

3
4 **Oblique Propagation of Nonlinear Solitary Waves in**
5 **Magnetized Plasma with Nonextensive Electrons**
6

7
8
9
10
11 **ABSTRACT**
12

In this paper, authors have studied the properties of obliquely propagating nonlinear solitary waves in a plasma system consisting of warm ions and nonextensively distributed electrons. The nonlinear Korteweg-de-Vries (KdV) equation and its solution have been derived using the standard reductive perturbation method. The effect of ion temperature on the propagation of solitary waves has been investigated numerically. The critical value of nonextensivity at which solitary structures transit from negative to positive potential is found to shift to the lower value under the effect of finite temperature. The numerical results are interpreted graphically. The results may be useful for understanding the wave propagation in laboratory and space plasmas where magnetic field is present.

13
14 *Keywords: Magnetized plasma, q-nonextensive distribution, reductive perturbation method,*
15 *nonlinear waves and soliton*
16

17 **1. INTRODUCTION**

18 The nonlinear wave structures have provided a fascinating field of research for the
19 plasma physics community owing to their importance in explaining various laboratory, space
20 and astrophysical atmospheres [1-3]. Nonlinear structures like solitons, shock waves, double
21 layers etc. are observed in space and laboratory. Out of them, solitons have become the
22 main source of interest for the researchers from across the globe owing to their rich physical
23 insight underlying the various nonlinear phenomena. Solitons are stable nonlinear entities
24 and arise due to a delicate balance of nonlinearity and dispersion. Nonlinear wave structures
25 in various plasma models and compositions have been investigated theoretically and
26 observationally for the last half century [4-8]. The existence of magnetic field in a plasma
27 system has found a significant impact on the nonlinear wave propagation. Such a strong
28 magnetic field is observed to exist on the surface of fast rotating neutron stars and in the
29 pulsar magnetosphere [9-10]. Considering this, an immense interest has been developed in
30 researchers to study nonlinear propagation of ion-acoustic waves in magnetized plasmas
31 [11-15]. Dubouloz et al [16] reported that the electric field spectrum produced by an electron-
32 acoustic solitary wave (EASW) is not significantly modified by the presence of a magnetic
33 field. Mace and Hellberg [17] studied the influence of the magnetic field on the features of
34 the weakly nonlinear electron-acoustic waves in magnetized plasma. They predicted the
35 existence of negative potential structures in both magnetized and unmagnetized cases.
36 Devanandhan et al [18] have investigated EASWs in two component magnetized plasma
37 and predicted negative solitary potential structures. They further showed that with the
38 increase in magnetic field, the soliton electric field amplitude increases while the soliton
39 width and pulse duration decreases. The properties of small amplitude wave in magnetized
40 plasma are investigated by Pakzad and Javidan [19]. They observed both rarefactive and

41 compressive solitons whose profiles become narrower with the application of stronger
42 magnetic fields.

43 The deviations of electron populations from their thermodynamic equilibrium have been
44 reported by many space plasma observations. A nonextensive distribution is the most
45 generalized distribution to study the linear and nonlinear properties of solitary waves in
46 different plasma systems, where the non-equilibrium stationary states exist. The
47 nonextensive statistical mechanics has gathered immense attention over the last two
48 decades. This mechanics is based on the deviations of Boltzmann-Gibbs-Shannon (B-G-S)
49 entropy measures first recognized by Renyi [20] subsequently proposed by Tsallis [21]. The
50 Maxwellian distribution in Boltzmann-Gibbs statistics is valid universally for the macroscopic
51 ergodic equilibrium systems. While for systems having long-range interactions, the complete
52 description of the features becomes inadequate with Maxwellian distribution. The parameter
53 q that underpins the generalized entropy of Tsallis, is associated to the underlying dynamics
54 of the system and measures the amount of its nonextensivity. For $q < 1$ (i.e. superextensivity),
55 the generalized entropy of whole (i.e. S_{whole}) is greater than the entropies of subsequent
56 parts (i.e. $S_{\text{sub-parts}}$). However $q > 1$ i.e. subextensivity corresponds to $S_{\text{whole}} < S_{\text{sub-parts}}$. The
57 nonextensive statistics has found applications in a large quantity of astrophysical and
58 cosmological atmospheres such as stellar polytropes [22], the solar neutrino problem [23],
59 peculiar velocity distributions of galaxies [24] and systems with long range interactions and
60 also fractal-like space-times. Different types of waves, viz. ion acoustic (IA) waves, electron-
61 acoustic (EA) waves, or dust-acoustic (DA) waves in nonextensive plasmas are investigated
62 by many researchers considering one or two components to be nonextensive [25-33].
63 Ferdousi et al [34] studied the properties of small amplitude ion-acoustic solitary waves
64 (IASWs) in three component magnetized electron-positron-ion plasma. They considered
65 Tsallis distributed electrons and cold ions for their analysis and discussed the effects of
66 magnetic field and electron and positron nonextensivity on the propagation of solitary waves.
67 However, in the present investigation, we aim at studying the effect of ion temperature on
68 the obliquely propagating solitary waves in two component magnetized plasma system with
69 nonextensive distributed electrons. The paper is organized as follows: in Sec. 2, the basic
70 equations governing the plasma dynamics and the derivation of Korteweg-de Vries (KdV)
71 equation is given. In Sec. 3, we present the numerical analysis and discussion of the results.
72 Finally, we conclude the paper in Sec. 4.

73
74

2. BASIC EQUATIONS AND NONLINEAR ANALYSIS

75 Let us consider the homogeneous magnetized plasma containing q -nonextensive electrons
76 and stationary warm ions. The external static magnetic field is assumed to point in the z -
77 direction i.e. $B = B_0 \hat{z}$. The dynamics of the propagation of waves in such magnetized
78 plasma is governed by the following set of normalized equations:

79
$$\frac{\partial n}{\partial t} + \nabla \cdot (nu) = 0 \quad (1)$$

80
$$\frac{\partial u}{\partial t} = (u \cdot \nabla)u = -\nabla \phi - \omega_0 (u \times \hat{z}) - \frac{5}{3} \frac{\sigma}{n^{1/3}} \nabla n \quad (2)$$

81
$$\nabla^2 \phi = n_e - n \quad (3)$$

82
83
84
85
86

where n and u are the ion number density and ion fluid velocity normalized to equilibrium
plasma density n_0 and ion acoustic speed $C_s = (T_e/m)^{1/2}$, T_e is the electron temperature and m
is the mass of positively charged ions, respectively. ϕ is the electrostatic wave potential
normalized to T_e/e , where e is the magnitude of electron charge and $\sigma = T_i/T_e$ with T_i being the

87 ion temperature. In this plasma model, ion plasma period $\omega_p^{-1}=(m/4\pi n_0 e^2)^{1/2}$, the Debye
 88 length $\lambda_D=(T_e/4\pi n_0 e^2)^{1/2}$ and ion cyclotron frequency is given by $\omega_c=(eB_0/m)$. The number
 89 density of electron fluid with nonextensive distribution is given by:

$$90 \quad n_e = \left(1 + (q-1)\phi\right)^{\frac{(q+1)}{2(q-1)}} \quad (4)$$

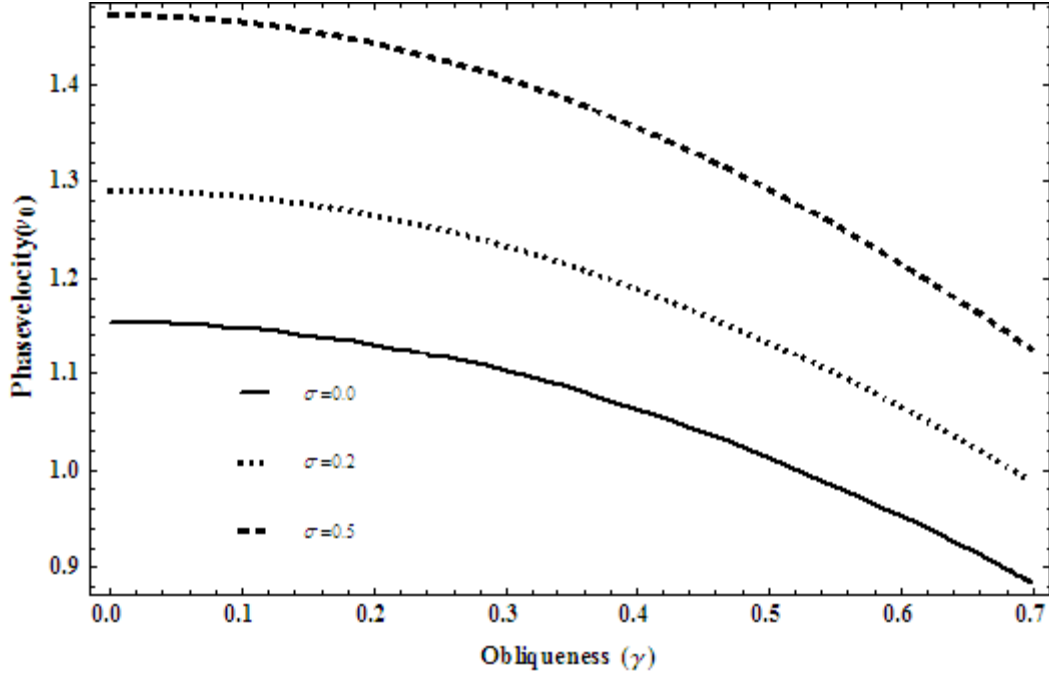
91 where q is the nonextensivity parameter. The electron distribution reduces to the well-known
 92 Maxwell Boltzmann distribution for the extensive limiting case q approaches to 1 [33]. In
 93 transformations given by Gardner and Morikawa [35] put $\alpha=1/2$ the stretched coordinates
 94 becomes $\xi=\varepsilon^{1/2}(l_x x+l_y y+l_z z-v_0 t)$, $\tau=\varepsilon^{3/2}t$. Here v_0 is the linear phase velocity and ε is a small
 95 parameter. l_x, l_y, l_z are the direction cosines of the wave vector with respect to the x, y and z
 96 axes respectively. The perturbed quantities are expanded in power series of ε as follows:
 97
 98

$$99 \quad \begin{aligned} n &= 1 + \varepsilon n^{(1)} + \varepsilon^2 n^{(2)} + \varepsilon^3 n^{(3)} + \dots \\ u_{x,y} &= 0 + \varepsilon^{\frac{3}{2}} u_{x,y}^{(1)} + \varepsilon^2 u_{x,y}^{(2)} + \varepsilon^{\frac{5}{2}} u_{x,y}^{(3)} + \dots \\ u_z &= 0 + \varepsilon u_z^{(1)} + \varepsilon^2 u_z^{(2)} + \varepsilon^3 u_z^{(3)} + \dots \\ \phi &= 0 + \varepsilon \phi^{(1)} + \varepsilon^2 \phi^{(2)} + \varepsilon^3 \phi^{(3)} + \dots \end{aligned} \quad (5)$$

100 Now using the number density of electron fluid given by equation (4), stretching coordinates
 101 ξ and τ and the expansions (5) into (1)-(3). Comparing the coefficients of lowest order of ε
 102 i.e. $\varepsilon^{3/2}$, we get the linear dispersion relation which is given by the following expression.
 103
 104

$$105 \quad v_0^2 = \frac{l_z^2}{c_1} \left[1 + \frac{5}{3} \sigma c_1 \right] \quad (6)$$

106 where $c_1=(q+1)/2$ and the phase velocity depends upon the ion to electron temperature ratio
 107 σ , the strength of nonextensivity q and obliqueness of propagation γ . It may be noted that in
 108 the limit $\sigma \rightarrow 0$, our expression of phase velocity becomes exactly similar to that derived by
 109 Ferdousi et al [34] for $\mu_p=0$. Mathematical relation (6) shows that phase velocity increases
 110 with ion to electron temperature ratio σ and decreases with non-extensive parameter (q) for
 111 all ranges of q . The q -dependence of phase velocity comes from the factor c_1 in the
 112 expression (6). Similar kind of behavior has been observed by Ferdousi et al [34], Akhtar et
 113 al [27] and Sahoo et al [36] in their respective researches. To investigate the effect of ion
 114 temperature, figure 1 shows the typical variation of the phase velocity v_0 with respect to
 115 angle of propagation γ for three different values of $\sigma=T_i/T_e$. It is observed that wave phase
 116 velocity decreases with angle between the direction of the wave propagation vector k and
 117 the external magnetic field B_0 . The decrease of v_0 with γ also becomes clear from the
 118 expression (6) where $v_0 \propto \sqrt{\cos \gamma}$ and becomes zero for $\gamma = 90^\circ$. This decreasing trend of
 119 v_0 with γ is similar to that observed by Misra and Wang [37]. In order to investigate the
 120 electrostatic propagation, we consider small oblique angle. From the figure 1, it becomes
 121 clear that the phase velocity increases with increase in the temperature ratio σ . Hence ion
 122 temperature significantly effect the dynamics of given plasma system. Further, the wave
 123 phase velocity is found to be independent of the magnetic field strength and decreases with
 124 nonextensivity q (similar to the observations of Ferdousi et al [34]).
 125
 126



127
128 **Fig.1. Variation of wave phase velocity (v_0) with angle of propagation (γ) for three**
129 **values of ion temperature σ for $q= 0.5$.**

130
131 Going to the next higher order of ϵ i.e. ϵ^2 and by doing algebraic manipulations, we get the
132 following Korteweg-de Vries (KdV) equation (7) in which we have replaced $\phi^{(1)}$ with ϕ for
133 simplicity.

134
$$\frac{\partial \phi}{\partial \tau} + A \phi \frac{\partial \phi}{\partial \xi} + B \frac{\partial^3 \phi}{\partial \xi^3} = 0 \quad (7)$$

135 where A is non-linear and B is dispersion coefficients and are given as:

136
$$A = l_z \sqrt{c_1} \sqrt{1 + \frac{5}{3} \sigma c_1} \left[\frac{3}{2} - \left[\frac{5\sigma}{18} + \frac{c_2}{c_1^3} \right] \frac{c_1}{\left[1 + \frac{5}{3} \sigma c_1 \right]} \right] \quad (8)$$

137
$$B = \frac{1}{2} \frac{l_z}{c_1 \sqrt{c_1} \sqrt{1 + \frac{5}{3} \sigma c_1}} \left[1 + \left[\frac{1 - l_z^2}{\omega_0^2} \right] \left[1 + \frac{5}{3} \sigma c_1 \right]^2 \right] \quad (9)$$

138
139 where $c_2=(q+1)(3-q)/8$ and in the the limit $\sigma \rightarrow 0$, our expressions of nonlinear and dispersion
140 coefficients A and B become exactly similar to that derived by Ferdousi et al [34] for $\mu_p=0$
141 and $\mu_e=1$. Now, the stationary solitary wave solution of Eq. (7) is directly given by

142
143
$$\phi = \phi_0 \left[\sec h \left(\frac{\eta}{\delta} \right) \right]^2 \quad (10)$$

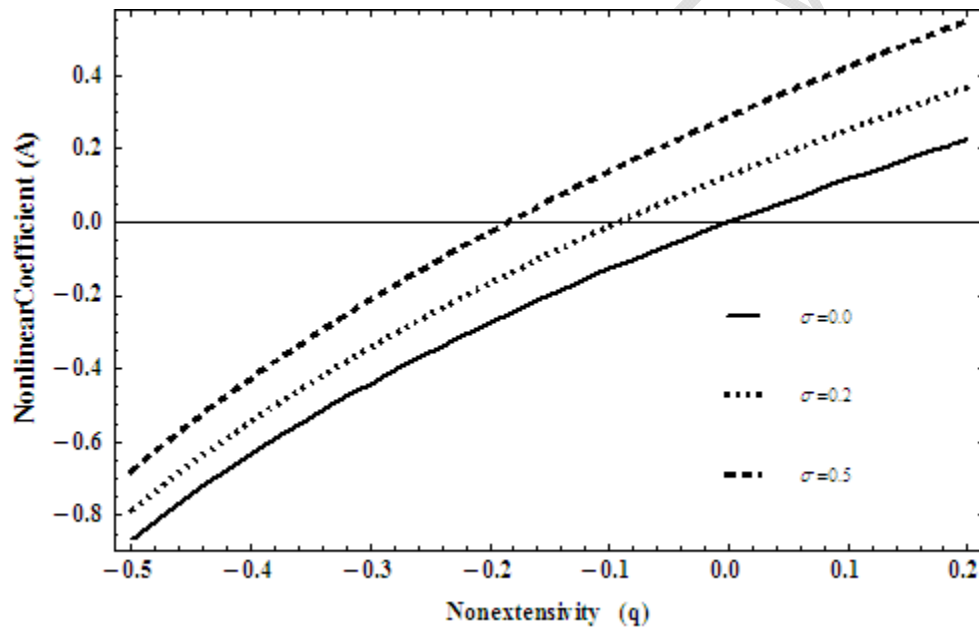
144

145 where the amplitude ϕ_0 and width δ of the soliton are given by $\phi_0 = 3u_0/A$ and $\delta = (4B/u_0)^{1/2}$
 146 and here $\eta = \xi - u_0\tau$. From the expressions of A and B (i.e. Eqns. (8) and (9)), it is found
 147 that the amplitude of the soliton depends on the ion and electron temperature ratio σ and
 148 independent of magnetic field. On the other hand, the width of the soliton depends on the
 149 strength of external magnetic field.

151 3. RESULTS AND DISCUSSION

152 In this paper, we have investigated the effects of ion temperature on the nonlinear wave
 153 propagation of small amplitude solitary waves in two component magnetized plasma. To
 154 describe the nonlinear propagation of the waves, we have derived a KdV equation (7) and
 155 obtained solitary wave solution (10). Depending upon the value of nonlinear coefficient A,
 156 the solitary wave might be associated with positive or negative potentials. Equation (8)
 157 indicates that A is dependent on parameters such as $q, \sigma, l_z = \cos(\gamma)$ which define the nature
 158 of solitary waves. We have concentrated our investigation to study the effect of ion
 159 temperature as much of other features are studied by Ferdousi et al [34].

160
 161

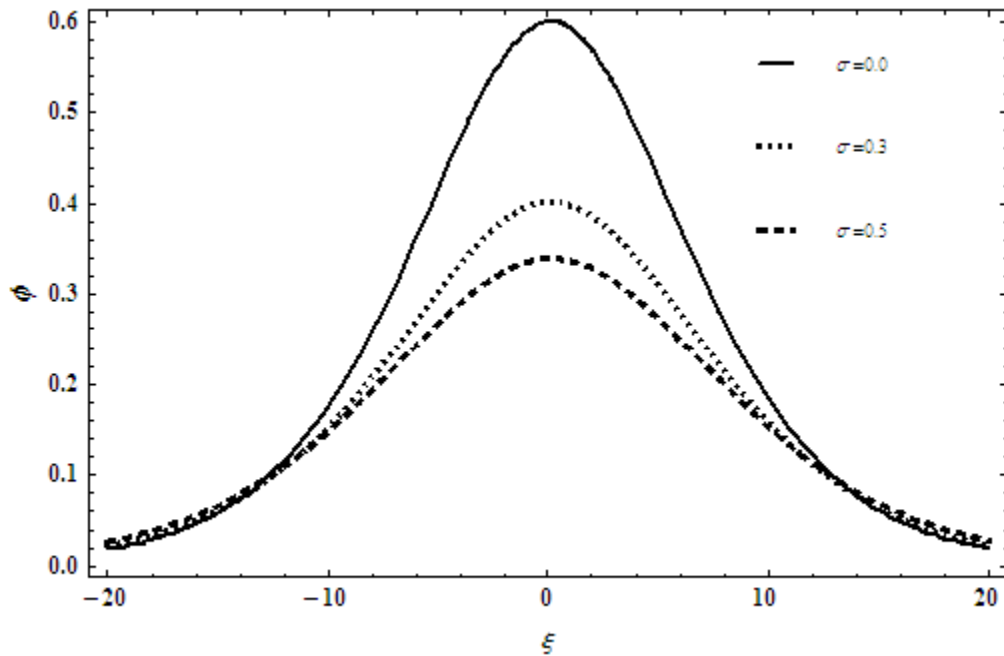


162
 163
 164
 165

Fig.2. For $\gamma = 30^\circ$, variation of nonlinear coefficient (A) as a function of nonextensivity q at three different values of ion temperature σ . Here solid line stands for $\sigma=0.0$, dotted line for $\sigma=0.2$ and dashed line is for $\sigma=0.5$.

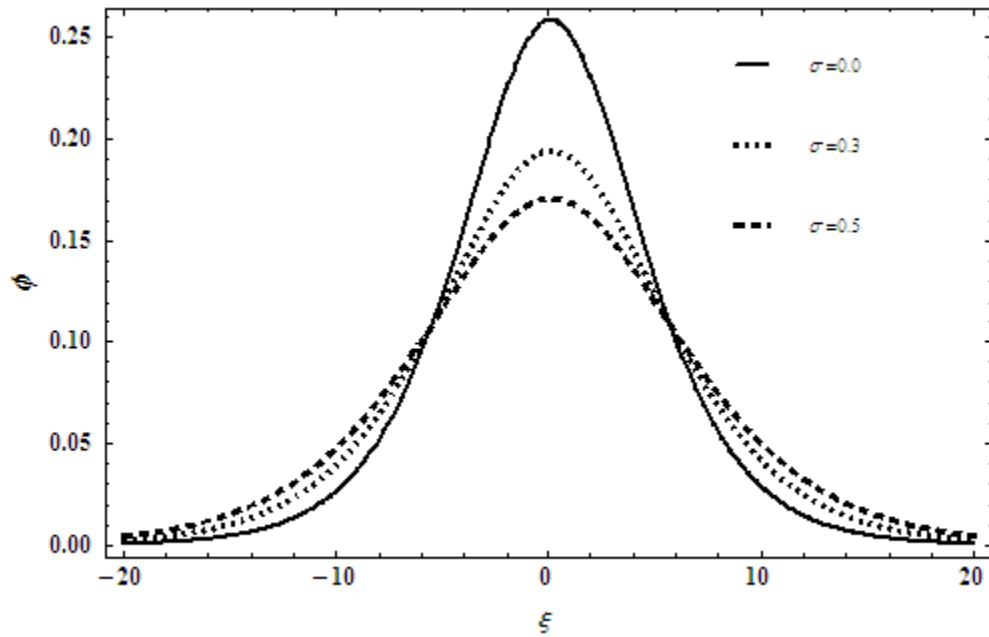
166 The nonlinear coefficient (A) as a function of nonextensivity (q) is displayed in Figure 2 for
 167 three different values of ion temperature σ . A transition from negative to positive potential
 168 structures results at a certain critical value of nonextensive parameter (q_c). We observe that
 169 at $q > q_c$, positive (hump shape or commonly known as compressive soliton) solitary waves
 170 exist, whereas at $q < q_c$, negative (dip shape or rarefactive solitons) solitary waves exist.
 171 Ferdousi et al [34] reported that the critical value q_c dependent on the parameters such as
 172 positron and electron density and electron-positron temperature ratio and independent of the
 173 obliqueness. In our case, the critical value of nonextensivity is also a function of ion
 174 temperature. It becomes obvious from figure 2, where a plot of nonlinear coefficient A as a

175 function of nonextensivity is displayed for three values of ion temperature. The critical value
176 of nonextensivity i.e. q_c decreases with increase in ion temperature.



177
178
179 **Fig. 3. For the range $0 < q < 1$, variation of soliton solution ϕ as a function of parameter ξ**
180 **at three different values of ion temperature i.e. $\sigma = 0.0$ (Solid Line), $\sigma = 0.3$ (Dotted Line)**
181 **and $\sigma = 0.5$ (Dashed Line) with other parameters as $\gamma = 30^\circ$, $\omega_0 = 0.40$ and $u_0 = 0.10$.**

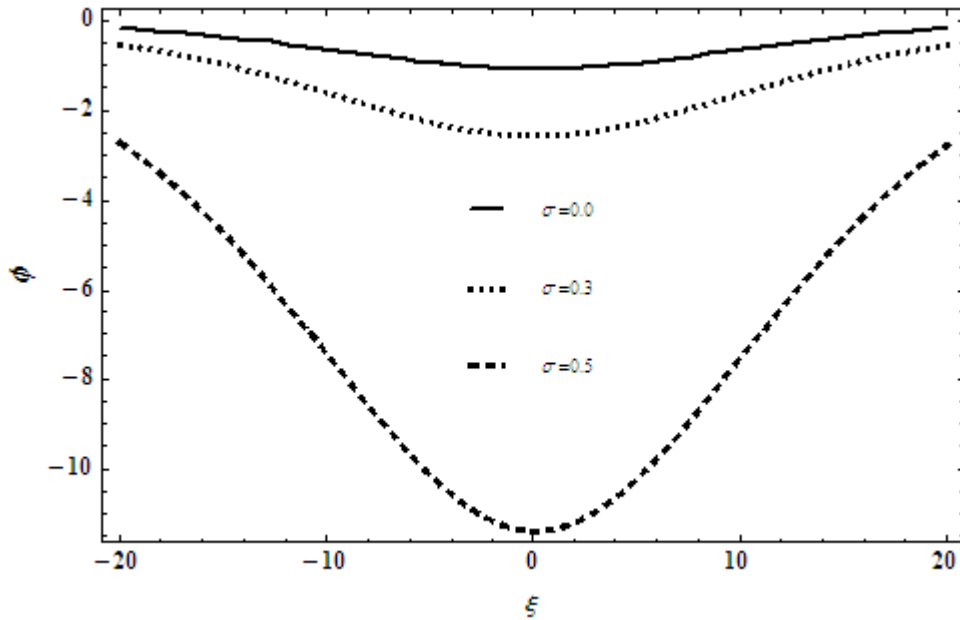
182
183



184

185
186
187
188
189

Fig. 4. For the range $q>1$, variation of soliton solution ϕ as a function of ξ for three different values of ion temperature i.e. $\sigma=0.0$ (Solid Line), $\sigma=0.3$ (Dotted Line) and $\sigma=0.5$ (Dashed Line) with other parameters as $\gamma = 30^\circ$, $\omega_0 = 0.40$ and $u_0 = 0.10$.

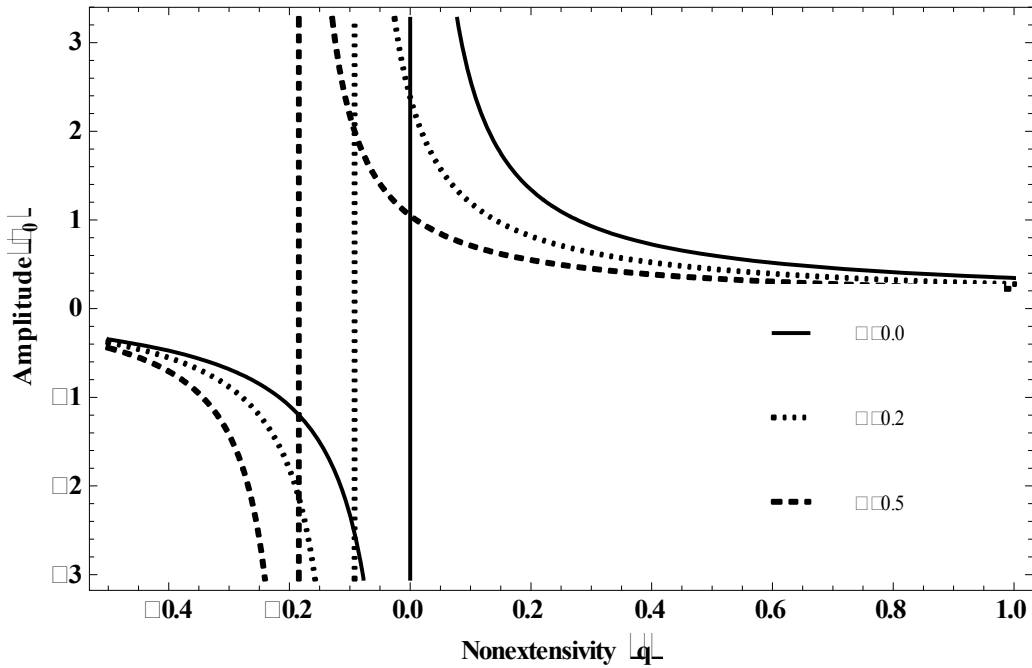


190
191
192
193
194
195
196

Fig. 5. For the range $-1<q<0$, variation of soliton solution ϕ as a function of ξ for three different values of ion temperature i.e. $\sigma=0.0$ (Solid Line), $\sigma=0.3$ (Dotted Line) and $\sigma=0.5$ (Dashed Line) with other parameters as $\gamma = 30^\circ$, $\omega_0 = 0.40$ and $u_0 = 0.10$.

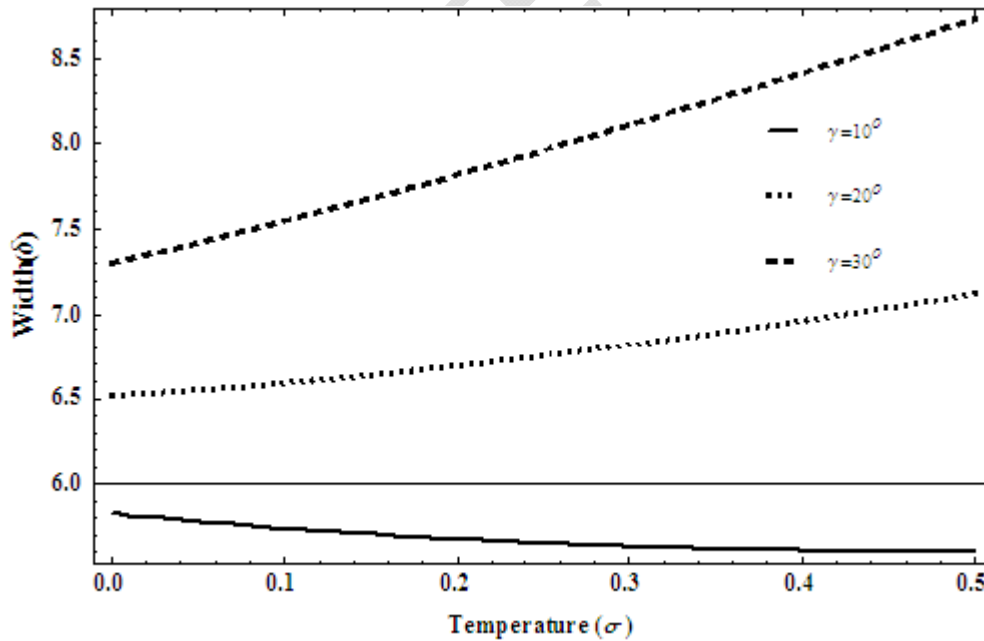
197
198
199
200
201
202
203
204
205
206
207
208
209
210
211

In order to investigate the effect of ion temperature σ on the solitary wave profiles for three different ranges of nonextensivity q viz. $0<q<1$, $q>1$ and $-1<q<0$, graphs have been displayed in Figures 3, 4 and 5 respectively. The values of other parameters taken for the analysis are as follows: obliqueness $\gamma = 30^\circ$, $\omega_0 = 0.40$ and $u_0 = 0.10$. Here the solid line corresponds to $\sigma=0.0$ i.e. cold ions, dotted and dashed lines correspond to $\sigma=0.2$ and $\sigma=0.5$ respectively. For the ranges $0<q<1$ and $q>1$, positive potential structures result as mentioned earlier. However, in the given parameter regimes, negative potential structures are observed for the range $-1<q<0$. It is observed that the peak amplitude of positive as well as negative potential structures decreases with increase in ion temperature. Hence the ion temperature plays a significant role here. Figure 6 presents a clearer picture of the dependence of ion temperature on the amplitude of solitary profiles. Here a plot of peak amplitude of solitary waves has been displayed as a function of nonextensivity q at three different values of ion temperature. Hence ion temperature is an important parameter in shaping the behavior of solitary structures.



212

213 **Fig. 6. Variation of soliton amplitude ϕ_0 as a function of q for three different values of**
 214 **$\sigma = 0.0$ (Solid Line), 0.2 (Dotted Line) and 0.5 (Dashed Line) with $\gamma = 30^\circ$, $\omega_0 = 0.40$ and**
 215 **$u_0 = 0.10$.**
 216



217

218 **Fig.7. Variation of soliton width δ as a function of σ for different values of $\gamma = 10^\circ$**
 219 **(Solid Line), 20° (Dotted Line) and 30° (Dashed Line) with $q = 0.5$, $\omega_0 = 0.5$ and $u_0 =$**
 220 **0.10 .**

221
222 Figure 7 represents soliton width δ as a function of ion temperature (σ) at three different
223 values of obliqueness with other parameters as $q = 0.5$, $\omega_0 = 0.5$ and $u_0 = 0.10$. This figure
224 clearly shows the impact of ion temperature on the width of the solitary structures. Here solid
225 line corresponds to $\gamma=10^\circ$, dotted line for $\gamma=20^\circ$ and dashed line for $\gamma=30^\circ$. A peculiar
226 behavior is observed at low and high value of obliqueness. It is found that for lower value of
227 obliqueness i.e. $\gamma=10^\circ$, the width of solitary structure decreases with ion temperature.
228 However. The trend becomes opposite on increasing the obliqueness as is clear from the
229 dotted ($\gamma=20^\circ$) and dashed ($\gamma=30^\circ$) curves. Width starts increasing with ion temperature for
230 higher values of obliqueness. Hence, introduction of finite ion temperature has significant
231 effect here. It is evident that higher magnitudes of σ cause significant reduction in the
232 amplitude of the solitary waves. But the soliton width increases with increase in ion
233 temperature σ , a result which is in agreement with Akhtar et al [27].

234

235 4. CONCLUSION

236 The properties of wave propagation of solitary waves are greatly modified by the
237 parameters like nonextensivity, strength of magnetic field, ion to electron temperature ratio
238 and obliqueness. In the limit of $\sigma \rightarrow 0$, all our results become similar to that obtained by
239 Ferdousi et. al [34]. However our main findings with special reference to ion temperature are
240 summarized below:

241 (i) Phase velocity of solitary wave increases with ion to electron temperature ratio.

242 (ii) The critical value of nonextensivity i.e. q_c decreases with increase in ion temperature.

243
244 (iii) The amplitudes of positive as well as negative potential structures decrease with ion
245 temperature.

246 (iv) Width decreases with σ for lower value of obliqueness, while it shows an increase with σ
247 at higher value of obliqueness.

248 The present investigation may be helpful in understanding the study of nonlinear
249 electrostatic waves propagating in astrophysical and laboratory plasmas.

250

251 Ethical: NA

252 Consent: NA

253

254 REFERENCES

255 1. Ikezawa S, Nakamura Y. Observation of Electron Plasma Waves in Plasma of Two-
256 Temperature Electrons. J Phys Soc Jpn. 1981;50: 962-67.

257 2. Dubouloz N, Pottellette R, Malingre M, Holmgren G, Lindqvist P A. Detailed analysis of
258 broadband electrostatic noise in the dayside auroral zone. J Geophys Res. 1991;96:3565.

259 3. Mozer F S, Ergun R, Temerin M, Cattell C, Dombeck J, Wygant J. New Features of Time
260 Domain Electric-Field Structures in the Auroral Acceleration Region. Phys Rev
261 Lett.1997;79:1281.

- 262 4. Stasiewicz K. Nonlinear Alfvén, magnetosonic, sound, and electron inertial waves in fluid
263 formalism. *J Geophys Res.* 2005;110:A03220.
- 264 5. Shinsuke I, Yukiharu O. Nonlinear Waves along the Magnetic Field in a Multi-Ion Species
265 Plasma. *J Plasma Fusion Res.* 2001;4: 500-504.
- 266 6. Dubinin E M, Sauer K, McKenzie J F, Chanteur G. Nonlinear waves and solitons
267 propagating perpendicular to the magnetic field in bi-ion plasma with finite plasma pressure.
268 *Nonlinear Process Geophys.*2002;9:87-99.
- 269 7. El-Taibany W F, Moslem W M. Higher-order nonlinearity of electron-acoustic solitary
270 waves with vortex-like electron distribution and electron beam. *Phys Plasmas.*
271 2005;12:032307.
- 272 8. Gill T S, Bala P, Kaur H, Saini N S, Bansal S. Ion Acoustic Solitons and Double Layers in
273 a multicomponent plasma consisting of positive and negative ions with nonthermal electrons.
274 *Eur Phys J D.* 2004;31:91.
- 275 9. Miller H R, Witta P J. *Active Galactic Nuclei.* Springer, Berlin, Germany; 1978.
- 276 10. Michel F C. Theory of pulsar magnetospheres. *Rev Mod Phys.*1982;54:1-66.
- 277 11. Singh S V, Devanandhan S, Lakhina G S, Bharuthram R. Effect of ion temperature on
278 ion-acoustic solitary waves in a magnetized plasma in presence of superthermal electrons.
279 *Phys Plasmas.* 2013;20: 012306.
- 280 12. Alinejad H, Mamun A A. Oblique propagation of electrostatic waves in a magnetized
281 electron-positron-ion plasma with superthermal electrons. *Phys Plasmas.* 2011;18:112103.
- 282 13. Mahmood S, Mushtaq A, Saleem H. Ion acoustic solitary wave in homogeneous
283 magnetized electron–positron–ion plasmas. *New J Phys.* 2003;5:28.1–28.10.
- 284 14. Jehan N, Salahuddin M, Saleem H, Mirza A M. Modulation instability of low-frequency
285 electrostatic ion waves in magnetized electron-positron-ion plasma. *Phys Plasmas.*
286 2008;15:092301.
- 287 15. Mio J, Ogino T, Minami K, Takeda S. Modulational instability and envelope solitons for
288 non-linear Alfvén waves propagating along the magnetic field in plasmas. *J Phys Soc Jpn.*
289 1976;41:667–73.
- 290 16. Dubouloz N, Treumann R A, Pottelette R, Malingre M. Turbulence generated by a gas of
291 electron acoustic solitons. *J Geophys Res.* 1993;98:17415–22.
- 292 17. Mace R L, Hellberg M A. The Korteweg–de Vries– Zakharov–Kuznetsov equation for
293 electron-acoustic waves. *Phys Plasmas.* 2001;8:2649.
- 294 18. Devanandhan S, Singh S V, Lakhina G S, Bharuthram R. Electron acoustic waves in a
295 magnetized plasma with kappa distributed ions. *Phys Plasmas.* 2012;19:082314.
- 296 19. Pakzad H R, Javidan K. Obliquely propagating electron acoustic solitons in magnetized
297 plasmas with nonextensive electrons. *Nonlin Process Geophys.* 2013;20:249-55.
- 298 20. Rényi A. On a new axiomatic theory of probability. *Acta Math Hung.* 1955;16:285-335.

- 299 21. Tsallis C. Possible generalization of Boltzmann-Gibbs statistics. J Stat Phys.
300 1988;52:479-87.
- 301 22. Plastino A R. Stellar polytropes and Tsallis' entropy. Phys Lett A. 1993;174:384-86.
- 302 23. Kaniadakis G, Lavagno A, Quarati P. Generalized Statistics and Solar Neutrinos. Phys
303 Lett B. 1996;369:308-12.
- 304 24. Lavagno A, Kaniadakis G, Rego-Monteiro M, Quarati P, Tsallis C. Non-extensive
305 thermostistical approach of the peculiar velocity function of galaxy clusters. Astrophys Lett
306 Commun. 1998;35: 449-55.
- 307 25. Rossignoli R, Canosa N. Non additive entropies and quantum statistics. Phys Lett A.
308 1999;281:148-53.
- 309 26. Abe S, Martinez S, Pennini F, Plastino A. Nonextensive thermodynamics relations. Phys
310 Lett A.2001;281:126-30.
- 311 27. Akhtar N, El Taibany W F, Mahmood S. Electrostatic double layers in arm negative ion
312 plasma with nonextensive electrons. Phys Lett A. 2013;377:1282-89.
- 313 28. Gill T S, Bala P, Kaur H. Electrostatic wave structures and their stability analysis in
314 nonextensive magnetized electron-positron-ion plasma. Astrophys Space Sci. 2015;357:63.
- 315 29. Reynolds A M, Veneziani M. Rotational dynamics of turbulence and Tsallis. Phys Lett A.
316 2004;327:9-14.
- 317 30. Sattin F. Non-Extensive Entropy from Incomplete Knowledge of Shannon Entropy. Phys
318 Scr. 2005;71:443-46.
- 319 31. Wada T. On the thermodynamic stability of Tsallis entropy. Phys Lett A. 2002;297:334-
320 37.
- 321 32. Wu J, Che H. Fluctuation in nonextensive reaction-diffusion systems. Phys Scr.
322 2007;75:722-25.
- 323 33. Tribeche M, Djebarni L, Amour R. Ion acoustic solitary waves in a plasma with a q-
324 nonextensive electron velocity distribution. Phys Plasmas. 2010;17:04211.
- 325 34. Ferdousi M, Sultana S, Mamun A A. Oblique propagation of ion-acoustic solitary waves
326 in a magnetized electron-positron-ion plasma. Phys. Plasmas 2015;22:032117.
- 327 35. Gardner C S, Morikawa G K. Similarity in the asymptotic behaviour of collision free
328 hydromagnetic waves and water waves. Courant Institute of Mathematical Sciences Rep.
329 NYO.1960;9082:1-30.
- 330 36. Sahoo H, Chandra S, Ghosh B. Dust Acoustic Solitary Waves in Magnetized Dusty
331 Plasma with Trapped Ions and q-Non-extensive Electrons. Afr Rev Phys. 2015;10:235-41.
- 332 37. Misra A P, Wang Y. Dust-acoustic solitary waves in magnetized dusty plasma with
333 nonthermal electrons and trapped ions. Afr Rev Phys. 2014;10:0032.
- 334

335
336
337

UNDER PEER REVIEW