

1 **DEPLETION ANALYSIS OF THE NIGERIAN RESEARCH REACTOR FUEL WITH**
2 **19.75% ENRICHED UO₂ MATERIAL**

3

4 **ABSTRACT**

5 The depletion analysis of the Nigerian research reactor fuel with 19.75% enriched UO₂ have
6 been performed using the VENTURE PC code. The matrix exponential method was selected
7 in this work to perform the depletion analysis. The volume fraction of the materials in this
8 mixture was calculated and multiplied by their respective atom densities to obtain the
9 effective atom density of the nuclide in the water, Al mix region of the fuel cell model. The
10 plot of the variation of k infinity versus hydrogen to Uranium ratio was generated using
11 Matlab programming language for processing of the computer code result. This shows that as
12 the ratio of hydrogen to uranium in the core of the reactor is increased, the reactivity also
13 increases by gradually increasing the fuel cell radii till it gets to the peak of 0.6193. Any
14 further increment in the radius of the fuel cell radii, the reactivity of the reactor decreases as
15 the hydrogen to uranium ratio increases.

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17 Key words: Depletion, reactor, uranium, reactivity.

18

19 **INTRODUCTION**

20 It has been more than three decade since the first nuclear reactor achieved a critical fission
21 chain reaction. Since that time, an extensive worldwide effort has been directed towards
22 nuclear reactor research and development in an attempt to harness the enormous vigour

23 contained within the atomic nucleus for peaceful application. Nuclear reactors have evolved
24 from an embryonic research tool into the mammoth electrical generating building block that
25 drive century of central-station power industrial plant around the world today. [1]

26 The current shortage of fissile fuels has made it quite obvious that nuclear fission reactor will
27 play a dominant role in meeting man's energy requirements for many years to come. The
28 dominant function played via nuclear fission reactors in the generation of electricity can be
29 predicted to proceed well into the next century. Nuclear energy will signify the solely doable
30 choice to fissile-fueled plant for most nations.

31 Fuel depletion analysis has to do with the prediction of the long-term changes in reactor fuel
32 composition caused by exposure to neutron flux during reactor operation. Such changes have
33 a vital bearing on the operating life of a reactor, as well as on its balance and control
34 The shift in the core power distribution that accompanies fuel burnup does not result in the
35 exceeding of core thermal limitations. Sufficient extra reactivity ought to be supplied in the
36 fresh core loading to acquire the desired fuel exposure which is consistent with safety
37 limitations.

38 Analysis of core composition is a necessity in order to optimize fuel exposure to achieve
39 minimal power costs as well as determine the cost of discharged fuel, since the fuel cost over
40 the operating lifetime of the reactor can exceed those of the capital cost of the plant itself.

41 Uranium dioxide (UO₂), a ceramic fuel is at present the most in many instances used nuclear
42 fuel for both research and power reactors. Uranium dioxide material is the fuel of preference
43 for most reactors due to its excessive melting point (2800°C), excessive neutron utilization,
44 first-rate irradiation stability, exceptional corrosion resistance in conventional coolants,

45 precise fission product retention, no segment change up to the melting point, compatibility
46 with cladding (Zircaloy and stainless steel), ease of fabrication, and excessive unique power
47 and energy per unit size of fuel pin. [2]

48 During reactor operation, the fuel material in the core of the system deplete with time due to
49 consumption for fission/absorption reaction inside the reactor system. For the existing Nigeria
50 Research Reactor-1 (NIRR-1), burnup calculations can be used to predict long- term changes
51 in the isotopic composition of its fuel material, brought about by exposure to neutrons of
52 different flux level, leading to fuel irradiation in the core of the system in the course of reactor
53 operation

54 The existing NIRR-1 system is fueled with UAl4-Al enriched to 90.2% U235 and the end
55 result from a range of depletion calculations has proven that the system can be operated with a
56 burnup of less than 1% for a length of 10 years [3]. It is designed on the whole to serve as a
57 neutron source. The core is a cylindrical fuel assembly, approximately containing 347 fuel
58 elements [4]

59 The fuel element is 248 mm in size with the active size being 230 mm. The diameter of the
60 fuel “meat” is 4.3 mm and the U235 loading in every fuel element is about 2.88 grams [5].

61 The current Highly Enriched Uranium (HEU) Nigeria Research Reactor-1 (NIRR-1) has a
62 tank-in-pool structural configuration and a nominal thermal power rating of 31.1 kW [1]. The
63 current core of the reactor is a 230 x 230 mm square cylinder and fueled by using U-Al4
64 enriched to 90.2%. [6]. The computer code selected to perform these depletion/burnup
65 calculations for the current NIRR-1 core is the VENTURE PC [7]

66 In this work, Depletion analysis was performed in order to determine variation of k infinity
67 versus hydrogen to Uranium ratio of the designed reactor system when fueled with the
68 proposed UO_2 material enriched to 19.75% U^{235}

69

70 **MATERIALS AND METHOD**

71 The NIRR-1 contains 347 fuel elements and is arranged in ten concentric circles. Between
72 these fuel pins are radial pitch which varies from one concentric circle to the other.

73 The NIRR-1 also consist of 4 tie rods and 3 dummy pin. The variation in the radial pitch
74 between the fuel pins as well as the tie rods and dummy pins in the core was a problem during
75 the selection of a single pin from any circle to calculate the volume of the moderator per pin
76 in order to develop the fuel cell model.

77 Supposing there are no dummy pin or tie rods in the core of the reactor, then we calculate the
78 entire volume of the core per pin using the 347 fuel pins. The volume of water region in the
79 fuel cell is a mixture of both the volume of moderator, tie rods and dummy pins.

80 The VENTURE module and the BURNER code module are two modules of VENTURE PC
81 code system that are used to perform depletion analysis of the NIRR-1 core.

82 While the venture module performs the neutronic part of the calculation, the burner code
83 module performs the depletion calculation.

84 The active material in the reactor fuel pin has a diameter of about 4.3mm and 230mm long. It
85 is surrounded with aluminum alloy of about 0.6mm thick called the fuel clad .

86 The matrix exponential method which has been selected in this work to perform the depletion
 87 analysis is one of the several methods that can be used by burner code to solve burnup
 88 equation. This matrix exponential method result from the need to expand exponential in the
 89 first order differential equation solution associated with burnup as recommended in
 90 VENTURE Manual, 2002 [8]

91 The volume fraction of the materials in this mixture was calculated and multiplied by their
 92 respective atom densities to obtain the effective atom density of the nuclide in the water, Al
 93 mix region of the fuel cell model.

94 *Total vol. of fuel region in the core = vol. of core – guide tube vol* (1)

95 $\pi r^2 - \pi r^2 = \pi(11.55)^2 - \pi(0.6)^2 = 418.1336\text{cm}^2$

96 $\text{total vol of core per fuel pin} = \frac{418.1336}{347} = 1.2050\text{cm}^2$

97 $\text{Thus, fuel cell outer radii} = \sqrt{\frac{\text{total vol of core per fuel pin}}{\pi}}$

98 $= \sqrt{\frac{1.2050\text{cm}^2}{\pi}}$

99 $= 0.6193\text{cm}$

100

101 The total number of Hydrogen atoms in each of the eleven cases was computed; firstly the
 102 moderator volume associated with each of the fuel cell outer radius was calculated by
 103 subtracting the fuel plus clad volume from the fuel cell volume.

104 The value of the moderator volume was multiplied by the hydrogen region atom density to
 105 obtain the total number of hydrogen atoms in each of the eleven cases.

106 The total number of uranium atoms in the fuel cell was also obtained by first determining the
107 volume of the active fuel in each of the fuel radii.

108 The uranium in the HEU fuel is enriched to 19.75% with each fuel pin containing 2.88g of
109 U235. The height and diameter of the active fuel materials are 23.0cm and 0.43cm respective.

110 Since the mass density, ρ , of a material is known, then the material atom density, N , can be
111 calculated using equation 2

$$112 \quad N = \frac{(\rho g/cm^3)(N_A atoms/gmole)}{Mg/gmole} \quad (2)$$

113 Since there are several isotopes present with known abundances we have:

$$114 \quad N_i = \frac{Y_i \rho N_A}{M} \quad (3)$$

115 The chemical composition of a mixture of element in terms of weight
116 percent is expressed as:

$$117 \quad N_i = \frac{\rho_i N_A}{M_i} = \frac{W_i \rho N_A}{M_i} \quad (4)$$

118 The molecular weight of the mixture was calculated in order to perform
119 density computations

120 For any components given in fraction, equation 5 applies.

$$121 \quad \therefore \frac{1}{M} = \sum \frac{W_i}{M_i} \quad (5)$$

122 The density of Uranium dioxide (UO_2) is $10.6g/cm^3$ and the weight percent of U235 is
123 19.75%

124 The molecular weight of U and UO_2 was determined by

$$125 \quad \frac{1}{M_u} = \sum \frac{W_i}{M_i} \quad (6)$$

126 The Uranium atom density was calculated by summing the atom density of U235 and U238 as
127 shown in the equation below

$$128 \quad N_u = N_{u235} + N_{u238} \quad (7)$$

129 The total number of Uranium atoms in the fuel cell is then calculated by multiplying the
130 volume of the active fuel by the Uranium atom density as shown in equation 8

$$131 \quad U - atom = N_u \times volume \ of \ active \ fuel \quad (8)$$

132 The homogenized atom density for U235, U238 and O were calculated by simply multiplying
133 the region atom density by the region volume fraction.

134 The volume fraction was calculated first by calculating the volume of each zones in the
135 system and then divide each value by the total volume of the equivalent fuel cell.

136

137 **RESULT AND DISCUSSION**

138 The calculation was performed using the highly sophisticated code VENTURE PC. The plot
139 of the variation of k infinity versus hydrogen to Uranium ratio was generated using Matlab
140 programming language for processing of the computer code result.

141 The value of the total number of hydrogen atom in each fuel cell radius is given in the table
142 below.

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148 Table 1.0

S/No	Fuel cell radii (cm)	Moderator volume (cm^2)	Hydrogen region atom density. (atom/b-cm)	H-atom (Atom/b- cm^2)
1.	0.298	0.9526	6.640e-2	6.3253e-2
2.	0.306	1.3018		8.6440e-2
3.	0.324	2.1216		14.0874e-2
4.	0.357	3.7460		24.8734e-2
5.	0.408	6.5663		43.6002e-2
6.	0.459	9.7625		64.8230e-2
7.	0.510	13.3348		88.5431e-2
8.	0.561	17.2831		114.7598e-2
9.	0.6192	22.2483		147.7287e-2
10.	0.714	31.3843		208.3918e-2
11.	0.816	42.6652		283.2969e-2

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150 Table 1.1: Table for Uranium atom density

S/No.	Fuel cell radii (cm)	Volume of fuel cell (cm^2)	Uranium region atom density. (atom/b-cm)	U- Atoms (atom/b- cm^2)
1.	0.298	6.4193	2.36267e-2	7.8946e-2
2.	0.306	6.7685		
3.	0.324	7.5883		

4.	0.357	9.2127		
5.	0.408	12.0330		
6.	0.459	15.2292		
7.	0.510	18.8015		
8.	0.561	22.7498		
9.	0.6192	27.7150		
10.	0.714	36.8510		
11.	0.816	48.1319		

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153 Table 1.2: Table for the average homogenized atom density for the fuel cell

Metal name	f_i	Nuclides	N_{ij}	$N_{ij}f_i$	N_{iz}
Fuel	0.0694	U235	4.727e-3	3.2803e-4	3.2803e-4
		U238	1.896e-2	1.3117e-4	1.3117e-4
Clad	0.0442	Zr-40090	2.165e-2	9.5693e-4	1.8599e-5
		Zr-40091	4.721e-3	2.0867e-4	
		Zr-40092	7.217e-3	3.1899e-4	
		Zr-40094	7.314e-3	3.2328e-4	
		Zr-40096	1.178e-3	5.2068e-5	
Moderator	0.8864	H1	6.640e-2	5.8857e-2	5.8857e-2
		O16	3.320e-2	2.9428e-2	4.1998e-2

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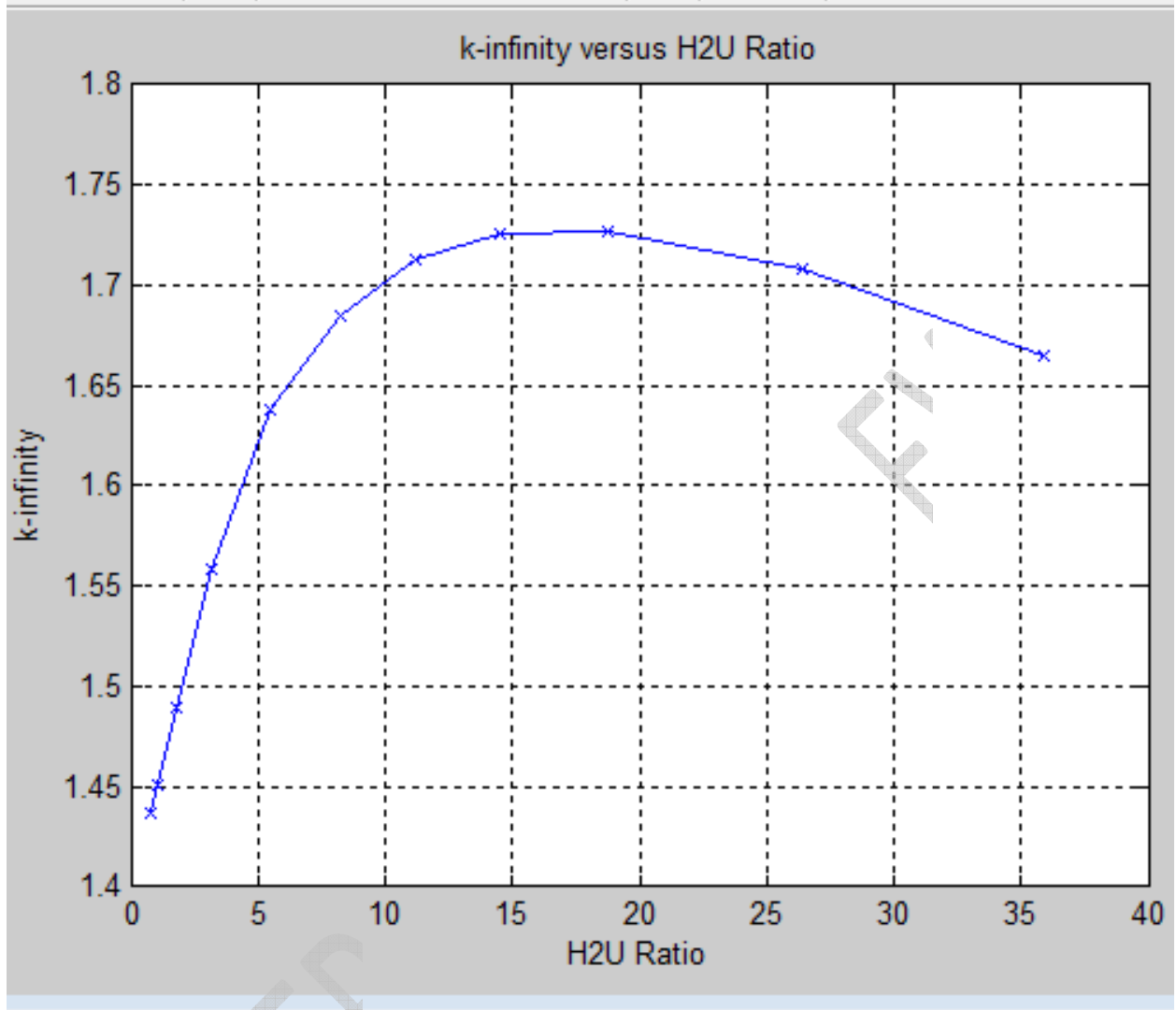
155 Table 1.3: Table for atom density of various nuclides present in cladding material (Zirc4alloy)

Matl name	Nuclide name	Nuclide ID	M_i	$W_i(W/o)$	N_{mix} (atoms/b – cm)
Zircaloy-4	Zirconium	40000	91.224	98.23	4.208e-2
	Tin	50000	118.71	1.45	5.377e-4
	Iron	26000	55.845	0.21	1.780e-4
	Chromium	24000	51.996	0.10	8.339e-5
	Hafnium	72000	178.49	0.01	4.491e-6

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158 Figure 1.0 shows the result of the variation in k-infinity versus hydrogen to uranium ratio for
 159 the LEU core.



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161 This shows that the ratio of hydrogen to uranium in the core of the reactor is increased, the
 162 reactivity also increases by gradually increasing the fuel cell radii till it gets to the peak of
 163 0.6193. Any further increment in the radius of the fuel cell radii, the reactivity of the reactor
 164 decreases as the hydrogen to uranium ratio increases.

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166 **CONCLUSION**

167 The Nigeria Research Reactor -1(NIRR-1) is one of the reactor around the world that require
 168 conversion from HEU to LEU fuel. It is a compact low power nuclear research reactor

169 designed by China Institute of Atomic Energy. Several analyses have been going on around
170 the world on core conversion studies of this type of research reactor.
171 This work contain useful information about the process for the preparation of input for
172 depletion calculation for the Nigeria Research Reactor (NIRR-1) using VENTURE PC code.
173 Most of the data generated in this work can be very useful in explaining the behavior of the
174 proposed 19.75% fueled LEU core for NIRR-1.

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