	3.789	17.728	.000b
1	Residual	3.633	17	.214		
	Total	11.211	19			

a. Dependent Variable: LNY

b. Predictors: (Constant), LN(Xs)2, LN(Xs)

Coefficients^a

Model	Unstandardize	d Coefficients	Standardized Coefficients	t	Sig.	
	В	Std. Error	Beta			
(Constant)	906	1.245		727	.477	
1 LN(Xs)	1.791	1.003	1.870	1.785	.092	
LN(Xs)2	193	.189	-1.069	-1.021	.322	

a. Dependent Variable: LNY

GT BANK SERVICE RECORD

LOG-NORMAL MODEL Time to Failure (t) (min)

ANOVA^a

Mode	el	Sum of Squares	df	Mean Square	F	Sig.
	Regression	.657	2	.329	.944	.409b
1	Residual	5.922	17	.348		
	Total	6.579	19			

Coefficients^a

Model	Unstandardized Coefficients		Standardized Coefficients	t	Sig.
	В	Std. Error	Beta		
(Constant)	3.091	.346		8.927	.000
1 LN(Xf)	564	.422	999	-1.337	.199
LN(Xf)2	155	.113	-1.023	-1.369	.189

a. Dependent Variable: LNY

LOG-NORMAL MODEL FOR Successful Service Time (t) (min)

ANOVA^a

Мо	odel	Sum of Squares	df	Mean Square	F	Sig.
	Regression	5.939	2	2.969	78.775	.000b
1	Residual	.641	17	.038		
	Total	6.579	19			

a. Dependent Variable: LNY

Coefficients^a

_						
Model		Unstandardized Coefficients		Standardized Coefficients	t	Sig.
ı		В	Std. Error	Beta		
I	(Constant)	086	.657		131	.898
	1 LN(Xs)	.843	.479	.890	1.762	.096
	LN(Xs)2	010	.085	060	120	.906

a. Dependent Variable: LNY

FIDELITY BANK SERVICE RECORD

LOG-NORMAL MODEL Time to Failure (t) (min)

Model Summary

Model	R	R Square	Adjusted R Square	Std. Error of the Estimate
1	.752ª	.566	.515	.45129

a. Predictors: (Constant), LN(Xf)2, LN(Xf)

ANOVA^a

M	lodel	Sum of Squares	df	Mean Square	F	Sig.
	Regression	4.515	2	2.257	11.083	.001 ^b
1	Residual	3.462	17	.204		
	Total	7.977	19			

a. Dependent Variable: LNY

Coefficients^a

N	Model	Unstandardize	zed Coefficients Standardized Coefficients		t	Sig.
		В	Std. Error	Beta		
	(Constant)	1.515	.334		4.534	.000
1	LN(Xf)	.628	.372	1.100	1.687	.110
	LN(Xf)2	051	.091	364	558	.584

a. Dependent Variable: LNY

LOG-NORMAL MODEL FOR Successful Service Time (t) (min)

a. Dependent Variable: LNY b. Predictors: (Constant), LN(Xf)2, LN(Xf)

b. Predictors: (Constant), LN(Xs)2, LN(Xs)

b. Predictors: (Constant), LN(Xf)2, LN(Xf)

ANOVA^a

Ν	/lodel	Sum of Squares	df	Mean Square	F	Sig.
Г	Regression	1168.352	2	584.176	69.255	.000b
1	Residual	143.398	17	8.435		
	Total	1311.750	19			

a. Dependent Variable: LNY

Coefficients^a

ĺ	Model	Unstandardized Coefficients		Standardized Coefficients	t	Sig.
ı		В	Std. Error	Beta		
ľ	(Constant)	3.233	1.285		2.516	.022
ı	1 LN(Xs)	.551	.073	1.026	7.512	.000
ı	LN(Xs)2	066	.087	105	765	.455

a. Dependent Variable: LNY

ECOBANK SERVICE RECORD

LOG-NORMAL MODEL Time to Failure (t) (min)

Model Summary

Model	R	R Square	Adjusted R Square	Std. Error of the Estimate
1	.535ª	.287	.203	.64163

a. Predictors: (Constant), LN(Xf)2, LN(Xf)

$\textbf{ANOVA}^{\textbf{a}}$

Mod	el	Sum of Squares	df	Mean Square	F	Sig.
	Regression	2.814	2	1.407	3.417	.057b
1	Residual	6.999	17	.412		
	Total	9.812	19			

a. Dependent Variable: LNY

Coefficients

Model		Unstandardize	d Coefficients	Standardized Coefficients	t	Sig.
		В	Std. Error	Beta		
	(Constant)	2.511	.403		6.236	.000
	1 LN(Xf)	558	.549	794	-1.016	.324
	LN(Xf)2	258	.160	-1.259	-1.612	.125

a. Dependent Variable: LNY

LOG-NORMAL MODEL FOR Successful Service Time (t) (min)

Model Summary

Model	R	R Square	Adjusted R	Std. Error of the	
			Square	Estimate	
1	.691ª	.478	.416	.54898	

a. Predictors: (Constant), LN(Xs)2, LN(Xs)

ANOVA^a

Model	Sum of Squares	df	Mean Square	F	Sig.
Regression	4.689	2	2.345	7.780	.004 ^b
1 Residual Total	5.123 9.812	17	.301		

a. Dependent Variable: LNY

b. Predictors: (Constant), LN(Xs)2, LN(Xs)

b. Predictors: (Constant), LN(Xf)2, LN(Xf)

b. Predictors: (Constant), LN(Xs)2, LN(Xs)

Coefficients^a

ľ	Model	Unstandardize	d Coefficients	Standardized Coefficients	t	Sig.
L		В	Std. Error	Beta		
ľ	(Constant)	1.971	1.985		.993	.335
ľ	l LN(Xs)	383	1.483	325	258	.799
L	LN(Xs)2	217	.270	-1.012	803	.433

a. Dependent Variable: LNY

UBA BANK SERVICE RECORD

LOG-NORMAL MODEL Time to Failure (t) (min)

ANOVA^a

Mod	lel	Sum of Squares	df	Mean Square	F	Sig.
	Regression	1.575	2	.788	2.410	.120 ^b
1	Residual	5.556	17	.327		
	Total	7.131	19			

- a. Dependent Variable: LNY
- b. Predictors: (Constant), LN(Xf)2, LN(Xf)

Coefficients^a

Model		Unstandardize	d Coefficients	Standardized Coefficients	t	Sig.
L		В	Std. Error	Beta		
ſ	(Constant)	2.169	.342		6.341	.000
1	1 LN(Xf)	.054	.451	.090	.119	.907
L	LN(Xf)2	065	.128	383	508	.618

a. Dependent Variable: LNY

LOG-NORMAL MODEL FOR Successful Service Time (t) (min)

\textbf{ANOVA}^{a}

Mod	del	Sum of Squares	df	Mean Square	F	Sig.
	Regression	3.980	2	1.990	10.738	.001 ^b
1	Residual	3.151	17	.185		
	Total	7.131	19			

- a. Dependent Variable: LNY
- b. Predictors: (Constant), LN(Xs)2, LN(Xs)

Coefficients^a

Mo	odel	Unstandardize	ed Coefficients	Standardized Coefficients	t	Sig.
		В	Std. Error	Beta		
	(Constant)	.904	1.786		.506	.619
1	LN(Xs)	.517	1.372	.548	.377	.711
	LN(Xs)2	035	.252	200	137	.892

a. Dependent Variable: LNY

APPENDIX B

ANOVA

Successful Service Time (t) (min)

	Sum of Squares	df	Mean Square	F	Sig.
Between Groups	2486.340	4	621.585	3.587	.009
Within Groups	16460.250	95	173.266		
Total	18946.590	99			

Successful Service Time (t) (min)

(I) 1=First bank, 2=GT Bank, 3=Fidility, 4=Ecobank, 5= UBA	(J) 1=First bank, 2=GT Bank, 3=Fidility, 4=Ecobank, 5= UBA	N	Subset for a	lpha = 0.05
			1	2
	5.00	20	16.5500	
	4.00	20	17.6000	17.6000
Tukey HSD ^a	1.00	20	17.8500	17.8500
rancy riob	3.00	20	25.5000	25.5000
	2.00	20		28.9500
	Sig.		.208	.057

Means for groups in homogeneous subsets are displayed.

a. Uses Harmonic Mean Sample Size = 20.000.

Failure Time Rate ANOVA

ANOVA

Time to Failure (t) (min)

	Sum of Squares	df	Mean Square	F	Sig.
Between Groups	757.700	4	189.425	1.828	.130
Within Groups	9845.050	95	103.632		
Total	10602.750	99			

Time to Failure (t) (min)

Tukey HSD

VAR00010	N	Subset for alpha = 0.05
5.00 2.00 4.00 1.00 3.00 Sig	20 20 20 20 20	8.3000 8.8000 8.9500 10.9500 15.7500

Means for groups in homogeneous subsets are displayed.

a. Uses Harmonic Mean Sample Size = 20.000.