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Original Research Article

Shallow Water Empirical Remote Sensing Bathymetry using the blue/green and red spectrum regions.

ABSTRACT:

7 An atmospherically corrected Sentinel-2 image and a 1/25000 scale nautical chart were used to 8 investigate the performance of the electromagnetic spectrum blue/green and red regions in 9 bathymetric data retrieval. The imaging optical empirical remote sensing bathymetry, using Stumpf 10 (2003) reflectance model was adopted in the investigation. In clean water depth (3.1-7.3) meters both 11 spectrum regions can be used to retrieve bathymetric data with an accuracy of \pm (082-1.10) m. The 12 optimum electromagnetic spectrum regions in this depth range were the blue/green spectrum range (0.457-0.523 μm) and the red range (0.773-0.793 μm). For depth range (2.1-15.5) m, the blue/green 13 14 spectrum region (0.457-0.523 µm) produced better results than those of the red region. The clean 15 water derived bathymetric data quality decreases with the increase of water depth in general and with the red spectrum region in particular. The blue/green spectrum region (0.457-0.523 μ m) 16 and the red spectrum region (0.773-0.793 µm) correlation coefficient values can be adopted 17 as a measure of the water turbidity, using the characteristic of the water depth strong 18 correlation in turbid water. 19

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Keywords: Electromagnetic spectrum, blue/green spectrum region, red spectrum region, correlationcoefficient, root mean square error, absolute mean error.

23 **1. Introduction.**

24 1.1 Bathymetry

Water depth determination is a requirement for many processes that are applied in different fields 25 and for different purposes, to name, but a few, navigational nautical charts, dredging operations, 26 27 under water topography mapping, benthic mapping (morphology and habitat) etc. Bathymetry was traditionally dominated by the expensive, inefficient process of depth profiling using 28 29 conventional depth measurement methods. Typical examples of these methods are the vesselbased graduated rods, plumb lines and echosounders. These conventional bathymetric methods 30 are characterized by the high cost, inefficiency and inapplicability in shallow waters due to 31 difficult navigation. However, the remote sensing methods represent a flexible, efficient and 32 33 cost- effective alternative to these conventional methods. A brief informative summary of these methods was given by Jay Gao 2009, (table 1) who stated that "Remote sensing of bathymetry 34 takes several forms each having its own determination depth, accuracy, strengths, limitations and 35 best application settings". 36

Method	System	Sensible	Accuracy	Affecting factors	Strengths	Limitations	Best use
Non-imaging	LiDAR	Up to 70 m	Up to 15 cm	Water clarity, bottom material, surface state, background light	Wide depth range; concurrent measurement not essential	Expensive Limited swath width	Diverse environments of a narrow range (eg, tens of km wide)
Imaging	Microwave (space-borne)	Shallow to deep	Low	Image resolution slicks, fronts, weather condition (eg, waves)	Over large areas Not subject to cloud cover	Not so accurate	Open oceanic waters
Imaging	Optical – analytical	Up to 30 m	High	Water quality, atmospheric conditions	Based on physical process Accurate	Complex as several input parameters required Concurrent sea truth essential	Turbid and shallow inland waters, estuarie and river channels
Imaging	Optical – empirical	Up to 30 m	Varying	Atmospheric calibration, water turbidity Bottom reflectance	Simple to implement Accurate at certain depth	Limited depth Accuracy lower at a larger depth Concurrent sea truth essential	Nearshore and coastal waters; open waters
Imaging	Video	Tidal height	High	Image resolution	Able to reveal minor bathymetric change	Restrictive area Bathymetry along profiles	Intertidal zone and estuaries

This investigation was limited to the imaging optical empirical form of remote sensing bathymetry. It was carried out using shallow water multi-spectral passive satellite sensor data.

41 1.2 Bathymetric models.

The ability of light to penetrate the water body provides a physical basis for modelling water depth from remote sensing spectral data (Zhongwei Deng et al., 2008).

As the incident solar radiation propagates through the water, it is increasingly scattered and absorbed by water and in-water constituents, leaving varied energy to be scattered and recorded in remote sensing imagery. The energy received at the sensor is inversely proportional to the depth of water after atmospheric and water column effects have been removed. Therefor, the intensity of the returned signal is indicative of the depth at which the solar radiation has penetrated (Jay Gao, 2009).

50 Different models were used for retrieving water depth using remote sensing spectral data. 51 Some are theoretical and based on the sophisticated transmission equation of the 52 electromagnetic radiation in water, others are empirical and are based on the calibration 53 between the image pixel values and their corresponding depth measured values. The semi-54 analytical methods integrate the empirical and theoretical methods using statistical regression.

The use of passive satellite sensor data in shallow waters is complicated by the combined atmospheric, water and bottom signals (William J. et al., 2008). Thus, the most optimum model for retrieving waer depth from remote sensing spectral data should consider, the attenuation

effects resulting from the atmosphere, water body and bottom topography. However, due to 58 59 the difficulties in modelling the water body and bottom topography parameters, most of the models consider the relationship between the water depth and the atmospherically corrected 60 amount of energy leaving the water body. Typical examples of such models were those 61 62 developed by Lyzenga (Lezenga, 1978) and Stumpf (Stumpf et al., 2003). The last model was 63 used in this investigation via SNAP software, Sentinel-2 toolbox. The Sentinel-2 Toolbox consists of a rich set of visualization, analysis and processing tools for the exploitation of MSI data from 64 65 the upcoming Sentinel-2 mission [4]. Similar to a variety of empirical bathymetry models, 66 Stumpf reflectance model relies on the assumption of exponential attenuation of light with depth and is based on the log transform of two bands and the derived depth z value is given by 67 (Stumpf at al., 2003): 68

69 $Z = m_1 (in (n * R_i)/in(n*R_j)) + m_0$ where,

n is a constant to ensure positive value after the log transform and a linear relationshipbetween the ratio and the depth.

- 72 R_i and R_j are atmospherically corrected reflectances in the two bands i and j.
- m_1 is a tunable constant to scale the ratio to depth and m_0 is an offset value when z equals zero.
- 75 1.3 Optimal bathymetric bands.

The selection of optimal electromagnetic spectrum for bathymetric modelling is important for obtaining reliable bathymetric results from the spectral remote sensing data.

Never-the less, the short wavelength algorithms advocated for bathymetric measurements in clear water can not be applied to turbid productive water. Turbid waters shift the optimum wavelength of sensing bathymetry towards longer radiation away from the vicinity of 0.45 µm that tends to have the maximum penetration in clear water (Siegal and Gillespie, 1980). In this environment water depth is strongly correlated with the red band of 0.746-0.759 µm range, but not the blue end of the spectrum (George, 1997), (Jay Gao, 2009).

Due to the lack of information related to water turbidity in the study area, both the blue and red ends of the electromagnetic spectrum will be used to retrieve bathymetric data to elaborate on the performances of the different portions of the spectrum in this specific spectrum range.

- 88 **2. Methodology.**
- 89 2.1 The study area.

The study area lies in the Gulf of Aden, Yemen, Aden Harbor and approaches. It is covered by the nautical chart sheet 7, published at Taunton U.K., July 1884, under the superintendence of Rear Admiral sir David K.E.C.B., Hydrographer of the Navy, Edition 26th August, 1999. Two test areas covered by this nautical chart were used in this investigation and the water depths

- ranged between 3.1 and 7.3 meters in the first area (area1) and between 2.1 to 15.5 meters in
- 95 the second area (area2) (Fig. 1).



Fig. 1, Part of the nautical chart showing, the study area, and the two test areas, bounded red.

97 2.2 Data sets.

The data sets used in this investigation included an atmospherically corrected 10 m resolution
Sentinel-2 satellite image, and a 1/25000 scale nautical chart (Fig 1).

Sentinel-2 is a wide-swath, high resolution multi-spectral imaging mission supporting, Copernicus land monitoring studies, including the monitoring of vegetation, soil and water cover as well as observation of inland waterways and coastal areas. The Sentinel-2 multispectral instrument (MSI) samples 13 spectral bands, four bands at 10 meters, six bands at 20 meters and three bands at 60 meters spatial resolution, table 2, [5]. The specifications of the Sentinel-2 image used in this investigation are presented in table 3.

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Band	Resolution	Central	Band	Band range (nm)	Purpose	
name	(m)	wavelength	width			
		(nm)	(nm)			
B01	60	443	20	433-453	Aerosol	
B02	10	490	65	457.5-522.5	Blue	
B03	10	560	35	577.5-667.5	Green	
B04	10	665	30	650-680	Red	
B05	20	705	15	697.5-712.5	Vegetation classification	
B06	20	740	15	732.5-747.5	Vegetation classification	
B07	20	783	20	773-793	Vegetation classification	
B08	10	842	115	784.5-899.5	Near infrared	
B08A	20	865	20	855-875	Vegetation classification	
B09	60	945	20	935-955	Ware vapor	
B10	60	1375	30	1360-1390	Cirrus	
B11	20	1610	90	161565-1655	Snow/ice/cloud	
					discrimination	
B12	20	2190	180	2100-2280	Snow/ice/cloud	
					discrimination	

111 Table 2. Sentinel-2 bands wavelength and spatial resolution.

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113 Table 3, Sentinel-2 image meta data (Copernicus Open Access Hub).

Date: 2018-12-19T07:23:19.024Z Filename: S2B_MSIL2A_20181219T072319_N0211_R006_T38PMV_20181219T100100.SAFE Identifier: S2B_MSIL2A_20181219T072319_N0211_R006_T38PMV_20181219T100100

Instrument: MSI	Dark features percentage:	Degraded ancillary data						
Satellite: Sentinel-2	2.052944	percentage: 0.0						
Aot retrieval accuracy: 0.0	Cloud shadow percentage:	Degraded MSI data						
Cloud cover percentage: 6.119724	0.238857	percentage: 0						
JTS footprint: POLYGON ((44.077333957933234 13.037282661543257,44.08545881814128								
13.072948458972885,44.120819107714496 13.220716873321877,44.153547744704206								
13.369309127002692,44.18550686304525 13.51813639364872,44.19643473607472								
13.566941289209904,45.09021225129309 13.568434978835024,45.089852282995246								
12.57555163480923,44.07905548219917 12.573983802224875,44.077333957933234								
13.037282661543257))								
Format: SAFE	General quality: PASSED	High proba clouds						
Format correctness: PASSED	Generation time: 2018-12-	percentage: 2.745525						
Geometric quality: PASSED	19T10:01:00.000000Z	Ingestion Date: 2018-12-						
		19T13:18:31.739Z						
Medium proba clouds percentage:	No data pixel percentage:	Pass direction:						

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1.872717	3.232	DESCENDING	
Mission datatake id:	Not vegetated percentage:	Processing baseline: 02.11	
GS2B_20181219T072319_009327_N02.11	65.298164	Processing level: Level-2A	
	Orbit number (start): 9327		
Product type: S2MSI2A	Sensing start: 2018-12-	Sensor quality: PASSED	
Radiometric quality: PASSED	19T07:23:19.024Z	Snow ice percentage: 0.0	
Relative orbit (start): 6	Sensing stop: 2018-12-	Thin cirrus percentage:	
Saturated defective pixel percentage: 0.0	19T07:23:19.024Z	1.501483	
Sensor quality: PASSED	Vegetation percentage:		
Snow ice percentage: 0.0	0.234787	Water vapour retrieval	
Thin cirrus percentage: 1.501483	Water percentage:	accuracy: 0.0	
Unclassified percentage: 9.865181	16.190347		

3. Water depth retrieval and formation of bathymetric band.

116 3.1 Formation of bathymetric bands.

The blue/green spectrum region provides the higher water penetration for improved 117 118 bathymetry retrieval (William J. et at., 2016). Spectral bands of short wavelengths are preferred in bathymetric mapping from space as there is low attenuation from electromagnetic radiation 119 120 (Jay Gao, 2009). As quoted in section 3, both the blue/green and red regions of the electromagnetic spectrum can be used for water depth retrieval and the decision as to which 121 122 region to use depends on the water turbidity. The main problem here is the lack of information 123 related to water turbidity in the large water areas covered by the satellite multi-spectral imagery. This paper considered the use of both regions to derive a shallow water bathymetric 124 125 layer, adopting the reflectance ratio model developed by Stumpf et at., 2003. This would facilitate an insight elaboration in the performance of the different portions of the 126 127 electromagnetic spectrum in these regions. The spectrum portions used are based on Sentinel-2 bands wavelengths and spatial resolutions (table 2). A total of nine reflectance ratio models 128 was formed, one blue/green model, four blue/red models and four green/red models. The 129 bathymetric layer of test area 1, was derived using these nine models, the Sentinel-2 130 atmospherically corrected image and a total of 16 calibration points extracted from the 131 132 1/25,000 scale nautical chart of the area. A typical example of the blue/red models derived bathymetric bands, is presented in Fig.2. 133





Figure 2, A typical example of an imagery derived bathymetric band of the blue/red spectrum region models, the satellite image (upper) and the water mask (middle).

135 3.2 Quality assessment of derived bathymetric data.

The quality assessment of the derived bathymetric data was based on the calibration points extracted from the 1/25,000 nautical chart of the study area. It was carried out by comparing the calibration points derived and nautical chart extracted corresponding data values, using simple statistical models. The statistical models adopted in this investigation are, the root mean square error (RMSE), correlation coefficient (r), mean absolute error (MAE) and maximum error (ME) (equations 1,2 and 3) below:

142
$$RMSE = \sum_{i=0}^{n} (x_i - y_i)^2 /n$$
 (1)

143 MAE =
$$\sum_{l=1}^{n} abs(x_{i-y_l})/n$$
 (2)

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$$r = \sum_{i=1}^{n} (x_{i-x_0}) * (y_{i-y_0}) / Sqrt \sum_{i=1}^{n} (x_{i-x_0})^2 * (y_{i-y_0})^2$$
 (3)

145 x_i is the calibration point derived depth value.

- 146 y_i is the calibration point nautical chart depth value.
- 147 x_0 is the mean of the derived depth values.
- 148 y_0 is the mean of the nautical chart values.
- 149 **4. Results.**
- 150 4.1 Test area1 results.

151 The results obtained for test area 1, are presented in table 4, which shows, the Model Number

152 (MN), reflectance ratio bands, Root Mean Square Error (RMSE), correlation coefficient (r) and 153 maximum error value (ME).

MN	Ratio	RMSE (m)	AME(m)	r	ME (m)	Remarks
	bands					
1	B2-B3	1.10	0.77	0.68	2.38	Blue/Green
2	B2-B4	0.93	0.97	0.19	2.83	Blue/Red
3	B2-B5	0.80	0.92	0.20	2.56	Blue/Red
4	B2-B6	0.85	0.88	0.23	2.74	Blue/Red
5	B2-B7	0.82	0.85	0.27	2.64	Blue/Red
6	B3-B4	0.83	0.88	-0.07	2.76	Green/Red
7	B3-B5	0.86	0.79	0.56	1.92	Green/Red
8	B3-B6	0.90	0.79	0.50	2.38	Green/Red
9	B3-B7	0.86	0.78	0.50	2.36	Green/Red

154 Table 4, The results obtained for test area1, applying the nine models.

155

156 The statistical results for test area1, table 3, showed that the RMSE values vary from 0.82 to 1.1 157 meters, with the maximum value associated with the blue/green model 1, while the AME values vary from 0.77 to 0.97 meters, with the minimum value associated with the same model. 158 The high correlation value was delivered by the blue/green region, model1 (0.68) and may 159 suggest that the water was not turbid (Siegal and Gillespie, 1980). Although all the red region 160 161 models delivered similar performances with respect to the RMSE and MAE statistical parameters, but the correlation coefficient and maximum error values demonstrated bad 162 performances for the blue/green model 2 and the green/red model 6. The red spectrum region 163 green/red models 5,6 and 7, delivered the best performances with resect to all the statistical 164 measures. This clearly revealed that the best performance of the two tested spectrum regions 165 166 was recorded by the red electromagnetic spectrum portion (0.6975-0.793 µm). This almost 167 agreed with the red band wavelength width given by George, 1997, (0.746-0.759 μm). Though the red region models performed better than the blue/green region model, these results 168 demonstrated that both the regions can be used for depth retrieval in the applied depth range 169 170 (3.1-7.3 meters), as the difference between the red region models average RMSE value and the blue/green region value is only 24 cm (1.1-.86 m). The green/blue model1 performed better 171

than all the red region models with respect to the correlation coefficient and absolute mean

error values (0.68, 0.77 m). Also, this model delivered a low maximum error value compared to

the red region models (2.38 m), with an exception of the green/red model 7, which delivered a

value better than the blue/green model1 (1.92 m).

176 The results for test area1 demonstrated the performances of the blue/green and red spectrum

regions in a depth range of 3.1 to 7.3 meters. In order to elaborate more in the performances of

these two spectrum regions the same nine models were applied in test area2 with a depth

- 179 range of 2.1 to 15.5 meters.
- 180 4.2 Test area2 results.
- 181 The results obtained for test aarea2 are presented in table 5,

MN	Ratio	RMSE	AME	r	Maximum	Remarks
	bands	(m)	(m)		error	
1	B2-B3	1.74	1.43	0.79	3.51	Blue/Green
2	B2-B4	1.77	1.42	0.53	5.06	Blue/Red
3	B2-B5	1.90	1.42	0.59	4.45	BLUE/Red
4	B2-B6	1.78	1.47	0.50	5.79	Blue/Red
5	B2-B7	1.86	1.45	0.52	4.87	Blue/Red
6	B3-B4	1.83	1.33	0.66	3.90	Green/Red
7	B3-B5	1.93	1.27	0.68	4.11	Green/Red
8	B3-B6	1.80	1.42	0.59	5.18	Green/Red
9	B3-B7	1.88	1.36	0.60	4.24	Green/Red

182 Table 5, The results obtained for test area 2, applying the nine models,

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184 The statistical results in table 4, showed RMSE, correlation coefficient, and mean absolute error values ranging from 1.74 to 1.93 m, 0.5 to 0.79 and 1.27 to 1.47 m respectively. These results 185 indicated that the best performance was delivered by the blue/green region model1, which 186 records the best values for all statistical measures in general and the maximum error value in 187 particular (3.51 m). This value in fact credited the blue/green model, compared to all the red 188 region models' values, which ranged between 3.90 and 5.79 meters. The blue/green region 189 maximum correlation value (0.79) suggested that the water was not turbid at the moment of 190 Sentinel-2 image recording, otherwise the water depth would be strongly correlated with the red 191 region models (Siegal and Gillespie, 1980). The red region models delivered good performances 192 with respect to the statistical parameters, but recorded large maximum error values that ranged 193 between 3.90 to 5.79 meters. Compared to area 1, maximum error values 91.92-2.38) recorded in 194 table 3, these values demonstrated the increase of the maximum error values with the depth 195 increase. 196

197 **5. Visible light water penetration.**

Light water penetration decreases with the decrease of the light energy. The amount of light energy depends on the band wavelength and the shorter the wave the higher the energy. Different visible light wavelengths penetrate to different depths depending on water condition, wave energy and absorptivity. Most of the visible light spectrum is absorbed within 10 meters (33 feet) of the water's surface, and almost none penetrates below 150 meters (490 feet) of water depth, even when the water is very clear [1]. This demonstrated that all the visible light bands are approximately equally absorbed up to the depth of 10 meters.

205 The long wavelengths of the light spectrum-red, yellow, and orange-can penetrate to approximately 15, 30, and 50 meters (49, 98, and 164 feet), respectively, while the short 206 wavelengths of the light spectrum—violet, blue and green—can penetrate further, to the lower 207 limits of the euphotic zone[1]. This is clearly, demonstrated in Fig. 3 [3] which revealed the 208 water depth penetrations for the visible light spectrum in clean ocean water and turbid coastal 209 water. The penetration depths of the blue, green and red bands waves in turbid coastal water are 210 approximately, 30, 55 and 25 meters respectively, but can reach up to 205, 105 and 50 meters 211 respectively in clean ocean water. The depths tested in the investigation ranged between 2.1 and 212 15.5 meters and the tested regions (blue/green and red) can penetrate these depths with almost 213 equal absorption attenuation up to 10 meters [1]. Therefore, the tested regions have no energy 214 and absorptivity constraints up to the maximum tested depth (15.5). The water turbidity effect 215 depends on the presence of solid particles in the water column and the tested spectrum regions 216 are affected differently, due to light scattering and absorption characteristics. The turbidity 217 218 attenuation would increase with the depth but the amount of energy would decrease. The energy received at the sensor can be modelled to retrieve the water depth if the atmospheric, water 219 column and bottom topography effects are removed. The multi-spectral data used in this 220 investigation was atmospherically corrected, the bottom topography noise was reduced applying 221 filtering operations and the water column effect was considered by the adopted bathymetric 222 model parameters m_0 and m_1 . 223



Fig. 4, The penetration depth of the visible light spectrum in clear oceanic waters compared with turbid coastal waters. Adapted with permission. [103] Copyright 2016, NOAA Ocean Explorer [3].

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6. Discussions.

The results obtained for the two test areas, (area1 and area2) demonstrated strong depth 230 correlation with the blue/green region (0.68, 0.79). For test areal (table 3), weak depth 231 correlation (0.19-0.27) and large maximum error values (2.64-2.83) were associated with the red 232 spectrum region models blue/red models 2, 3, 4 and 5 and green/red model 6. The green/red 233 models 7, 8 and 9 delivered good correlation coefficient values (0.5-0.56) and maximum error 234 values (192-2.38). The green/red model 6 was the only model recorded a negative correlation 235 236 coefficient value (-0.07) but associated with good absolute mean error value (0.88). Though the best performance for test areal was recorded by the blue/green modell, but the green/red 237 models 7, 8 and 9 delivered an acceptable performance. This revealed that both the blue/green 238 spectrum region (0.457-0.523 μ) and red spectrum region (0.698-0.793 μ m) can be used to 239 retrieve bathymetric data for clean water depth range of 3.1-7.3 meters. 240

For test area2, the best performance with respect to all the statistical parameters was obtained by the blue/green region model1 (1.74, 1.43, 0.79 and 3.51). The red region model's performance was good with an exception of the maximum error values (3.90-5.79). These results clearly,

demonstrated that, for depth range (2.1-15.5) meters, the blue/green spectrum region is better 244 245 than the red region with respect to all the statistical parameters in general and the maximum error 246 value in particular. Thus, for clean water depth range (3.1-7.3) m both regions can be used to retrieve bathymetric data, but for depth range (2.1-15.5) meters, the blue/green spectrum region 247 is preferred. The strong correlation of depth with the blue/green spectrum region suggested that 248 249 the water turbidity was not enough to shift the depth correlation from the blue/green region to the red region. The blue/green spectrum region (0.457-0.523 µm) and the red spectrum region 250 (0.773-0.793 µm) correlation coefficient values can be adopted as a measure of the water 251 turbidity. 252

7. Conclusions.

254 In clean water depth range (3.1-7.3) meters, both the blue/green region $(0.457-0.523 \mu m)$ and the red region (0.773-0.793 µm) can be used for bathymetric data retrieval, using the empirical 255 256 form of remote sensing bathymetry. The best log ration division band for both regions is band 3 (0.578-0.668 µm). For water depth (2.1-15.5) meters, the blue/green spectrum region (0.457-257 0.523 µm) was the optimum. The effort made in the investigation revealed that the blue/green 258 spectrum region (0.457-0.523 µm) and the red spectrum region (0.773-0.793 µm) correlation 259 coefficient values can be adopted as a measure of the water turbidity, using the characteristic of 260 the water depth strong correlation in turbid water. 261

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