

DEVELOPMENT OF A SINGLE WHEEL TEST RIG FOR MEASURING MOTION RESISTANCE

ABSTRACT

Research on soil-wheel interaction is *sine qua non* in studies of motion resistance. This however requires test rig facility for controlled experiment. However, such facility is non-existent presently in Nigeria. A single wheel Test Rig facility was developed at FUTA. It consists of a soil bin, tool carriage, single wheel tester, trolley and drive system. The indoor soil bin facility was equipped with a soil bin which dimension was 9.76 m length x 1.98 m width x 0.92 m height. The wall of the soil bin was constructed with wood. The woods are clad with bin wall (angle iron) for better reinforcement, rigidity and effective behaviour of bin walls in service

A single-wheel tester facility was utilized to investigate the effect of tire inflation pressure and vertical load on motion resistance of wheel. Two narrow wheels of 90/10-10 in width, IRC MB90 tire was used as the tester wheel on clay soil and was installed on a carriage traversing the length of soil bin. Two inflation pressures of 274 kPa and 380 kPa and four levels of vertical load applied on wheel (i.e. 15, 20, 30, and 40 kg) was examined at two different soil conditions (8% and 10% moisture content). The soil leveling and compaction roller mounted on the carriage was used to achieve a certain soil compaction, before it is processed by the active body or performing various experiments with the tire test wheel. When the carriage is towed by the means of the cable, the wheel rotates due to the force on the cable. Towing cable is connected to the carriage by the means of a hitch hook, allowing the measurement of the towing force needed to displace the carriage. A control panel is used for the power supply of the two electric reducing motors. The data obtained will be analysed using graphical method and statistical inherent analysis to get the significant effect of the factors with the response using ANOVA using statistical package for social sciences (SPSS 16). Exponential regression was obtained for the two wheels to check for linearity at different moisture content, R^2 value for test wheel 1 with inflation pressure of 270 kPa at 8% moisture content was 0.9974 while that of inflation pressure of 380 kPa at 10% moisture content was 0.9952; also for test wheel two (2) R^2 value was 0.9977 and 0.9914 at moisture content of 8% and 10% respectively, this shows for test wheel 1 with inflation pressure of 270 kPa at 8% moisture content showed more motion resistance compared to motion resistance of test wheel 1 at inflation pressure of 380 kPa and 10% moisture content, while for test wheel 2 with inflation pressure of 270 kPa showed low motion resistance at 8% motion content. In general, at constant level of soil compaction, the MR was found to increase within the increase in vertical load, and in all inflation pressures, the effect of vertical load seems to be similar. Figure 5 – Figure 6 showed the comparism between Motion resistance (MR) for the two test wheel as the vertical load and inflation pressure increases. Design Expert software was used to establish and validate a model based on how the experiment was designed, the model established shows the coefficient determination (R^2) of 0.9822 and the validation shows R^2 value of 0.9727. The contact area for all tests was in the range of 309-330 cm², average contact pressure increased nearly linearly with increase in vertical load and increase in

44 inflation pressure. A single wheel test rig has been developed to study motion resistance of
45 narrow wheels. The effect of different inflation pressures and vertical loads on the motion
46 resistance of the narrow wheels has been investigated under different moisture content (8% and
47 10%). Data to assist in the development of simple, low cost and easy to maintain agricultural
48 machines with narrow pneumatic wheel as traction members have been provided in terms of
49 motion resistance and motion resistance ratios.

50 **Keywords:** Single wheel, test rig, Soil bin, motion resistance, vertical load, inflation pressure
51 and moisture content.

52 1. INTRODUCTION

53 Field machines contribute a major portion of the total cost of crop production. The proper
54 operation is essential for any system to be reasonably profitable. The machines and equipment
55 used for operations make use of wheels and they are used on our farms. They make impact on
56 the soil; then there is the need to measure motion resistance and its effect on soil is essential.

57 Zoz and Grisso (2003) reported that tractive ability of tractor is normally affected by soil
58 reactions against the front and rear wheels. In the tractive performance of off- road vehicles,
59 rolling resistance is a major factor in the determination of the drawbar pull of agricultural
60 vehicles. Motion resistance is defined as the force opposing the motion of a free rolling wheel in
61 contact with a surface. Motion resistance also refers to the resistance to motion of a wheel
62 caused by the absorption of energy in the contacting surfaces of the wheel and the soil upon
63 which the wheel rolls (Plackett, 1985; Macmillan, 2002). Therefore, simple and low-cost
64 appropriate machines will help to increase the agricultural productivity of the agricultural
65 mechanisation development in developing countries is a key solution to increased agricultural
66 productivity and economic survival (Akande *et al.*, 2008). The specific objectives of these
67 research is to design and fabricate a single wheel test rig to measure motion resistance of towed
68 wheels in an indoor soil bin; evaluate the performance of the test rig under different soil
69 moisture content; and establish and validate models to predict motion resistance for single towed
70 wheels. The soil bin designed by Siemens and Weber (1964), Stafford (1979), Durant *et al.*
71 (1980), Godwin *et al.* (1980), and Onwualu and Watts (1989) are some examples of small-scale
72 soil bin. Researchers have been using soil bins to investigate the phenomena of soil-traction and
73 soil compaction. Raheman and Singh (2002) studied the effect of steering forces on a driven
74 tractor wheel in a soil bin. Canillas and Salokhe (2002) developed a decision support system to
75 predict soil compaction based on a soil bin research. Carmen (2002) evaluated the degree of
76 compaction caused by a towed wheel in a soil bin. Others (Watyotha *et al.*, 2001; Hendriadi and
77 Salokhe, 2002) utilized a soil bin to gain a better understanding in Cage wheel design to
78 improve the traction of the cage wheel.

79 2. Test Rig Facility

80 The study is located in the soil Dynamics laboratory of the Department of Agricultural
81 and Environmental Engineering, Federal University of Technology, Akure. A soil bin is
82 required for this study, an existing soil bin was extended from its initial dimensions of 5.49 m
83 length x 1.98 m width x 0.92 m height; and after extension it was 9.76 m length x 1.98 m width
84 x 0.92 m Other features of the equipment are: an electric drive system, trolley, carriage which
85 houses the test rig, a selected soil type and narrow wheels of different sizes and torque meters

86 for the measurement of drought force and torques. The load shall be measure using weighing
87 balance to get the vertical loading on the wheel. Preparation of soil was done by soil processing
88 roller guided by the use of recording soil penetrometer to get the soil condition (moisture
89 content and bulk density).

90 **2.7 Design Considerations**

91 Design considerations for the single wheel test rig include;

- 92 i. Power requirement: Two electric motors will be used for the test rig; one to move the
93 carriage and the other to rotate the wheel.
- 94 ii. Sizes of wheels to be tested: tyre sizes ranges from 5.0 x 12 and 5.5 x 13 of rim sizes
95 which are used for the calculation of the minimum and maximum width of the wheel.
- 96 iii. Location of the test rig facility: the test rig facility will be located in the Soil Tillage
97 dynamics Research Laboratory of the Department of Agricultural Engineering of the
98 Federal University of Technology, Akure.
- 99 iv. Type of soil: the soil was gotten from Federal university of Technology, Akure, STEP-B
100 site and analyzed to get the class of soil; the soil was clay soil.
- 101 v. Soil processing device: Soil Processing device include frame and weigh pan.
- 102 vi. Control measurement
- 103 vii. Safety: The machine was design to be safe to man and its environment by avoiding sharp
104 edges.

105 **2.2 Test rig development**

106 The test rig consists of a rigid frame, the soil bin, the carriage, on which the active part for
107 soil working is mounted, the wheel with tire; at the end of laboratory test rig a winch is fixed,
108 which is for trolley carriage with the cable. An electric motor, pulley, shaft, bearing and belt are
109 used for transmission of motion to drive the trolley; the trolley was driven by the cable, thus
110 towing the cart. The ends of the drive are attached to the carriage by the means of the hitches.
111 The carriage is also fitted with an electric motor and a gear transmission in order to drive the tire
112 wheel. The working depth of the wheel can be adjusted by the means of the hydraulic fork,
113 dependent on the vertical load and it is used to adjust the vertical position of the tire wheel.

114 **Characteristics of the Soil to be studied**

115 **Sample Location**

116 The sample of soil used in the indoor soil bin facility for testing was taken at the
117 Teaching and Research Farm of the Agricultural and Environmental Engineering (AGE),
118 Federal University of Technology, Akure (FUTA) for soil-analyses. The area has a general
119 elevation of between 300 and 700 metres above the mean sea level and means annual rainfall
120 between 1300 mm to 1500 mm.

121 **Sampling Method**

122 The sampling method used in collecting the sample is the pit sampling. It is done by
123 using farm tools (which include: digger, spade, cutlass and hand trowel) to collect the soil
124 sample through the soil profile.

125 During the collection of this sample, the outermost layer of the soil (about depth of 5cm)
126 was removed. Then, the soil is dug in profiles such that five profiles of soil were collected. The
127 depth of each profile is 10cm as shown in table 1 below.

128 **Characteristics of the wheels to be studied**

129 Brand - IRC (INOUE RUBBER COMPANY); Front/Rear - Front, rear
130 Tire size - 90/90-10; Bias/Radial - Bias Ply; Rim size - 10
131 Tube/Tubeless - Tubeless

132 **Experimental setup**

133 The soil leveling and compaction roller mounted on the carriage was used to achieve a
134 certain soil compaction, before it is processed by the active body or performing various
135 experiments with the tire test wheel. When the carriage is towed by the means of the cable, the
136 wheel rotates due to the force on the cable. Towing cable is connected to the carriage by the
137 means of a hitch hook, allowing the measurement of the towing force needed to displace the
138 carriage. A control panel is used for the power supply of the two electric reducing motors. The
139 dynamic braking principle is used in order to stop the carriage at the end of travel with the use of
140 a forward contactor. Switches on the control panel allow the selection of the electric motor (the
141 carriage towing motor or the tire wheel driving motor), as well as its forward or reverse motion.
142 The soil moisture content was obtained experimentally, the inflation pressure was achieved
143 using pressure gauge, vertical loading with the weighing scale, the rolling resistance (towing
144 force) and torque were calculated.

145 **Test variables**

146 For this study on the motion resistance (towing force) of pneumatic wheels; two wheels were
147 used of the same overall wheel diameter 510 mm but different design at four levels of added
148 loads, two levels of tyre inflation pressures at 274 kPa (40 psi) and 380 kPa (55 psi) and at two
149 different soil conditions (8% and 10% moisture content).

150 **Dynamic loads**

151 The dynamic loads which is synonymous to the axle or vertical loads are first measured in the
152 laboratory comprise the weight of the test rig and the test wheel. Four levels of added dynamic
153 loads (dead weights) of 98.1 N (10 kg), 147.15 N (16 kg), 196.2 N (20 kg), 294.3 N (30 kg) and 392.4 N
154 (40 kg).

155 **Effect of Vertical Load and Inflation Pressure on Motion Resistance of the Wheels**

156 The vertical loading and wheel inflation pressure was varied to evaluate its effect on the
157 motion resistance of the wheel.

158 **Effect of Vertical Load and Inflation Pressure on Contact Area**

159 The vertical loading of 150 N, 200N, 300 N, 400 N and wheel inflation pressure of 274
160 kPa and 380 kPa was varied for every experiment to evaluate its effect on the contact area. The

161 contact area was measure by the use of A4 paper placed on the path of the wheel to calculate the
 162 contact area of the wheel with the soil.

163 **Data Analysis**

164 The data obtained will be analysed using graphical method and statistical inherent
 165 analysis to get the significant effect of the factors with the response using ANOVA using
 166 statistical package for social sciences (SPSS 16) to test whether there is significant difference
 167 between the means of the measured motion resistance on the test surfaces and the two pneumatic
 168 wheels of the same sizes. Design expert 9 would be used to establish a two level factorial model
 169 and validated using the Excel 10.

170 **3. Results and Discussion**

171 **Component Design and Features of the Single Wheel Test Rig**

172 The soil bin facility consists of (i) The bin (ii) tool carriage (iii) Single wheel tester (iv)
 173 Trolley (v) drive. The bin is a soil box with rails on the top on which the carriage rides. The
 174 indoor soil bin facility was equipped with a soil bin which dimension was 9.76 m length x 1.98
 175 m width x 0.92 m height, respectively. The walls of the soil bin were constructed with wood.
 176 The woods are clad with bin wall (angle iron) for better reinforcement, rigidity and effective
 177 behavior of bin walls in service. Soil fitting refers to the process used to prepare the bin soils to
 178 provide desired soil conditions. The soil fitting sequence usually begins with the leveling of the
 179 soil surface to refill irregularities, pits and furrows and to make sure there is an even distribution
 180 of soil side to side and end to end of the bin, also the roller for compacting the soil to have
 181 different bulk density.

182 **Table 1. Towing force acting on the Test Wheel 1(soil condition: moisture content: 8%,**
 183 **inflation pressure: 274 kPa)**

Actual Velocity Va (m/s)	Theoretical velocity Vt (m/s)	Wheel Radius r (m)	Weight (kg)	Torque T(N)	Draw bar pull P(N)	Wheel slip (S)	Motion Resistanc e(MR)(N)	Contact Area(cm ²)	Motion Resistance ratio(MRR)
0.31	0.47	0.4	15	5060	7150	0.34	8.48	312	0.57
0.27	0.42	0.4	20	4598	8250	0.36	14.35	321	0.72
0.25	0.4	0.4	30	4378	8800	0.37	23.79	324	0.79
0.22	0.4	0.4	40	4378	9900	0.45	36.18	336	0.90

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185 **Table 2. Towing force acting on the Test Wheel 1 (soil condition: moisture content: 10%,**
 186 **inflation pressure: 380 kPa)**

Actual Velocity Va (m/s)	Theoretical velocity Vt (m/s)	Wheel Radius r (m)	Weight (kg)	Torque T(N)	Draw bar pull P(N)	Wheel slip (S)	Motion Resistance(MR)(N)	Contact Area(cm ²)	Motion Resistance ratio(MRR)
0.34	0.46	0.4	15	5073	7176	0.35	8.48	312	0.64
0.28	0.43	0.4	20	4612	8351	0.36	13.25	315	0.82
0.25	0.4	0.4	30	4423	8785	0.38	24.69	321	0.69
0.23	0.38	0.4	40	4388	9971	0.44	38.38	330	0.86

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188 **Table 3. Towing force acting on the Test Wheel 2(soil condition: moisture content: 8%,**
 189 **inflation pressure: 274 kPa)**

Actual Velocity Va (m/s)	Theoretical velocity Vt (m/s)	Wheel Radius r (m)	Weight (kg)	Torque T(N)	Draw bar pull P(N)	Wheel slip (S)	Motion Resistance(MR)(N)	Contact Area(cm ²)	Motion Resistance ratio(MRR)
0.34	0.47	0.4	15	5074	7177	0.33	8.49	309	0.67
0.29	0.46	0.4	20	4622	8352	0.36	14.45	315	0.84
0.24	0.43	0.4	30	4424	8786	0.38	22.79	321	0.87
0.23	0.38	0.4	40	4398	9973	0.46	35.19	324	0.98

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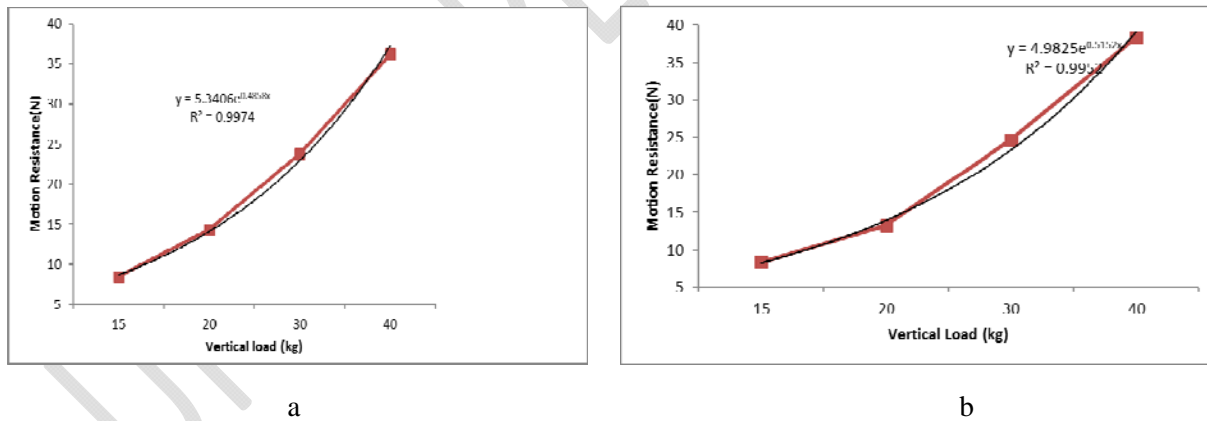
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192 **Table 4. Towing force acting on the Test Wheel 2(soil condition: moisture content: 10%,**
193 **inflation pressure: 380 kPa)**

Actual Velocity Va (m/s)	Theoretical velocity Vt (m/s)	Wheel Radius r (m)	Weight (kg)	Torque T(N)	Draw bar pull P(N)	Wheel slip (S)	Motion Resistance(MR)(N)	Contact Area(cm ²)	Motion Resistance ratio(MRR)
0.34	0.46	0.4	15	5074	7176	0.35	9.89	312	0.79
0.27	0.42	0.4	20	4632	8351	0.37	17.05	318	0.82
0.25	0.41	0.4	30	4422	8795	0.38	23.89	321	0.89
0.22	0.38	0.4	40	4398	9976	0.45	36.58	327	0.99

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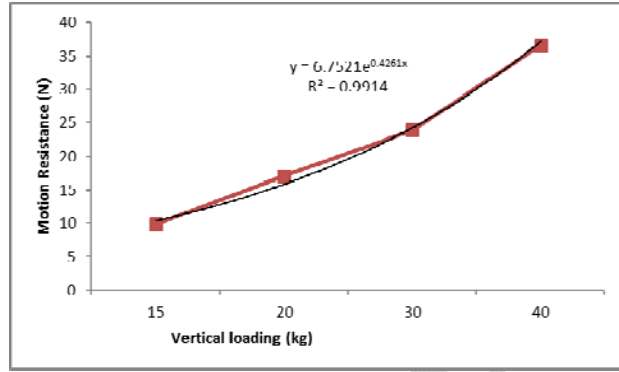
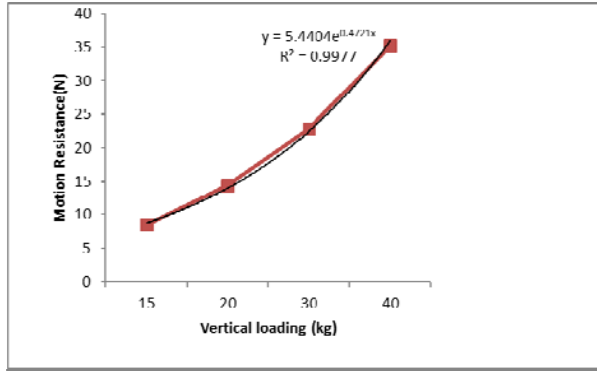


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198 Figure 1: (a)Effect of Vertical Load and Inflation Pressure (274 kPa) on Motion Resistance Test Wheel 1
199 8% moisture content; (b) Effect of Vertical Load and Inflation Pressure (380 kPa) on Motion Resistance
200 for Test Wheel 1 at 10% moisture content

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204 Figure 2: (a) Effect of Vertical Load and Inflation Pressure (274 kPa) on Motion Resistance Test Wheel 2
 205 at 8% moisture content; (b) Effect of Vertical Load and Inflation Pressure (380 kPa) on Motion Resistance
 206 Test Wheel 2 at 10% moisture content

207 Table 5. Analysis of variance (ANOVA), for the effect of tire inflation pressure (P) and vertical
 208 load (W) on wheel Motion Resistance (MR).

ANOVA

Motion resistance on Test wheel 1					
	Sum of Squares	Df	Mean Square	F	Sig.
Between Groups	.500	1	.500	.003	.017
Within Groups	971.163	6	161.860		
Total	971.663	7			

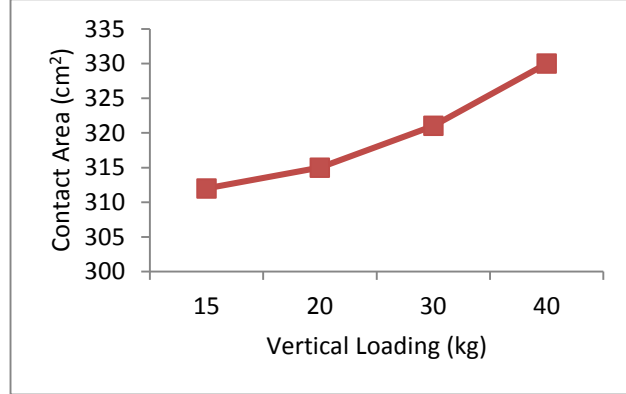
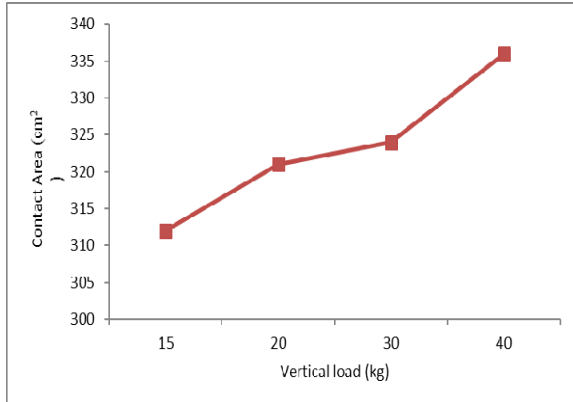
Motion resistance on Test wheel 2					
	Sum of Squares	Df	Mean Square	F	Sig.
Between Groups	5.265	1	5.265	.040	.048
Within Groups	788.807	6	131.468		
Total	794.072	7			

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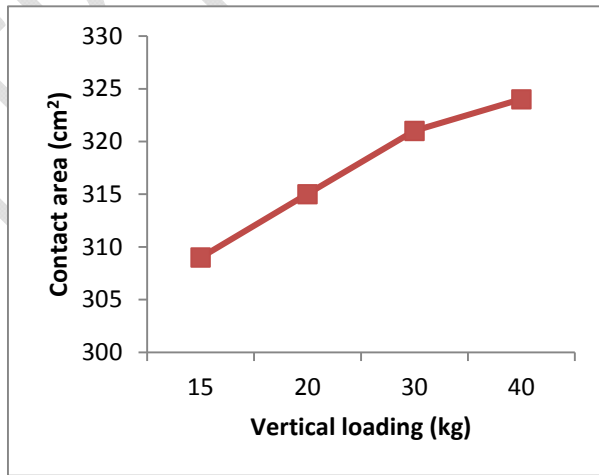
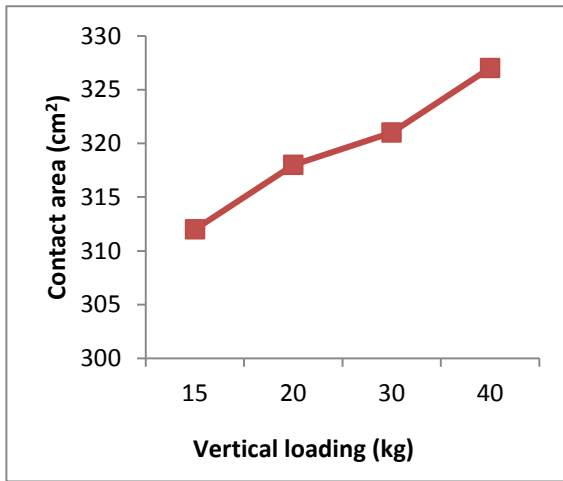
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215 Figure 3: (a) Effect of Vertical Load and Inflation Pressure (270 kPa) on Contact Area, Test
216 Wheel 1; (b) Effect of Vertical Load and Inflation Pressure (380 kPa) on Contact Area, Test
217 Wheel 1

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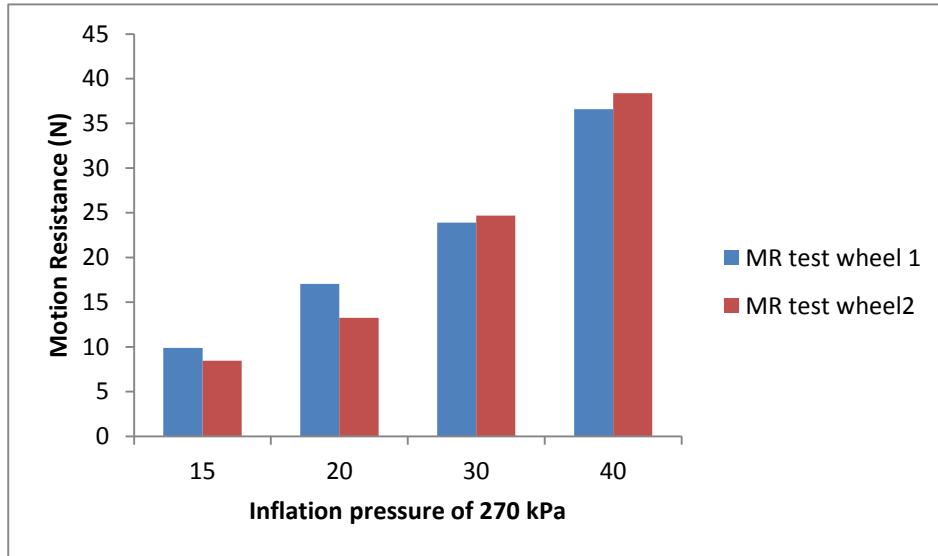
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221 Figure 4: Effect of Vertical Load and Inflation Pressure (270 kPa) on Contact Area, Test Wheel 2; (b)
222 Effect of Vertical Load and Inflation Pressure (380 kPa) on Contact Area, Test Wheel 2

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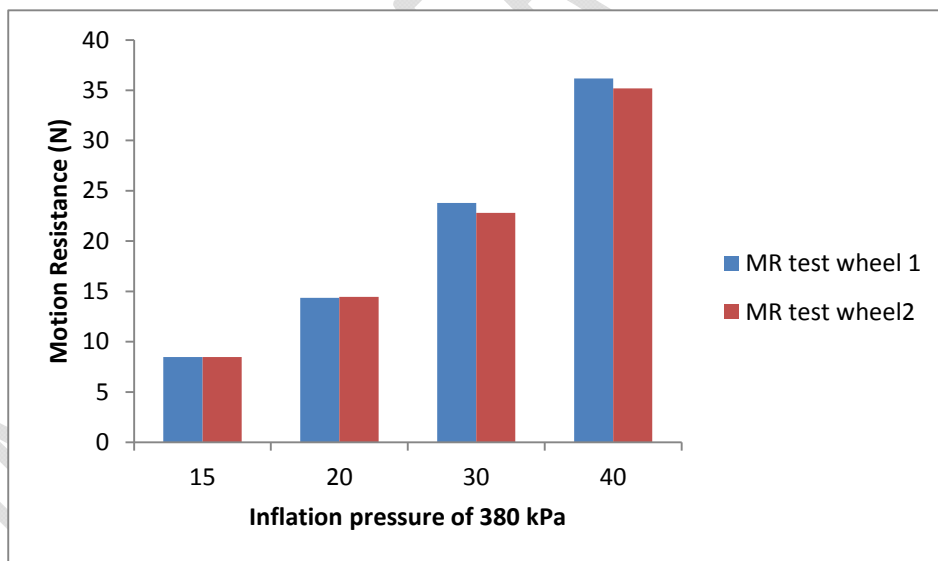


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228 Figure 5. Motion resistance of pneumatic wheels at 270 kPa pressure and 4 added loads on clay soil
 229 surface at 8% moisture content

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233 Figure 6. Motion resistance of pneumatic wheels at 380 kPa pressure and 4 added loads on clay soil
 234 surface at 10% moisture content.

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237 **Development of a Model for measuring Motion Resistance at 8% Moisture Content**

238 The data gotten from the experiment carried where separated into two; and this was done
239 in the ratio of 80% of the data to establish the model while 20% to validate the model. In this
240 study, BBD was used for response surface optimization with three process variables (inflation
241 pressure, vertical load, and wheel speed) at three levels. The design points fall within a safe
242 operating limit, within the nominal high and low levels, as BBD does not contain any points at
243 the vertices of the cubic region. Two different tests, namely, sequential model sum of squares
244 and model summary statistic were performed to check the adequacy of the models generated
245 from the obtained data.

246 Predictive model for motion resistance:

$$247 \quad MR = -0.011302 - 0.082711IP - 0.10229VL + 93.45734WS \quad R^2=0.9822 \quad (1)$$

248 Where *IP* is inflation pressure

249 *VL* is vertical load

250 *WS* is wheel speed

251 *MR* is motion resistance

252 **Validation of model**

$$253 \quad MR = +22.51389 - 0.086379IP - 0.023379VL + 5.44293WS \quad R^2=0.97274 \quad (2)$$

254 Where *IP* is inflation pressure

255 *VL* is vertical load

256 *WS* is wheel speed

257 *MR* is motion resistance

258 **4. Discussion**

259 Table 1-4 contain the actual velocity of the carriage, theoretical velocity, wheel radius,
260 load (weight), torque, drawbar wheel slip motion resistance, contact area and motion resistance
261 ratio (8% and 10%) and inflation pressure of 274 kPa and 380 kPa respectively. Figure 5 and
262 Figure 6 showed the relation of tire contact area pressure with vertical load and tire inflation

263 pressure. The tire contact pressure has a direct relation with vertical load and inflation pressure
264 of the wheels. The contact area for all tests was in the range of 309-330 cm² as shown in Figure 3
265 - Figure 4. Average contact pressure increased nearly linearly with increase in vertical load and
266 increase in inflation pressure. Comparing the results of contact area of tire-land with the results
267 of Cesbron *et al.* (2008) whose research about tire contact area showed that there is not much
268 different between tire contact areas in static and dynamic conditions (about 20%). Table 5 shows
269 the analysis of variance (ANOVA), for the effect of tire inflation pressure (P) and vertical load
270 (W) and the interaction of them on wheel Motion Resistance (MR). This table shows that both of
271 these two parameters have significant effect on MR changes. More ever the interaction of
272 independent variables (P, W) on dependent variable (MR) was significant with the probability
273 rate of 95%. A typical plot of vertical load versus MR as shown in Figure 1- Figure 2. The R^2
274 value shows exponential fits that best describe the relationship between tire inflation pressure
275 (P), vertical load (W) and the interaction of them on wheel Motion Resistance. Exponential
276 regression were obtained for the two wheels to check for linearity at different moisture content,
277 R^2 value for test wheel 1 with inflation pressure of 270 kPa at 8% moisture content was 0.9974
278 while that of inflation pressure of 380 kPa at 10% moisture content was 0.9952; also for test
279 wheel two (2) R^2 value was 0.9977 and 0.9914 at moisture content of 8% and 10% respectively,
280 this shows for test wheel 1 with inflation pressure of 270 kPa at 8% moisture content showed
281 more motion resistance compared to motion resistance of test wheel 1 at inflation pressure of 380
282 kPa and 10% moisture content, while for test wheel 2 with inflation pressure of 270 kPa showed
283 low motion resistance at 8% motion content. In general, at constant level of soil compaction, the
284 MR was found to increase within the increase in vertical load, and in all inflation pressures, the
285 effect of vertical load seems to be similar. Figure 6 showed the comparism between Motion
286 resistance (MR) for the two test wheel as the vertical load and inflation pressure increases. The
287 increase in inflation pressure caused MR to decrease at some point, but this effect was not
288 significant at low levels of vertical load. Kurjenluomar *et al.* (2009) reported “reduction of tire
289 inflation pressure reduced MR and rut depth only on soft soil, when the soil strength was low,
290 and in hard soil conditions the effect was opposite on MR” and this experiments were conducted
291 in clay, the results conforms the result of their research, and shows that reduction in inflation
292 pressure increases the MR of tire. Also Elwaleed *et al.* (2006) reported that reduction in tire
293 inflation pressure by 171.8 kPa from the recommended value resulted in decrease of tire motion

294 resistance ratio by 5.01%. However, further reduction by 380 kPa resulted in an increase in tire
295 motion resistance ratio by 9.96%, but their experiments were conducted on loosened soil
296 condition which was different from this test condition. The model established shows the
297 coefficient determination (R^2) of 0.9822 and the validation shows R^2 value of 0.9727

298 **Predictive models (exponential fit)**

299 $y = 5.3406e^{0.4858x}$ $R^2 = 0.9974$ Wheel 1, inflation pressure (274 kPa) (4.8)

300
301 $y = 4.9825e^{0.5152x}$ $R^2 = 0.9952$ Wheel 1, inflation pressure (380 kPa) (4.9)

302
303 $y = 5.4404e^{0.4721x}$ $R^2 = 0.9977$ Wheel 2, inflation pressure (274 kPa) (5.0)

304 $y = 6.7521e^{0.4261x}$ $R^2=0.9914$ Wheel 2, inflation pressure (380 kPa) (5.1)

305 **Other fits tested** :Linear fits ; $R^2=0.9757$, Logarithm fit; $R^2=0.8792$, Power fit; $R^2=0.9761$

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Plate 1. Test Rig facility

309 **5. Conclusion**

- 310 1. A single wheel test rig has been developed to study motion resistance of narrow wheels.
311 2. The effect of different inflation pressures and vertical loads on the motion resistance of
312 the narrow wheels have been investigated under different moisture content (8% and 10%)
313 3. Data to assist in the development of simple, low cost and easy to maintain agricultural
314 machines with narrow pneumatic wheel as traction members have been provided in terms of
315 motion resistance and motion resistance ratios.
316 4. The motion resistance ratio increases with increase in vertical load.
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318 **References**

- 319 Akande, F. B, Ahmad, D., Hadi, S., Shamsuddin, S. and Fashina A. B., (2008). "Status of
320 research on Narrow wheels," presented at Malaysian Scientist and Technologist
321 Conference (MSTC,2008), KLCC, Malaysia.examples. In *A textbook for Students and*
322 *Engineers*.
- 323 Cannilas, E. C and Salokhe V. M., (2002). A decision support system for compaction assessment
324 in agricultural soil. *Soil and Tillage Research* 65 (2):221-230.
- 325 Durant, D. M., Perumpral, J. V. and Desai C. S., (1980). Soil bin test facility for soil tillage Tool
326 interaction studies. *Soil and Tillage Research* 1:289-298.
- 327 Godwin, R. J., Spoor, G., Kilgour, J., (1980). The Design and Operation of a Simple Low Cost
328 Soil Bin. *Journal of Agricultural Engineering Research*, 25:99-104.
- 329 Hendriadi, M and Solakhe, V. M., (2002). Improvement of a power tiller cage wheel for use in
330 swampy peat soil. *Journal of Terramechanics*, 39(2): 55-70.
- 331 Macmillan, R. H., (2002). Mechanics of tractor-implement performance; Theory and
332 Worked.No. 89-1106, ASAE, St. Joseph: Michigan.
- 333 Onwualu, A. P. and Watts, K. C., (1989). Development of a soil bin test facility. ASAE Paper
- 334 Plackett, C. W., (1985). A review of force prediction methods for off-road wheels. *Journal of*
335 *Terramechanics*. (soils.usda.gov/technical/handbook)
- 336 Rahemen, H. and Singh, R., (2004). Steering forces on un-driven tractor wheel. *Journal of*
- 337 Stafford J. V. A., (1979). Versatile high-speed soil tank for studying soil and implement
338 interaction. *Agricultural Engineering Resources*. 24: 57-66.
- 339 *Terramechanics* ,40(3):161-178
- 340 Watyotha, C., Gee-Clough, D. and Salokhe, V. M., (2001). Effects of circumferential angle, lug
341 spacing and slip-on lug wheel forces. *Journal of Terramechanics* 38: 1-14.
- 342 Zoz, F. and Grisso, R.D., (2003). Traction and Tractor Performance. Agricultural Equipment
343 Technology Conference. ASAE Publication Number 913C0403. Louisville, KY.
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