Original research article Evolution and Emerging Trends in HFT Research

ABSTRACT

Aims: In this paper, we try to study the evolution and emerging trends of High Frequency Trading (HFT) research by examining papers published in the Web of Science (WOS) between 1993 and 2017.

Study design: A total of 241 papers were included, and 1876 keywords from these articles were extracted and analyzed.

Place and Duration of Study: For tracing the dynamic changes of the HFT Research, the whole 24 year was further separated three consecutive periods: 1993-2002, 2003-2012, and 2013-2017.

Methodology: The Ucinet is adopted to get keywords network, or knowledge network, to study the relationship of each research theme. NetDraw was applied to visualize network. We used social network analysis (SNA) technique to reveal patterns and trends in the research by measuring the association strength of terms representative of relevant publications produced in HFT field.

Results: Results indicate that HFT research has been strongly influenced by "market", "prices", "finance", "liquidity", "statistics", "financial markets", "stock", "stochastic", "model" and "trades" as shown in Table 1, which represent some established research themes. They are major focuses and the bridges connecting to other research themes in HFT. The detailed analysis in results and discussion provides an overview of evolution and emerging trends in HFT Research.

Conclusion: It concludes that market performance related keywords, which represent some established research themes, have become the major focus in HFT research. It also changes rapidly to embrace new themes. Especially, this research may make contribution to enlarge research method in that there is no SNA research in HFT research before.

Keywords: High Frequency Trading, HFT, social network analysis, SNA, emerging trends

1. INTRODUCTION

As the stock market has become nearly exclusively electronic, advances in computer technology and automated algorithm trading have speeding the transmission and execution of security transaction orders, and thus establishing High Frequency Trading (HFT) [1]. HFT is an emerging, ever changing and rapidly evolving area with highly interdisciplinary in nature for the markets, regulators, and the public [2]. This diversity may root from the emerging nature of computing technology and its wide appeal as well as unique researcher and practitioner viewpoints. Many academics raised the controversy concerning about HFT [3]. Even SEC Division of Trading and Markets Director Brett Redfearn admitted, "There are a lot of different definitions of HFT." The diverse issues and findings in the field of HFT represent the introduction of ideas and even new concepts about HFT. What are the areas

of focus in HFT? What are the developing trends in current research? Keywords have been generally identified as the words that reflect the research themes of individual publications that concern researchers. Further, keywords network represents relationships of keywords among HFT papers. When two keywords occur in a same article, it is an indication of connection between the themes which they represent. Therefore, a comprehensive network perspective analysis is required to reveal the developmental trends or future orientation of possible new research field from HFT.

- Social network analysis (SNA), sometimes also referred to as "structural analysis" [4], is a broad strategy for investigating social structures. For measurement, social network analysis (SNA) measures are a vital tool for understanding the behavior of networks and graphs. These algorithms use graph theory to calculate the importance of any given node in a network [5]. When they're well implemented, SNA measures allow the analyst to cut through noisy data and hone into the parts of a network that require further attention.
- In this paper, our focus is to construct and analyze keywords network by using the Social network analysis (SNA) techniques which have already been widely applied in many disciplines of science. Specifically, this study will quantitatively analyze existing empirical and theoretical HFT papers to address the following objectives:
- 1) To construct keywords network from HFT papers published in world leading journals during the period from 1993 to 2017.
- 48 2) To investigate the characteristics of keywords network of HFT papers by utilizing Social Network Analysis (SNA) techniques.
- 50 3) To find and compare the changes in keywords network of HFT papers over time.
- These investigations can help researchers to realize the breadth of HFT research and to establish future research directions and to provide an entry point to any academic, regardless of their prior knowledge of the theme.

2. METHODOLOGY

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2.1 Publication search

The objective of the present work is to identify the important keywords from the scientific output on the latest advances in HFT, and to describe the characteristics of the network of keywords of HFT research. To achieve these goals, we selected the Web of Science (WOS), which includes SCIE and SSCI and A&HCI from the Institute of Scientific Information (ISI) Web of Science databases. WOS is the most important and frequently used source for a broad review of scientific accomplishment in all research fields [6]. We constructed a database composed of keywords from HFT papers published in the WOS during the 24-year period from 1993 to 2017. The keywords were obtained from following two sources: (1) Author Keywords and (2) Keywords Plus in the ISI database [7].

2.2 Refinement of keywords and keywords databases

Due to different words may represent same or similar ideas and concepts, we standardize the keywords before constructing the keywords network. The basic rule for the refinement of keywords was that all keywords with identical meaning or similar ideas or concepts or even

misspelled keywords from different articles will be grouped and considered as a single keyword. This refinement leads to a meaningful keywords database. The example of SNA steps in literature-based research was shown in Fig.1.

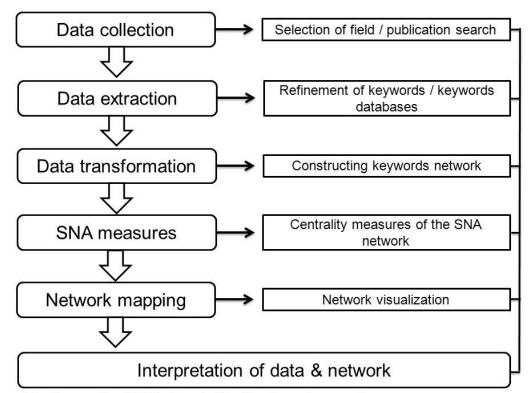


Fig. 1 example of SNA steps in literature-based research

2.3 Constructing keywords network

The construction of keywords network is based on three continuous stages which include data collection, data extraction, and data transformation. During the data extraction stage, core keywords are identified from HFT papers and are changed to a standard form. Then in the data transformation stage, all the refined keywords will be input to the most popular social network research tool, Ucinet 6 for Windows [8] to get keywords network, or knowledge network, to study the relationship of each research theme.

2.4 Centrality measures of the SNA network

Network centrality [9] in the keywords network can measure the degree of relations among keywords. Social network analysis (SNA) measures include measuring degree centrality, betweenness centrality, closeness centrality, EigenCentrality or PageRank for each network quantitatively [10]. In order to understand the characteristics of the overall keywords network in HFT research, we selectively used betweenness centrality measuring to study the relationship of each research theme. Betweenness centrality is the extent to which a node lies on the paths between other nodes. It is measured as the fraction of the shortest paths between all pairs of other nodes in the network containing the node. A keyword that lies between two distinctive research themes can have high betweenness centrality even though

it may have a small number of connections to other keywords in each theme [11]. In the keywords network, this represents the importance of a keyword in bridging subsets of keywords.

2.5 Network visualizations

Network visualizations is generally known as network mapping which can be generated from raw network data within Netdraw, a mapping program in Ucinet. NetDraw was applied to visualize network. It helps to obtain a clear sense of connectivity of keyword networks and to illustrate the overall patterns of networks over time. This method enables the researchers to explicitly understand representation of emerging themes.

3. RESULTS AND DISCUSSION

3.1 Keywords network

Fig. 2 shows keywords network by co-occurrence (1993-2017). The nodes are the keywords. The size of nodes can reflect the frequency of keywords. Larger size of node means higher frequency of occurrence of keyword. The lines between two nodes stand for the associations of two keywords, or represent the co-occurrence of these keywords in a paper. The thickness of line indicates the co-occurrence frequency of keyword pairs, or represents the number of times each pair of keywords was mentioned together in papers. The thickness of line is proportional to the closeness of connections between two keywords. The thicker line between two keywords, the closer their relationship is. The more co-occurrence between two keywords, the closer their relationship is. It shows the strength of the connection. According to Fig.2, we can see that keywords such as "market", "prices", "finance", "liquidity", "statistics", "financial markets", "stock", "stochastic", "model" and "trades" became important keywords, which means that they have played an important role in bridging other research themes.

3.2 Betweenness centrality measuring for all period (1993-2017)

Keywords serve as an indicator of the importance of the research themes they represent. The top ten keywords from betweenness centrality measuring for all period (1993-2017) are "market", "prices", "finance", "liquidity", "statistics", "financial markets", "stock", "stockastic", "model" and "trades" as shown in Table 1. The results indicate that these research themes are major focuses and the bridges connecting to other research themes in HFT. These findings show that these research themes attract more attention and have a closer relationship with other research themes in HFT. Notice that keywords like "High Frequency Trading" and "Algorithm(s)" have very broad meanings. Due to this kind of keywords are meaningless for this study, we excluded them from the above analysis.

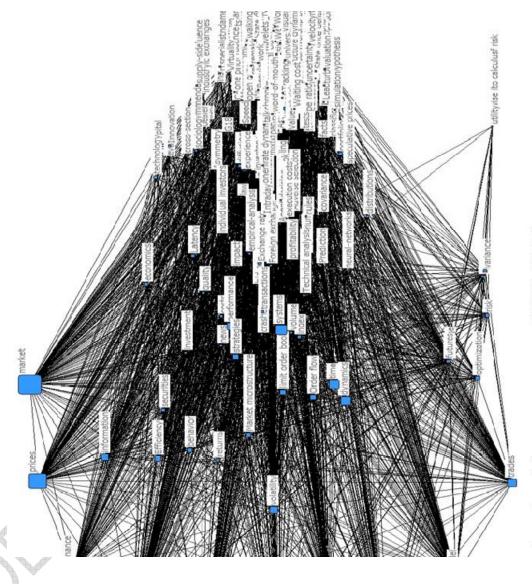


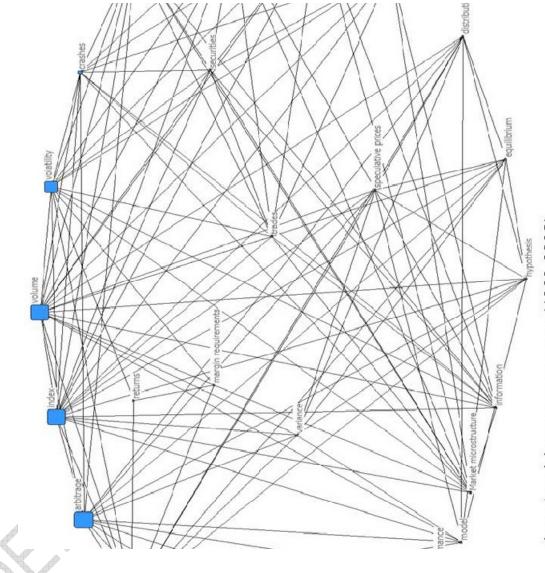
Table 1:Betweenness centrality measuring for all period (1993-2017)

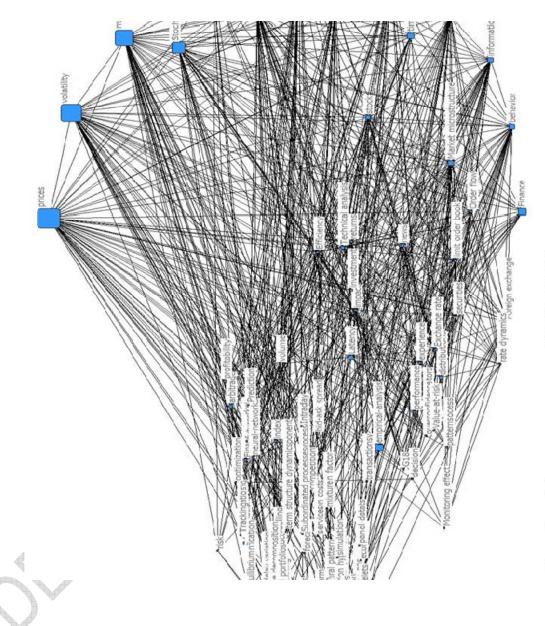
		1993 - 2017				1993 - 2017	
No.	rank	Keywords		No.	rank	Keywords	
196	1	High-frequency trading	20972.666	99	46	costs	479.408
13	2	Algorithms	14873.707	142	47	empirical-analysis	428.283
258	3	market	11343.833	339	48	quality	425.657
333	4	prices	9020.214	435	49	volume	425.474
169	5	Finance	8998.353	430	50	variance	420.01
250		Liquidity	8372.251	378	51	sociology	403.26
389	7	Statistics	6550.62	329		power	381.97
170		Financial markets	6365.009			Technical analysis	378.1
391		stock	5479.472			Foreign exchange	343.94
390		Stochastic	5255.224			universal portfolios	339.00
278		model	5207.57			impact	305.744
419		trades	4817.368			Exchange rate	291.83
408		systems	4643.722			Prediction	284.32
132		dynamics	4483.216			options	283.81
416		time	3957.8			equilibrium	253.83
434		volatility	3471.744	78		competition	241.31
255		management	3040.512	10		Agent-based modelling	209.28
215		information	2945.935			Innovation	207.79
302	19	Order flow	2761.069	291		neural-networks	194.05
392		strategies	2683.609	213	65	individual investors	186.
319	21	performance	2651.219	100	66	covariance	172.82
139	22	Efficiency	2355.799	91	67	Content-based	161.02
37	23	behavior	1895.172	39	68	bid-ask spread	158.613
259	24	Market microstructure	1890.566	115	69	decision	150.69
300	25	optimization	1622.698	371	70	sharpe ratio	140.98
352	26	returns	1461.738	155	71	evolution	129.90
210	27	index	1404,703	337	72	profitability	124.693
249	28	limit order book	1389.61	364	73	selection	123.28
54		capital	1313,427		74	Manipulation	117.72
326		portfolio	1312.679			turbulence	115.05
19		arbitrage	1276.097	159		execution costs	98.26
240		Latency	1247.931			law	94.13
184		futures	1177.844			rules	85.18
363		securities	1130.502			Lead-lag relationship	82.59
411		technology	1065.972			exchange	76.93
354		risk	1020.679	9		Adverse selection	70.17
226		investment	974.707	18		Approximation	68.29
138		economics	806.251	160		experience	63.36
293		news	750.328	22		ask	51.96
420		transactions	713.42	27		Asymmetry	40.40
30		Automation					
			681.092	70		Codings	40.02
122		diffusion	652.382			dealer	39.83
128		distributions	584.501	62		classification	39.25
101		crashes	532.398			speculative prices	38.483
297	45	Online learning	501.978	223	90	Intraday	38.16

3.3 Changes in important keywords over time

How have the important keywords changed over time and what are the recent important keywords? In order to trace dynamic changes of the HFT Research, the whole 24 year was further separated three consecutive periods: 1993-2002, 2003-2012, and 2013-2017. We constructed three keywords networks as shown in Fig. 3 to 5. For showing statistics of keywords network in different time slices, we compared the rank of the important keywords in the three keywords networks constructed as shown in Fig. 6 in order to thoroughly and precisely analyze the variations of trends. Please notice that the important keywords are from top ten keywords in Table 1. For the full lists of keywords in these three periods, see Appendix A through Appendix C.

This comparison reveals some notable results. "Market" revealed to be the most important keyword by betweenness centrality measuring for all three periods, because it has received consistent upward attention. "Stock" even received sharply upward attention since 1993 until 2017. "Liquidity" and "finance" and "financial markets" are emerging theme since 2003 year due to they were not appeared in period of 1993 to 2002. "Model" and "trades" were paid growing attention from 1993 through 2012 period, while 2013 to 2017 were not. The reason may be that "model" and "trades" are viewed as common sense already in HFT research until recent years. "Prices" and "stochastic" emerged since 2003 year, but they were paid less attention from 2013 through 2017 period. The above analysis provides an overview of HFT research and it concludes that market performance related keywords, which represent some established research themes, have become the major focus in HFT research. It also changes rapidly to embrace new themes.





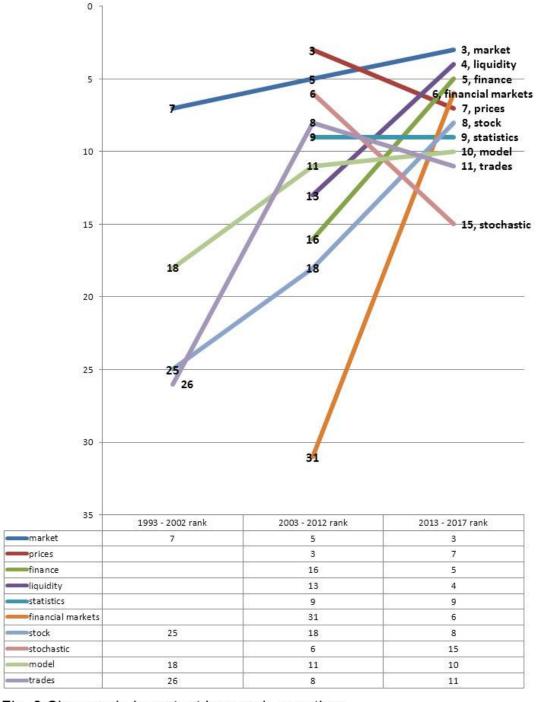


Fig. 6 Changes in important keywords over time

4. CONCLUSION

In this article, we used social network analysis (SNA) technique to give a comprehensive understanding of HFT research during 1993 to 2017. We obtain some clear and reasonable results which can provide useful insights to better understand evolution and emerging trends in HFT research.

Results indicate that HFT research has been strongly influenced by "market", "prices", "finance", "liquidity", "statistics", "financial markets", "stock", "stochastic", "model" and "trades", which represent some established research themes. They are major focuses and the bridges connecting to other research themes in HFT. "Market" revealed to be the most important keyword by betweenness centrality measuring for all three periods, because it has received consistent upward attention. "Stock" even received sharply upward attention since 1993 until 2017. "Liquidity" and "finance" and "financial markets" are emerging theme since 2003 year due to they were not appeared in period of 1993 to 2002. "Model" and "trades" were paid growing attention from 1993 through 2012 period, while 2013 to 2017 were not. The reason may be that "model" and "trades" are viewed as common sense already in HFT research until recent years. "Prices" and "stochastic" emerged since 2003 year, but they were paid less attention from 2013 through 2017 period. The above analysis provides an overview of HFT research and it concludes that market performance related keywords, which represent some established research themes, have become the major focus in HFT research. It also changes rapidly to embrace new

This research is just a preliminary and still has limitations need to be addressed. The main limitation of SNA technique is that it is just one of the tools that can be used to understand evolution and emerging trends in HFT research. It is just one piece of the puzzle. Subject matter experts are needed to provide a context for the research. On the other hand, this study tries to explore the evolution and emerging trends in HFT papers published in world leading journals but the Web of Science database may not completely cover the scientific research

In the future, comparative research with other method in the same HFT field could also be explored because different methods may have very different research emphases which would also be worthy of further exploration to extend HFT research theme.

This study utilizes the advantage of SNA technique and such keywords analysis might be helpful to stimulate further research or identify some fruitful future research opportunities.

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Appendix A
Betweenness centrality measuring for the first sub-period (1993-2002)

		1993 - 2002	
No.	rank	Keywords	
8	1	futures	91.474
1	2	arbitrage	69.006
11	_	index	68.29
27		volume	68.29
26		volatility	46.118
5		crashes	9.371
14		market	9.371
2		bid-ask spread	0
3		components	0
4		costs	0
6		distributions	0
7		equilibrium	0
9		High-frequency trading	0
10		hypothesis	0
12		information	0
13		margin requirements	0
15		Market microstructure	0
16	18	model	0
17	19	performance	0
18	20	profitability	0
19	21	returns	0
20	22	risk	0
21	23	securities	0
22	24	speculative prices	0
23		stock	0
24	26	trades	0
25	27	variance	0

Appendix B
Betweenness centrality measuring for the second sub-period (2003-2012)

No. rank				measuring t	or the	secor	nd sub-period (2003-2012)	
S			2003 - 2012				2003 - 2012	
113 3 prices 1943.382 62 48 futures 19							•	
113 3 prices 1943.382 62 48 futures 19. 153 4 volatility 1592.97 13 49 bid-ask spread 18. 86 5 market 1466.067 149 50 Value-at-risk 15. 129 6 Stochastic 1124.416 75 51 Intraday 12. 130 7 systems 1108.412 15 52 Boosting 2. 144 8 trades 844.66 1 53 1st passage 128 9 Statistics 844.555 2 54 Active measurement 131 10 strategies 776.203 3 55 Adaptive trader-agents 92 11 model 714.488 4 56 Agent-based modelling 141 12 time 550.082 6 57 amorphous solids 14 17 12 time 550.082 6 57 amorphous diffusion 17 14 information 387.353 8 59 Approximation 17 15 behavior 379.06 10 60 Asynchronous data 15 behavior 379.06 10 60 Asynchronous data 15 behavior 379.06 10 60 Asynchronous data 15 behavior 305.516 16 62 C33 C31 19 distributions 198.327 18 64 C50 C50 137 20 Technical analysis 190.978 19 65 cascades 190.978 19 69 Codes of conduct 190.978 19 65 cascades 190.978			•				100.000	21.541
153				1947.709				21.067
86 5 market 1466.067 149 50 Value-at-risk 15. 129 6 Stochastic 1124.416 75 51 Intraday 12. 136 7 systems 1108.412 15 52 Boosting 2. 144 8 trades 844.666 1 53 1st passage 2. 128 9 Statistics 844.355 2 54 Active measurement 131 10 strategies 776.203 3 55 Adaptive trader-agents 92 11 model 714.488 4 56 Agent-based modelling 141 12 time 550.082 6 57 amorphous solids 84 13 Liquidity 393.819 7 58 anomalous diffusion 12 15 behavior 379.06 10 60 Asynchronous data 15 16 Finance 330.972 14 61 <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td>19.741</td>								19.741
129	153	4	volatility	1592.97	13	49	bid-ask spread	18.193
136	86		37.335.536.5.5.37.74.		149	50	Value-at-risk	15.594
1444 8 trades 844.66 1 53 1st passage 128 9 Statistics 844.355 2 54 Active measurement 131 10 strategies 776.203 3 55 Adaptive trader-agents 92 11 model 714.488 4 66 Agent-based modelling 141 12 time 550.082 6 57 amorphous solids 84 13 Liquidity 393.819 7 58 anomalous diffusion 73 14 information 387.353 8 59 Approximation 12 15 behavior 379.06 10 60 Asynchronous data 55 16 Finance 330.972 14 61 Binary classification 87 17 Market microstructure 305.516 62 C33 3130 18 stock 276.927 17 63 C41 41 19 distributions 199.327 18 64 C50 137 20 Technical analysis 190.978 19 65 cascades	129	6	Stochastic	1124.416	75			12.218
128	136	7	systems	1108.412	15	52	Boosting	2.133
131 10 strategies 776.203 3 55 Adaptive trader-agents 92 11 model 714.488 4 56 Agent-based modelling 141 12 time 550.082 6 57 amorphous solids 84 13 Liquidity 393.819 7 58 anomalous diffusion 73 14 information 387.353 8 59 Approximation 12 15 behavior 379.06 10 60 Asynchronous data 15 behavior 379.06 10 60 Asynchronous data 17 Market microstructure 305.516 16 62 C33 C31 C33 C34 C		8	trades	844.66	1	53	1st passage	0
92 11 model 714.488 4 56 Agent-based modelling 141 12 time 550.082 6 57 amorphous solids 84 13 Liquidity 393.819 7 58 anomalous diffusion 73 14 information 387.353 8 59 Approximation 12 15 behavior 379.06 10 Asynchronous data 55 16 Finance 330.972 14 61 Binary classification 87 17 Market microstructure 305.516 16 62 C33 130 18 stock 276.927 17 63 C41 41 19 distributions 198.327 18 64 C50 137 20 Technical analysis 190.978 19 65 cascades 95 21 news 186.846 20 66 choice 80 22 Latency <td>128</td> <td>9</td> <td>Statistics</td> <td>844.355</td> <td>2</td> <td></td> <td></td> <td>0</td>	128	9	Statistics	844.355	2			0
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73 14 information 387.353 8 59 Approximation 12 15 behavior 379.06 10 60 Asynchronous data 55 16 Finance 330.972 14 61 Binary classification 87 17 Market microstructure 305.516 16 62 C33 130 18 stock 276.927 17 63 C41 41 19 distributions 198.327 18 64 C50 137 20 Technical analysis 190.978 19 65 cascades 95 21 news 186.846 20 66 choice 80 22 Latency 164.73 21 67 classification 9 23 arbitrage 163.332 22 68 Cloud computing 45 24 Efficiency 135.079 23 69 Codes of conduct 46 25 empirical-analysis 134.262 24 70 Codings 100 26 Order flow 130.235 25 71 Commodity hardware 58 27 Foreign exchange 128.547 26	141	12	time	550.082	6	57	amorphous solids	0
12	84	13	Liquidity	393.819	7	58	anomalous diffusion	0
12 15 behavior 379.06 10 60 Asynchronous data 55 16 Finance 330.972 14 61 Binary classification 87 17 Market microstructure 305.516 16 62 C33 130 18 stock 276.927 17 63 C41 41 19 distributions 198.327 18 64 C50 137 20 Technical analysis 190.978 19 65 cascades 95 21 news 186.846 20 66 choice 80 22 Latency 164.73 21 67 classification 9 23 arbitrage 163.332 22 68 Cloud computing 45 24 Efficiency 135.079 23 69 Codes of conduct 46 25 empirical-analysis 134.262 24 70 Codings 100 26	73	14	information	387.353	8	59	Approximation	0
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130 18 stock 276.927 17 63 C41 41 19 distributions 198.327 18 64 C50 137 20 Technical analysis 190.978 19 65 cascades 95 21 news 186.846 20 66 choice 80 22 Latency 164.73 21 67 classification 9 23 arbitrage 163.332 22 68 Cloud computing 45 24 Efficiency 135.079 23 69 Codes of conduct 46 25 empirical-analysis 134.262 24 70 Codings 100 26 Order flow 130.235 25 71 Commodity hardware 58 27 Foreign exchange 128.547 26 72 Common factor 76 28 investment 128.284 27 3 Commonality 118 29 returns 114.102 28 74 competition 83 30 limit order book 109.02 29 75 component analysis 56 31 Financial markets 97.433<	55	16	Finance	330.972	14	61	Binary classification	0
41 19 distributions 198.327 18 64 C50 137 20 Technical analysis 190.978 19 65 cascades 95 21 news 186.846 20 66 choice 80 22 Latency 164.73 21 67 classification 9 23 arbitrage 163.332 22 68 Cloud computing 45 24 Efficiency 135.079 23 69 Codes of conduct 46 25 empirical-analysis 134.262 24 70 Codings 100 26 Order flow 130.235 25 71 Commodity hardware 58 27 Foreign exchange 128.547 26 72 Common factor 76 28 investment 128.284 27 73 Commonality 118 29 returns 114.102 28 74 competition 83 30 limit order book 109.02 29 75 component analysis 56 31 Financial markets 97.433 30 76 components 107 32 performance 87.288 31 77 continuous double auction 71 33 index 56.19 32 78 costs	87	17	Market microstructure	305.516	16			0
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Appendix C
Betweenness centrality measuring for the third sub-period (2013-2017)

			y measuring	for th	e thir	d sub-period (2013-2017)	
		2013 - 2017				2013 - 2017	
No.	rank	Keywords			rank	Keywords	
163	1	High-frequency trading	15349.117	255		options	322.945
10		Algorithms	9033.231	277	47	power	320.466
217	3	market	8454.144	248	48	news	298.916
211	4	Liquidity	7070.412	365	49	volume	244.794
143	5	Finance	6733.11	362	50	variance	210.176
144	6	Financial markets	5455.364	246	51	neural-networks	206.152
280	7	prices	5301.453	7	52	Agent-based modelling	185.942
333	8	stock	5137.49	279	53	Prediction	181.464
331	9	Statistics	4706.375	62	54	competition	168.874
234	10	model	3940.322	171	55	impact	158.898
353	11	trades	3479.517	74	56	Content-based	144.998
111	12	dynamics	3275.315	309	57	selection	135.227
346	13	systems	2731.716	203	58	law	107.017
275	14	portfolio	2696.57	216	59	Manipulation	104.194
332	15	Stochastic	2543.021	120	60	empirical-analysis	97.351
215	16	management	2533.632	305	61	rules	95.875
256	17	Order flow	2276.406	83	62	covariance	85.314
352		time	2174.244	181	63	Innovation	85.282
180	19	information	2104.56	127	64	equilibrium	79.572
269	20	performance	1684.337	178	65	individual investors	77.577
254	21	optimization	1560.585	134	66	exchange	75.6
117	22	Efficiency	1499.502	33	67	bid-ask spread	74.359
44	23	capital	1204.612	136		execution costs	68.596
297		returns	1129.319	6	69	Adverse selection	64.104
31	25	behavior	1043.882	315	70	sharpe ratio	58.984
210	26	limit order book	981.42	348	71	Technical analysis	53.715
349	27	technology	929.715	17	72	ask	52.004
218	28	Market microstructure	885.26	135	73	Exchange rate	48.534
175	29	index	855.817	22	74	Asymmetry	45.24
364	30	volatility	833.319	139	75	facts	42.178
14	31	arbitrage	755.86	94	76	dealer	35.465
299	32	risk	752.568	38	77	book	33.13
308	33	securities	745.66	97	78	decision	31.873
191	34	investment	711.843	132	79	evolution	31.071
155	35	futures	635.551	192	80	issues	27.821
354	36	transactions	618.743	327	81	spread	23.048
334	37	strategies	590.264	106	82	discovery	22.219
202		Latency	579.702	133		Evolutionary computation	20.034
24	39	Automation	509.524			Momentum	18.852
103		diffusion	495.759	50	85	classification	17.174
116	41	economics	456.811	245		networks	16.995
285		quality	415.741	190		Inventory risk	16.062
321		sociology	409.809	8		aggressiveness	15.185
82		costs	401.178		89	entropy	14.797
84		crashes	334.673	89	_	cross-section	14.076