

1 **Experimental design for optimization of β -Xylosidase production by *A. fumigatus* isolated from the Atlantic**
2 **Forest (Brazil).**

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5 **Abstract**

6 The production of β -Xylosidase by a new strain of *Aspergillus fumigatus* (PC-7S-2 M), isolated from the Brazilian
7 Atlantic Forest, was analyzed at 28° C using modified Czapeck media supplemented with different agroindustrial
8 residues at 1% (w/v). Conidia were inoculated for 7 days, and the best activity for β - Xylosidase was obtained in the
9 presence of barley brewing residue after 4 days (15 U mL⁻¹). To optimize the production of β -Xylosidase, this carbon
10 source was used for a central composite rotational design (CCRD) to obtain a significance level of $p < 0.10$, which
11 predicted an enzyme activity of 245.04 U mL⁻¹. The model validation revealed β -Xylosidase activity was optimized at
12 229.06 U mL⁻¹. Furthermore, the production of intracellular *A. fumigatus* β -Xylosidase increased by 1,500% (15 times)
13 over that initially obtained, achieving 93.47% of the predicted model. This finding emphasizes the availability of *A.*
14 *fumigatus* β -Xylosidase production with possible applications in biotechnological processes.

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16 **Keywords:** barley brewing residue; experimental design; agroindustrial residue; hemicellulose; β -Xylosidase,
17 *Aspergillus fumigatus*.

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35 **Introduction**

36 The xylan molecule is one of the most important hemicellulose components in plant cell walls. It is present in
37 agricultural residues and is degraded by synergistic action of several enzymes, mainly by endo-Xylanases (EC 3.2.1.8)
38 and β -Xylosidases (EC 3.2.1.37) (Liu et al. 2008). The endo-Xylanases cleave the main chain of xylan and release
39 smaller sugars, such as xylobiose, which is degraded to xylose by β -Xylosidases (Teng et al. 2011). These enzymes are
40 well characterized by different biochemical and molecular approaches and can be used in industrial processes to degrade
41 the hemicellulose present in agricultural waste. Therefore, these enzymes have great applicability in different textiles,
42 food industries, such as juices and animal feed, and the production of cellulosic ethanol (Lasrado and Gudipati, 2013).

43 In view of the fact that the variability in the production of various enzyme systems fungi are usually capable of
44 degrading contaminants from soil and water at low concentrations; they are excellent degraders in the absence of
45 nutrients, such as in low nitrogen conditions found in polluted sites (Oliveira et al. 2011). Additionally, fungi are able to
46 extract energy from organic compounds and carbon found in wastewater and agro-industrial residues, such as corn
47 stover, rice husks, and coconut fiber residues from the brewing industry, which are generated in abundance in Brazil. The
48 global need to decrease agricultural waste contamination to the environment has stimulated investment in innovative
49 processes to obtain these enzymes from waste yeast in recent decades (Benassi et al. 2012).

50 *Aspergillus* species have been widely studied in response to its wide distribution in different regions on the
51 planet. The species of this genus are known to be great at degrading soil contaminants by producing higher levels of
52 secreted proteins. They present a viable maintenance cost and their genetic properties are better characterized than
53 several available mutant strains (Wongwisansri et al. 2013). *Aspergillus fumigatus* is specifically used in various
54 biotechnological processes, such as the production of antibiotics and enzymes, and the biodegradation of toxic
55 compounds, such as dyes from textile environments, thereby providing an alternative to the treatment of effluent while
56 producing fewer by-products (Jin et al. 2007). The microorganism presents asexual spores, is saprophyte and mesophilic
57 and is found in different environments, e.g., air, land and marine ecosystems. Furthermore, they can be cultured at
58 temperatures from 28 °C to 40 °C (Saqib et al. 2010).

59 The application of experimental design techniques is a very useful tool to optimize the process the production of
60 enzymes that are of biotechnological interest, while minimizing costs and maximizing yield, productivity and quality.

61 This statistical tool is known to determine and quantify the influence of variables on the desired responses (Sena et al.
62 2011).

63 In the present work, we analyzed and optimized the production of intracellular β -Xylosidase from a new strain
64 of *A. fumigatus* (PC-7S-2 M), isolated specifically from the Atlantic Forest of West Paraná State, Brazil, in an area under
65 environmental protection named Dog Head State Park, which presently features a great biodiversity of microorganisms
66 that have been little explored. The production of β -Xylosidase was analyzed using different agro-industrial residues as
67 carbon sources for growth of the fungus, and the best conditions for inducing enzyme activity were analyzed by applying
68 experimental design techniques and statistical approaches to maximize optimal production and induction of fungal β -
69 Xylosidase activity using different combinations of variables.

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Materials and Methods

Description of the collection site of the fungus

A. fumigatus (PC-7S-2 M) was isolated during collections in the Dog Head State Park, Paraná, Brazil. The park has a total area of 60.98 hectares and is located in the south central portion of the municipality of São Pedro do Iguaçu, under the coordinates 24 54 '47' latitude (south) and 53 54 '35' longitude (west). The unit of conservation receives this name because the area is shaped similar to a dog's head from aerial views of the area by camera and satellite. The park also has a subtropical climate with hot summers, infrequent frosts and concentrated rainfall trends in the summer months. The formation of the vegetation is semideciduous forest submontane, and its surroundings are predominantly composed of forest and agricultural areas, which are considered important remnants from the development for the entire western region of Paraná.

Identification and maintenance of the fungal species

A. fumigatus (PC-7S-2 M) was first identified by morphological taxonomists by the Federal University of Pernambuco, Brazil. However, identification of the isolate at genus and species levels was confirmed by nucleotide sequence analysis of the ITS region corresponding to the rRNA of the microorganism in the Laboratory of Molecular Biochemistry of UNIOESTE by extracting the total DNA from the fungus followed by DNA replication using an amplicon target for sequencing (HELIXXA-DNA Sequencing Service, Brazil). The obtained sequence was analyzed by the algorithm Blast-X from the National Center for Biotechnology Information (NCBI). The sequence was deposited in GenBank under accession number *KM 349230*.

A. fumigatus (PC-7S-2M) conidia were maintained in test tubes containing 5 mL of solid medium potato dextrose agar (PDA), composed of 1.5% (w/v) glucose, 2.0% (w/v) agar and 20% (v/v) potato juice. These samples were cultured and grown at 28 °C for 7 days, and after its growth, the microorganism was kept and stored at 4 °C for 30 days. The isolate was deposited in the fungal collection of the Laboratory of Biochemistry (UNIOESTE, Cascavel).

Preparation of by-products and residues from agriculture

120 The carbon sources tested in these trials for fungal growth and induction of enzyme activity were randomly
121 selected: barley brewing residue, wheat bran, passion fruit peel, pokan peel and ripe banana peel. The residues used in
122 the tests were prepared starting with oven drying at 70 °C for 24 hours followed by crushing using a mill (SL30 slicer -
123 SOLOLAB) and a sieve. The shredded waste was sieved using four screens ranging from 12 to 48 mesh and
124 subsequently stored in clear glasses at room temperature.

125 *Culture conditions of A. fumigatus*

126 Conidia of the fungus *A. fumigatus* (PC-7S-2M) were maintained on PDA medium at 4 °C and, after the fresh
127 state, were used for the preparation of 1 mL suspensions (1×10^5 conidia mL^{-1}) using sterile distilled water and were
128 inoculated in 25 mL of modified mineral Czapeck medium (0.3 g NaNO_3 , KH_2PO_4 0.1 g; $\text{MgSO}_4 \cdot 7\text{H}_2\text{O}$ 0.05 g, KCl 0.05
129 g, 0.001 g $\text{FeSO}_4 \cdot 7\text{H}_2\text{O}$; 0.1 mg casein at pH 6.0), separately supplemented with 1% (w/v) of the different agricultural
130 residues, such as passion fruit peel, pokan peel, barley brewing residue, soya flakes and ripe banana peel. The
131 cultivations were carried out in two ways: stationary liquid and agitated liquid, maintained at 28 °C for 10 days in
132 duplicates. After this period, cultures were vacuum filtered on sterile Whatman paper, and the frozen mycelium was
133 macerated using glass beads in 5 mL of distilled water and centrifuged at 4 °C 8,000 x g for 5 minutes. The supernatant
134 was used to determine the amount of β -Xylosidase and the optimum pH and temperature.

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136 *Activity assay for β -Xylosidase*

137 Fifty μL of the enzyme extract was added to 250 μL of the synthetic substrate *p*-nitrophenyl β -D-xylopyranoside
138 (pNPX) (Sigma-Aldrich) and incubated in a water bath at 50 °C for 10 minutes. The reaction was stopped by adding 1
139 mL of saturated solution of sodium tetraborate, and the product of the reaction was read by a spectrophotometer at 410
140 nm. Enzyme activity values were calculated using the formula obtained from the standard calibration curve using *p*-
141 nitrophenol, 1 mg mL^{-1} , and the results were expressed in mmol mL^{-1} . One unit of enzyme activity was defined as being
142 able to release 1 micromole of *p*-nitrophenol per milliliter of reaction (Simão et al. 1997).

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144 *Influence of time on A. fumigatus β -Xylosidase production*

145 *A. fumigatus* (PC-7S-2 M) was grown in culture medium containing modified Czapeck medium with the
146 different tested residues. We selected the best carbon source for the production of β -Xylosidase. Furthermore,
147 standardized stationary liquid culture was the most efficient for production of the enzyme. Therefore, the fungus was
148 inoculated in liquid phase in the presence of the agroindustrial residue that operated as the best inducer of β -Xylosidase
149 activity for a period of 7 days, and every day, two vials were withdrawn. The samples were taken, filtered and submitted

150 to enzymatic assays. We measured the intracellular β -Xylosidase and determined the best day of production of the
151 protein. All assays were conducted in duplicate, and measurements were performed in triplicate.

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155 *Influence of pH and temperature on the activity of A. fumigatus β -Xylosidase.*

156 β -Xylosidase was also measured under different values of pH (5 to 7.5) using McIlvaine solution buffer
157 (McIlvaine, 1921). To analyze the effect of temperature on the enzymes activity in crude extracts, samples were
158 incubated at temperatures from 35 °C to 60 °C, with 5 degree increments. The enzymatic reaction was performed
159 according to the optimal assay conditions. The experiments were performed in duplicate and measurements in triplicate.

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161 *Experimental design*

162 From the experiments highlighted above, it was possible to obtain the optimal conditions for the production of
163 *A. fumigatus* intracellular β -Xylosidase (PC-7S-2 M). Therefore, we determined the variables that had the greatest
164 influence on the performance of the fungus to produce β -Xylosidase, enabling a reduction in process variation and
165 obtaining better agreement between the nominal values and the desired values, which reduces the process time, reduces
166 operating costs, improves process yield and utilizes industrial waste, which is widely produced in large quantities in
167 Brazil by the brewing industry.

168 The factorial experimental design CCRD was conducted to determine the optimal conditions for β -Xylosidase
169 production from the fungal isolated from the selected residue, barley brewing residue (Saini et al. 2013). The
170 combination of the variables was determined using two levels, three factors, an additional six axial points and center
171 point repetition, totaling 17 samples. The main effects of variables on enzyme production, their interactions, and analysis
172 of variance (ANOVA) with a significance level of 10% were calculated. The CCRD experimental design and response
173 surface methodology were used for optimizing the conditions and providing a suitable mathematical model specifically
174 for the activity of β -Xylosidase in this process (Sukhbaatar et al. 2014), aiming to maximize the production of the
175 enzyme and progressively facilitate the selection of variables, such as temperature, days of incubation, agitation, and the
176 concentration of the residual, to increase the production of the desired enzyme.

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178 *The First Experimental design: Central Composite Design (CCD)*

179 The central composite design was characterized by an experiment with a central point and run in duplicates,
180 giving an estimate for the pure error, and two levels of axial points and factors that determined the quadratic terms
181 (Walia et al. 2013). This design was adjusted to the working conditions of the laboratory to obtain the main effects of the
182 studied factors. The levels used for each factor are presented in Table 1. The coded and actual values of the factors are
183 shown in Table 2, where testing was performed with 11 different combinations. The statistical analysis was performed to
184 obtain linear effects, and a model has been adjusted according to Eq. 1 below to describe the response surface.

$$186 \quad \hat{y} = b_0 + \sum_{i=1}^3 b_i X_i + \sum_{i,j=1}^3 b_{ij} X_i X_j \quad (\text{Eq. 1})$$

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188 Path of Maximum Slope

189 After obtaining the results from the first design, 8 combinations were employed to figure out the greatest points
190 for the factors using the barley brewing residue and nitrogen source yeast extract. Once a mesophilic microorganism was
191 isolated, the temperature of the experiment was set at 28 °C, as shown in Table 3, and the experimental approach was
192 determined based on which strategies would be improving the dependent variables and responses. The test showed that
193 the best response for the production of β -Xylosidase was selected as the central point of the second event, when the
194 CCRD was prepared. The tests with the combinations described were used for establishing the relationships between the
195 response variables and the independent variables because these were not known and needed to be determined to allow
196 analysis of the data if these are far from optimal points. Such tests were performed as punctual goals to enable the
197 alignment of points and finally to select the optimum point (Córdoba et al. 2012).

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199 *Second Experimental Design: CCRD*

200 The design was based on three factors: concentration of residue (barley brewing residue) as a carbon source;
201 temperature; and concentration of yeast extract (nitrogen source). The microorganisms were cultivated for 4 days at 28
202 °C in stationary liquid. The experimental matrix consisted of three central points and six axial points, and the two factors,
203 combined with three levels, totaled 17 trials. We selected the combination of 0.750 g of barley brewing residue with
204 0.097 g of yeast extract as a central point because the test showed the highest production of β -Xylosidase from the
205 combinations shown in Table 3. Table 4 shows factor levels of the second event. In Table 5, the coded values and the
206 actual values of the planning conducted with the three central points and six axial points are presented, totaling 17 tests.

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208 *Optimization Process*

209 Optimization is performed to identify the setting that best determines both sets of response variables (Córdoba et
210 al. 2012). The optimal setting corresponds to the setting that minimizes the multivariate quadratic loss function, i.e., the
211 optimal setting incurs the lowest overall loss of all related factors. Therefore, process validation was performed until the
212 preparation of six samples equaled the optimal conditions defined by the experimental designs carried out according to
213 Table 5.

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215 *Validation of the Model*

216 The statistical analysis was performed to determine which coefficients were significant and adjust a second
217 order model (Eq. 2) to correlate the variables with their responses ($p < 0.1$).

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$$\hat{y} = b_0 + \sum_{i=1}^3 b_i X_i + \sum_{i=1}^3 b_{ii} X_i^2 + \sum_{i,j=1}^3 b_{ij} X_i X_j \text{ (Eq. 2)}$$

219 The significance of the coefficients of the model was evaluated using "t", where b_0 , b_i , b_{ii} , b_{ij} are the regression
220 coefficients of the model, and X_i and X_j are the independent variables in the coded values test.

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243 **Results and Discussion**

244 The influence of different concentrations of waste and by-products in the agro-industry on the production of β -
245 Xylosidase by the isolated fungus *A. fumigatus* (PC-7S-2 M) was observed in Fig. 1a, which shows the results of
246 incubating for 10 days under constant agitation or in stationary liquid at 28 °C. The barley brewing residue was the most
247 efficient at producing β -Xylosidase under stirring conditions compared to the other carbon sources; the differences
248 between these residues were very constrained. However, the residue from the brewing industry was very efficient in
249 inducing improved production of β -Xylosidase between different carbon sources tested under the conditions of stationary
250 liquid culture, providing a maximum enzyme activity of 15.45 U mL⁻¹.

251 Michelin et al. (2012) conducted experiments on the induction of β -Xylosidase activity of the fungi *A.*
252 *ochraceus* and *A. terricola*, and enzymatic activity levels of 30 U mL⁻¹ and 56 U mL⁻¹, respectively, were obtained in the
253 presence of another agroresidue that is very abundant in North America: corn cob. Therefore, induction of the activity of
254 β -Xylosidase by lignocellulosic-rich waste material in species of the genus *Aspergillus* has been reported in the literature.
255 However, to our knowledge, this is the first time that barley brewing residue has been used for induction of intracellular
256 β -Xylosidase from a species of the genus *Aspergillus*.

257 The levels of β -Xylosidase produced by the fungus *A. fumigatus* (CP-2 M-7S) during incubation in the presence
258 of barley brewing residue 1% (w/v) at 28 °C in stationary liquid culture were more than 2.5 times higher (41.20 U mL⁻¹)
259 on the fourth day at a steady temperature of 28 °C, than that previously observed after 10 days in liquid culture, showing
260 a positive influence of lower incubation time on enzyme activity (Fig. 1b).

261 According to Benassi et al. (2012), incubation of *A. phoenics* with different wastes, such as corn flakes, cassava
262 flour and rye flake, resulted in β -Xylosidase production values of 0.36 U mL⁻¹, 0.66 U mL⁻¹ and 7.60 U mL⁻¹,
263 respectively. These values are below the values obtained by the non-optimized experiments that we present in Fig. 1a
264 and b in the present report. To our knowledge, this work is also the first to use statistical approaches to optimize the
265 production of β -Xylosidase by varying barley brewing residue conditions in a species of *Aspergillus*.

266 The effects of pH and temperature on enzymatic activity were also analyzed for intracellular β -Xylosidase using
267 the crude enzyme extract obtained after culturing for 4 days in stationary and liquid cultures in the presence of barley
268 brewing residue (1% w/v) at 28 °C. In these experiments, changes in enzyme activity with pH values were analyzed
269 using McIlvaine (1921) buffer in a pH range from 5 to 7.5, and the samples were incubated in a temperature range from
270 35 °C to 60 °C (5 degree intervals) with the synthetic substrate pNPX, as described in the Materials and Methods, to
271 analyze the effect of temperature on β -Xylosidase activity. Our data showed that after 4 days of cultivation under the
272 above conditions, β -Xylosidase and *A. fumigatus* showed optimal activity at pH 5.5 and 45 °C.

273 Omardien (2013) conducted experiments to analyze the activity of β -Xylosidase with *Aerobasidium pullulans*
274 (isolate 23B25) by testing several residues, such as wheat bran and wheat bran mixed with rye, and the enzyme activity
275 was 0.22 U mL⁻¹ after 5 days of growth for the mixture with rye bran, showing an optimum pH at 3 and an optimum
276 temperature range of 80 to 90 °C. However, comparing the data obtained in the present work with that carried out by
277 Omardien, we obtained higher production of β -Xylosidase (41.20 U mL⁻¹) using barley brewing residue in just 4 days
278 and an optimum pH and temperature of 5.5 and 45 °C, respectively (data not shown). Knob and Carmona (2009) studied
279 the induction of β -Xylosidase by the fungus *Penicillium sclerotiorum* cultured in medium supplemented with waste; after
280 five days of cultivation at 28 °C under agitation, enzyme production was 1.47 U mL⁻¹, 0.24 U mL⁻¹ and 0.05 U mL⁻¹, in
281 the presence of bran, oat bran and corn cobs, respectively, applying 0.01 citrus pectin as the carbon source. In these
282 assays, the optimal temperature for activity was 60 °C and the optimum pH equal to 2.5.

283 The coefficient of linear correlation is observed between -1 and +1 levels, allowing quantification and
284 determination of the direction of the relationship, whereas the extreme values -1 and +1 refer to perfect, negative and
285 positive linear correlations, respectively. Intermediate coefficient values indicate weak relationships, coefficient close to
286 the extreme values represents a strong relationship, and coefficient near or equal to zero indicates the absence of a linear
287 (Rodrigues and Iemma, 2014) correlation. Therefore, the best culture medium was investigated by means of DCC linear
288 effects. The temperature had a negative effect, indicating that increasing cultivation from temperatures of 28 °C (-1) to 42
289 °C (+1) reduced the production of β -Xylosidase by the fungus *A. fumigatus* by 28 U mL⁻¹ (Fig. 2). In contrast barley
290 brewing residue showed a positive effect of 21 U mL⁻¹ when larger quantities were added, changing from 0.125 g (-1) to
291 0.375 g (+1). There was an increase of 9.9 U mL⁻¹ in the production of β -Xylosidase when the concentration of yeast
292 extract was increased from 0.025 g (-1) to 0.080 g (+1). We observed that the addition of yeast extract influenced the
293 production of the enzyme, which is an important source of nitrogen and other nutrients added to the culture medium;
294 however, when yeast extract is added in large quantities, it is possible to statistically observe inhibition in the production

295 of β -Xylosidase. Therefore, it is necessary to establish optimal quantities for optimal enzyme levels when combined with
296 crushed barley.

297 Using yeast extract as a nitrogen source, Vaithanomsat and colleagues (Vaithanomsat et al. 2011) optimized the
298 fermentation conditions using *A. niger* for the production of β -glucosidase using the response surface methodology in
299 medium consisting of 0.275% (w/v) yeast extract, 1.125% (w/v) cellobiose and 2.6% (w/v) ammonium sulfate, with a pH
300 of 3, resulting in a specific activity of 8.99 U mg⁻¹.

301 In the present work, analysis of variables has produced a first order mathematical model, and the summary from
302 ANOVA for the enzymatic activity with significant terms at 10% probability ($p < 0.10$) is presented in Table 6. The
303 coefficient of determination (R²) is equal to 0.68, and the F test showed that the model is adequate at predicting the
304 results using a response surface. The model is presented in Eq. 3 and B represents barley brewing residue, T is
305 temperature and E is yeast extract:

$$307 \hat{\beta} = 17,96 + 10,53B - 13,87T + 4,95E \quad (\text{Eq. 3})$$

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309 The surfaces from the response model (Eq. 3), shown in Fig. 3, show the relationship between temperature,
310 yeast extract and barley brewing residue. It was observed that the lower the temperature used in combination with a
311 greater amount of crushed barley, the greater was the activity of β -Xylosidase from *A. fumigatus* (40 U mL⁻¹) (Fig. 3a).
312 However, when the two factors were provided at steady increases, activities above 40 U mL⁻¹ were observed for β -
313 Xylosidase (Fig. 3b).

314 From the standpoint of utilizing agro-industrial waste, which may be cumulative in nature, it is advantageous to
315 optimize a process in which a larger amount of residue and less yeast extract are used for the industrial process of
316 enzymatic synthesis because it is less costly and beneficial to the environment. Lastly, when comparing yeast extract
317 with temperature, gradually increasing the amount of yeast extract combined with a lower temperature, approximately 28
318 °C, led to larger quantities of β -Xylosidase 40 U mL⁻¹ (Fig. 3c).

319 The production of β -Xylosidase by *Colletotrichum graminicola* when in contact with wheat bran was 57.9 U mL⁻¹
320 when grown at 65 °C for 72 hours with an optimum pH of 5 (Zimbardi et al. 2013). Supplementing the medium with
321 1% peanut shell led to an increase in enzyme production, up to 79 U mL⁻¹. With the application of experimental design,
322 the fungus grown in medium containing the residue peanut hulls optimized production to 126 U mL⁻¹, whereas
323 temperature had no significant effect when compared with other independent variables, such as the concentration of the
324 residual, time for cultivation and initial moisture content.

325 Compared to classical studies (not CCRD) performed with xylan-degrading enzymes and cellulolytic fungus
326 with *A. fumigatus* by Sherief and colleagues (Sherief et al. 2010) in solid state fermentation using mixed substrates
327 containing rice straw with wheat bran in different proportions, high enzyme production was observed after 4 days of
328 incubation in 75% humidity, an initial pH of 5-6, at 40 °C, and in the presence of NaNO₃ as the nitrogen source, yielding
329 activities of 8.51 and 42.7 IU g⁻¹ for -Xylanase and β-glycosidase, respectively.

330 Regarding the data presented here, given that the optimum point could not be found for the enzymatic activity of
331 β-Xylosidase from *A. fumigatus* (CP-2 M-7S), additional tests were performed combining the maximum slope of the
332 surfaces, generating new data to set a point for maximum enzyme production. The results of the tests from the parameters
333 in Table 3 are shown in Fig. 4. The combinations in test 4 showed the best results, with 0.750 g of barley brewing residue
334 and 0.097 g of yeast extract in 25 mL of modified Czapeck medium, generating enzymatic activity equal to 154.01 U
335 mL⁻¹. Therefore, this combination was adopted as a central point for the second experimental design, entitled CCRD.

336 Table 7 presents the planning array for 2³ levels and the values of each variable used at each level with the yield
337 response of β-Xylosidase from *A. fumigatus* (PC-7S-2M), noting that the enzyme production varied from 150.86 to
338 252.26 U mL⁻¹. According to Abdeshahian and colleagues (Abdeshahian et al. 2010), the maximum production of β-
339 Xylosidase was 6.13 U mL⁻¹ when applied to an experimental design using *A. niger* grown on palm kernel cake as the
340 substrate. Lenartovicz and co-authors (Lenartovicz et al. 2003) used corn cob powder as the carbon source for culturing
341 another strain of *A. fumigatus* and obtained 45 U mL⁻¹ extracellular β-Xylosidase at a temperature of 42 °C for 72 hours.

342 Interesting data were shown by Gottschalk et al. (2013) evaluating the production of β-Xylosidase by the fungus
343 *A. awamori* in submerged culture at 30 °C with agitation at 200 rpm in medium supplemented with 30 g mL⁻¹ of wheat
344 bran in a pH range between 5.5 to 6.5. They used different nitrogen sources, such as yeast extract, sodium nitrate,
345 ammonium sulfate and urea, to give a high yield of the enzyme in media containing 685 U mL⁻¹ of urea at 144 h of
346 culture, and used less yeast extract in 210 U mL⁻¹ at 168 h.

347 In addition to the above analyses, there were no CCRD studies that showed the production of β-Xylosidase by
348 *A. fumigatus* using barley brewing residue. Additionally, these variables are differentiated, the enzyme production was
349 also optimized by applying a CCRD to obtain high levels of the enzyme for preliminary statistical tests and experimental
350 activity. Table 8 shows the ANOVA (analysis of variance) model that describes the variables studied, i.e., the production
351 of β-Xylosidase as a function of barley brewing residue, temperature and yeast extract, with a significance level of p <
352 0.10, indicating that it was possible to obtain a predictive model.

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$$\hat{\beta} = 242,88 - 14,07B^2 - 7,61T - 13,69T^2 - 6,24E - 25,02E^2 - 10,37BE \text{ (Eq. 4)}$$

355 ANOVA was used for assessing the significance of the model fit. The coefficient of determination (R²) was
356 0.74, which means that the biological process studied was considered predictive because predicted variables from barley
357 brewing residue, temperature and yeast extract corresponded to the production of β -Xylosidase. The model with
358 significant terms is shown in Eq. 4; the F calculated from the regression (4.90) was greater than the tabulated F (2.46),
359 which proved that the quadratic model was significant for the selected experiment. The lack of fit of the model was
360 determined from the calculated F (8.26) and tabulated F (9.37); the calculated F value is less than the tabulated F value,
361 which represents that there is no lack of fit in the mathematical model.

362 The surfaces represent the responses generated by the mathematical model, which enables verification of the
363 combinations of the three factors analyzed in the experiment, displaying the influence of each and the maximal activity
364 of the β -Xylosidase enzyme (Fig. 5). The conditions for increased production of β -Xylosidase are obtained at
365 concentrations that are close to the central point condition for the three factors; however, the surfaces have regions of
366 contour curves, which indicate that there are slightly lower values for the center point and that the three variables lead to
367 the same responses.

368 It is therefore an important step to validate the data to confirm that they were obtained in this graphical
369 representation. This process assists with obtaining the ideal conditions, enabling the formulation of the composition of
370 the medium that leads to the maximum production of β -Xylosidase by the fungus while minimizing the final cost of the
371 process because it uses a small number of trials without losing quality information about the results. Fig. 6 shows the
372 regression model that illustrates the independent variables and the interactive effects from the graphical response
373 surfaces.

374 From Fig. 6 (a), barley brewing residue shows better interaction with temperature, with the optimal point located
375 in the temperature range from 24 °C to 28 °C, combined with 0.725 g of barley brewing residue, and the desirability of
376 production of β -Xylosidase is greater than 240 U mL⁻¹. As shown in Fig. 6 (b), the optimal conditions of yeast extract
377 and barley brewing residue would be 0.097 g and 0.725 g, respectively, to obtain values greater than 200 U mL⁻¹ of
378 enzyme. From Fig. 6 (c), the optimum temperature range is from 24 °C to 28 °C with 0.097 g of yeast extract, enabling
379 enzyme production greater than 200 U mL⁻¹.

380 The trend of the results in this report was proven to be statistically significant because the calculated F values
381 were higher than the tabulated F values (Table 6). It was certainly possible to prove that the proposed model is valid,
382 generating first and second order mathematical models (Eqs. 3 and 4, respectively) that were represented by surface
383 graphs (Fig. 3 and 5).

384 After determining the conditions that maximize the production of the enzyme of interest, it is also necessary to
385 analyze the behavior of individual answers to ensure that all of them are acceptable in all regions with satisfied
386 constraints. Therefore, it is necessary to perform confirmatory experiments on the selected optimal conditions.

387 The optimum conditions for the production of β -Xylosidase presented on the desirability chart allow you to
388 select the optimal points for the production of this enzyme, in which the combination between the analyzed factors
389 enables the formulation of medium and cultivation conditions with points greatly under appropriate conditions that lead
390 to maximum production of the protein of interest (Rodrigues and Iemma, 2014). There is an optimum range for barley
391 brewing residue, which is greater than the range of values for yeast extract temperature. The data show that increasing
392 minimal amounts of yeast extract leads to rapid decline in enzyme production. Additionally, the combination of barley
393 brewing residue and temperature are lower in sensitivity, leading to a more slow decrease in the production of β -
394 Xylosidase.

395 Therefore, adding a greater amount of barley brewing residue (0.730 g) to the medium and growing *A. fumigatus*
396 at the optimal temperature of 27 °C with 0.100 g of yeast extract are the most favorable conditions for obtaining higher
397 amounts of β -Xylosidase. Therefore, changing the amount of yeast extract from 0.100 g to 0.125 g led to a sharp
398 decrease in enzyme production.

399 The conditions set in the experiment were validated, with up to 6 replications of dosages and performing
400 duplicates of the following conditions: barley brewing residue 0.730 g, 27 °C and 0.100 g of yeast extract. The cultures
401 were incubated for 4 days in liquid medium without agitation, as proposed initially, and then doses of β -Xylosidase were
402 added according to established protocols in the Materials and Methods.

403 The validation data showed an experimental result with average production of β -Xylosidase of 229.06 U mL⁻¹,
404 very close to the result predicted by the model (245.04 U mL⁻¹). Therefore, the experimental design was extremely
405 important for improving the enzymatic activity of the isolated fungal *A. fumigatus* (PC-7S-2M) in the presence of barley
406 brewing residue. Initially, classic growth and cultivation without application of experimental design obtained activity of
407 15 U mL⁻¹ for β -Xylosidase from this microorganism. After applying the experimental design and the variable conditions
408 discussed previously, it was possible to reduce spending on materials, reagents, and time of experiment, while obtaining
409 an average increase in the activity of β -Xylosidase, up to 229.06 U mL⁻¹. The production of the enzyme of interest has
410 been improved by 1,500% (15 times). To our knowledge, this is the first record of such significant enzyme activities for
411 β -Xylosidase from *A. fumigatus* using barley brewing residue as a carbon source.

412 The discovery of new fungal strains capable of producing enzymes can add scientific knowledge to the
413 development of sustainable and environmental technologies. Here, we have shown that the *A. fumigatus* strain (PC-7S-

414 2M) was new and isolated from an environment whose biodiversity is unexplored, which comprises western Paraná. The
415 results presented here provide a positive contribution to the survey of microorganism biodiversity. Moreover, we have
416 indicated that the produced enzyme could be tested for biotechnological purposes because it is abundantly produced at
417 high levels from the residue of a brewery in Brazil, which decreases its accumulation in the environment.

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422 **Conclusions**

423 In this study, the best substrate for high β -Xylosidase activity among the tests was barley brewing residue,
424 which has not been previously used for this enzyme in the *Aspergillus* genus. This crude enzyme extract showed an
425 optimum temperature of 45 °C and optimum pH of 5.5. The application of experimental design was effective for
426 optimizing the production of β -Xylosidase from a new strain of *A. fumigatus*, leading to production of high enzyme
427 levels under the optimum conditions, increasing the initial production of the enzyme from 15 U mL⁻¹ to 229.06 U mL⁻¹.
428 This result corresponds to a 1,500% (15 times) improvement in the efficiency of enzymatic activity. The application
429 allowed for the CCRD to achieve 93.47% of the predicted model. Therefore, β -Xylosidase from *A. fumigatus* (PC-7S-M
430 2) is an interesting enzyme to test for application in various industrial and biotechnological processes.

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Figure legends

Fig. 1 (a) Intracellular activity of β -Xylosidase from *A. fumigatus* (strain PC-7S-2) was measured after culturing for 10 days at 28°C in 25 ml of modified Czapeck liquid medium under shaking at 120 rpm (black columns) or under steady state (white columns) using 1% (w/v) of the different agroindustrial (PFP: Passion fruit peel; PP: Pokan Peel; BBR: Barley brewing residue; SF: soy flakes and RBP: Ripe banana peel) residues as carbon sources. (b) Measurement of

Factors	-1	0	+1
Barley brewing residue (g)	0.125	0.250	0.375
Temperature (°C)	28	35	42

intracellular β -Xylosidase mycelia of *A. fumigatus* (strain PC-7S-2) were grown in stationary liquid culture for 7 days using 1% (w/v) barley brewing residue as the carbon source. The experiments

were performed in duplicate, and measurements were taken in triplicate. The error bars represent the means of independent results.

Fig. 2 Comparison of linear effects for the production of β -Xylosidase (absolute values).

Fig. 3 (a) Response surfaces of the production of β -Xylosidase as functions of barley brewing residue and temperature, (b) yeast extract and barley brewing residue and (c) temperature and yeast extract, without the axial points.

Fig. 4 β -Xylosidase activity (U mL^{-1}) in eight different concentrations (g) of the barley brewing residue (BBR) and yeast extract (YE).

Fig. 5 Response surfaces of the production of β -Xylosidase as functions of barley brewing residue and temperature (a); yeast extract and barley brewing residue (b); and, temperature and yeast extract (c).

Fig. 6 Desirable optimal conditions for the production of β -Xylosidase.

Yeast extract (g)	0.025	0.052	0.080
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Table 1 Levels used in CCD for the three factors studied. (Not clear)

568 **Table 2** Central composite design (CCD) with the coded and real values for the factors in the
569 study: residue concentration, temperature and concentration of yeast extract
570

Runs	Coded values			Real values				
	BBR (g)	°C	YE (g)	BBR (g) %	°C	YE (g) %		
1	-1	-1	-1	0.125	0.5	28	0.025	0.10
2	1	-1	-1	0.375	1.5	28	0.025	0.10
3	-1	1	-1	0.125	0.5	42	0.025	0.10
4	1	1	-1	0.375	1.5	42	0.025	0.10
5	-1	-1	1	0.125	0.5	28	0.080	0.32
6	1	-1	1	0.375	1.5	28	0.080	0.32
7	-1	1	1	0.125	0.5	42	0.080	0.32
8	1	1	1	0.375	1.5	42	0.080	0.32
9	0	0	0	0.250	1.0	35	0.052	0.20
10	0	0	0	0.250	1.0	35	0.052	0.20
11	0	0	0	0.250	1.0	35	0.052	0.20

571 BBR: Barley brewing residue; YE: Yeast extract

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576 **Table 3**Maximum inclination
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Runs	BBR (g)	%	YE (g)	%
1	0.375	1.5	0.064	0.25
2	0.500	2.0	0.075	0.30
3	0.625	2.5	0.086	0.34
4	0.750	3.0	0.097	0.38
5	0.825	3.5	0.108	0.43
6	1.000	4.0	0.119	0.47
7	1.120	4.5	0.130	0.52
8	1.250	5.0	0.141	0.56

578 BBR: Barley brewing residue; YE: Yeast extract
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585 **Table 4-** Levels for the factors used in the second design, CCRD.
586

Factors	-1.68	-1	0	1	+1.68
Barley brewing residue (g)	0.515	0.600	0.725	0.850	0.935
Temperature (°C)	22	24	28	32	35
Yeast extract (g)	0.074	0.085	0.097	0.115	0.125

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590 **Table 5** - CCRD with the coded and real values given the factors in the study: temperature,barley brewing
591 residue and yeast extract concentration.
592

Runs	Coded values			Real values				
	BBR (g)	°C	YE (g)	BBR (g)%	°C	YE (g) %		
1	-1	-1	-1	0.600	2.4	24	0.085	0.3
2	1	-1	-1	0.850	3.4	24	0.085	0.3
3	-1	1	-1	0.600	2.4	32	0.085	0.3
4	1	1	-1	0.850	3.4	32	0.085	0.3
5	-1	-1	1	0.600	2.4	24	0.115	0.5
6	1	-1	1	0.850	3.4	24	0.115	0.5
7	-1	1	1	0.600	2.4	32	0.115	0.5
8	1	1	1	0.850	3.4	32	0.115	0.5
9	0	0	0	0.725	2.9	28	0.097	0.4
10	0	0	0	0.725	2.9	28	0.097	0.4
11	0	0	0	0.725	2.9	28	0.097	0.4
12	-1.68	0	0	0.515	2.1	28	0.097	0.4

13	+1.68	0	0	0.935	3.7	28	0.097	0.4
14	0	-1.68	0	0.725	2.9	22	0.097	0.4
15	0	+1.68	0	0.725	2.9	35	0.097	0.4
16	0	0	-1.68	0.725	2.9	28	0.074	0.3
17	0	0	+1.68	0.725	2.9	28	0.125	0.5

593 BBR: Barley brewing residue; YE: Yeast extract

594

595 **Table 6** -Summary of ANOVA of the first order mathematical model for β -xylosidase

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Variation source	SS	DF	MS	F Value	F _{Tab}
Regression	2,624.442	3	874.81	5.13	3.07
Residual	1,192.580	7	170.37		
Total	3,817.022	10			

597 SS: sum of squares; DF: degree of freedom, MS: mean square, $R^2=0.68$; p-value < 0.10

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601 **Table 7** - Planning with 2^3 levels for the factors and the production of β -Xylosidase

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Runs	Levels for the factors					β -Xylosidase(U ml ⁻¹)
	BBR (g)	°C	%	YE (g)	%	
1	0.600	2.4	24	0.085	0.3	205.09
2	0.850	3.4	24	0.085	0.3	231.89
3	0.600	2.4	32	0.085	0.3	197.82
4	0.850	3.4	32	0.085	0.3	220.04
5	0.600	2.4	24	0.115	0.5	220.95
6	0.850	3.4	24	0.115	0.5	184.81
7	0.600	2.4	32	0.115	0.5	169.9
8	0.850	3.4	32	0.115	0.5	174.18
9	0.725	2.9	28	0.097	0.4	252.26
10	0.725	2.9	28	0.097	0.4	237.73
11	0.725	2.9	28	0.097	0.4	244.43
12	0.515	2.1	28	0.097	0.4	184.23
13	0.935	3.7	28	0.097	0.4	192.38
14	0.725	2.9	22	0.097	0.4	209.88
15	0.725	2.9	35	0.097	0.4	183.14
16	0.725	2.9	28	0.074	0.3	150.86
17	0.725	2.9	28	0.125	0.5	163.94

603 BBR: Barley brewing residue; YE: Yeast extract

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608 **Table 8** - Summary of ANOVA of the 2nd order mathematical model for the production of β -
609 xylosidase

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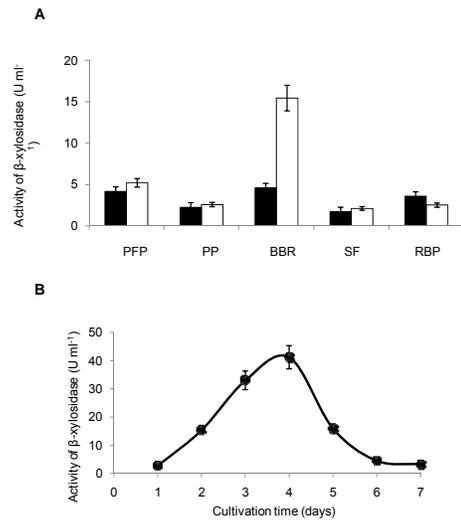
Variation source	SS	DF	MS	FValue	F _{Tab}
Regression	10,589.578	6	1,764.930	4.900	2.46
Residual	3,601.789	10	360,179		
Lack of fit	3,496.015	8	437,002	8.263	9.37
Pure error	105,773	2	52,887		
Total	14,191.367	16			

611 SS: sum of squares; DF: degree of freedom, MS: mean square; $R^2=0.74$; p-value < 0.10

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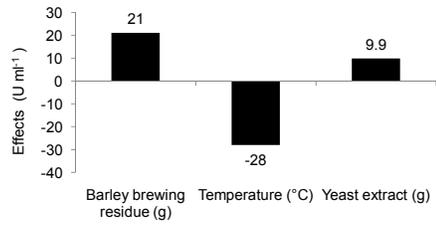
Fig. 1



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UNDER PEER REVIEW

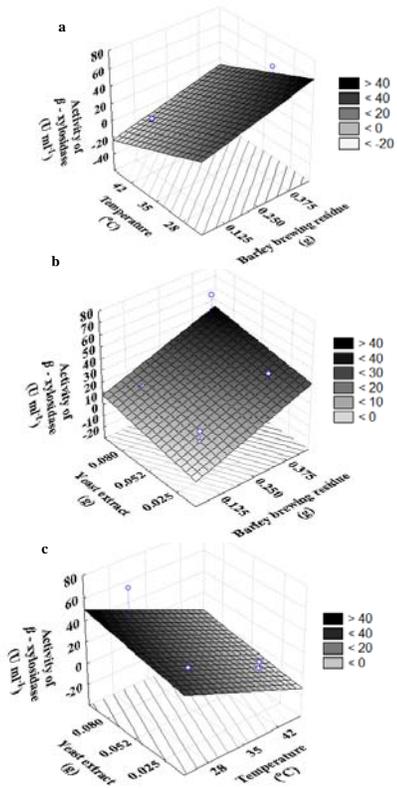
Fig. 2



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UNDER PEER REVIEW

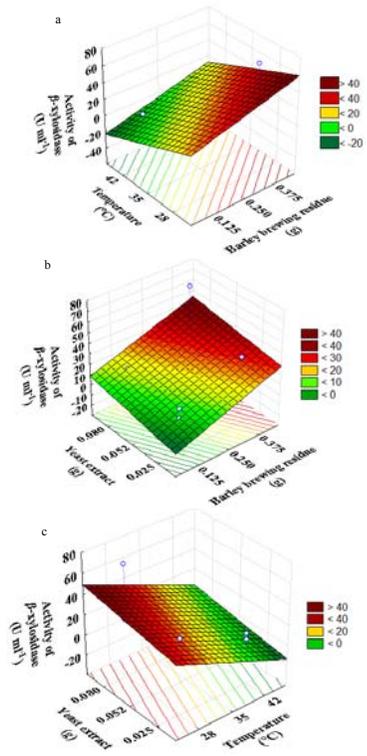
Fig. 3 - print version



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Fig. 3 – web version

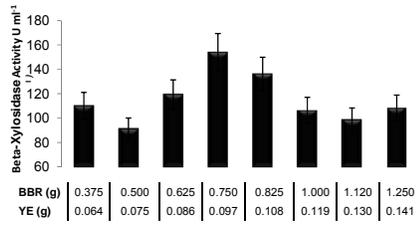


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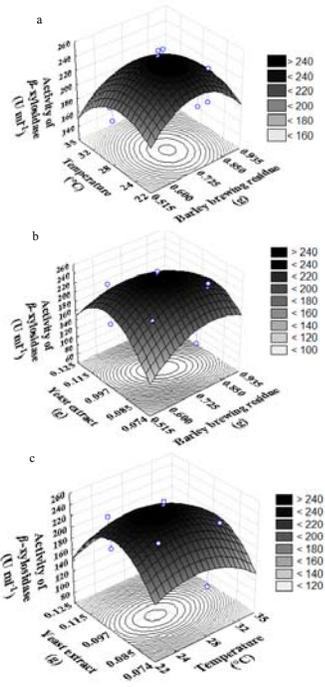
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Fig. 4



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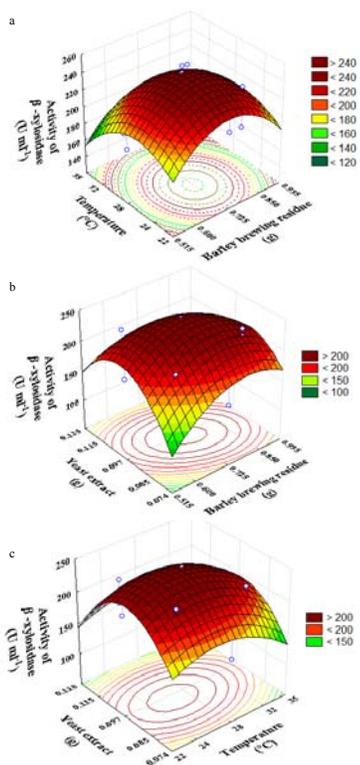
Fig. 5 print version



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UNDER PEER REVIEW

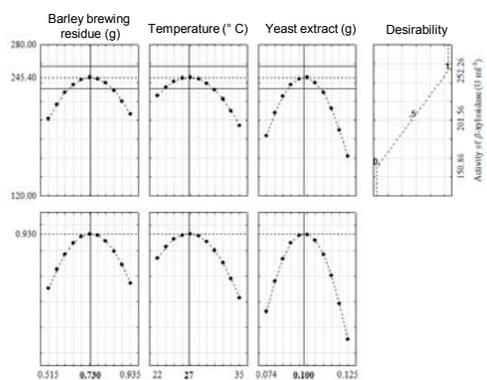
Fig. 5 – web version



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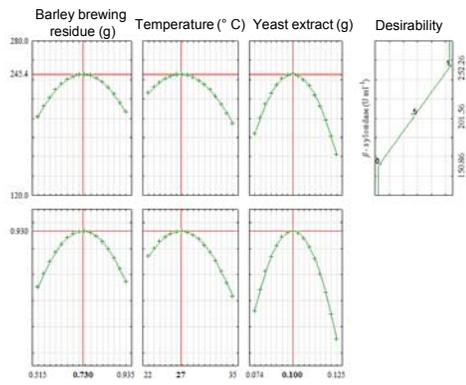
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Fig. 6 – Print version



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Fig. 6 - web version



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UNDER PEER REVIEW

$$\hat{y} = b_0 + \sum_{i=1}^3 b_i X_i + \sum_{i,j=1}^3 b_{ij} X_i X_j \quad (\text{Eq. 1})$$

$$\hat{y} = b_0 + \sum_{i=1}^3 b_i X_i + \sum_{i=1}^3 b_{ii} X_i^2 + \sum_{i,j=1}^3 b_{ij} X_i X_j \quad (\text{Eq. 2})$$

$$\hat{\beta} = 17,96 + 10,53B - 13,87T + 4,95E \quad (\text{Eq. 3})$$

$$\hat{\beta} = 242,88 - 14,07B^2 - 7,61T - 13,69T^2 - 6,24E - 25,02E^2 - 10,37BE \quad (\text{Eq. 4})$$

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UNDER PEE